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## CONDUCTION OF ELECTRICITY THROUGH GASES

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## CONDUCTION OF ELECTRICITY THROUGH GASES

William A Heaton

BY

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### PREFACE.

HAVE endeavoured in this work to develope the view that I the conduction of electricity through gases is due to the presence in the gas of small particles charged with electricity, called ions, which under the influence of electric forces move from one part of the gas to another. My object has been to show how the various phenomena exhibited when electricity passes through gases can be coordinated by this conception rather than to attempt to give a complete account of the very numerous investigations which have been made on the electrical properties of gases; I have therefore confined myself for the most part to those phenomena which furnish results sufficiently precise to serve as a test of the truth of this theory. The book contains the subject-matter of lectures given at the Cavendish Laboratory where a good deal of attention has been paid to the subject and where a considerable number of physicists are working at it.

The study of the electrical properties of gases seems to offer the most promising field for investigating the Nature of Electricity and the Constitution of Matter, for thanks to the Kinetic Theory of Gases our conceptions of the processes other than electrical which occur in gases are much more vivid and definite than they are for liquids or solids; in consequence of this the subject has advanced very rapidly and I think it may now fairly be claimed that our knowledge of and insight into the processes going on when electricity passes through a gas is greater than it is in the case either of solids or liquid. The possession of a charge by the ions increases so much the ease with which they can be traced and their properties studied that as the reader will see we know far more about the ion than we do about the uncharged molecule.

With the discovery and study of Cathode rays, Röntgen rays and Radio-activity a new era has begun in Physics, in which the electrical properties of gases have played and will play a most important part; the bearing of these discoveries on the problems of the Constitution of Matter and the Nature of Electricity is in most intimate connection with the view we take of the processes which go on when electricity passes through a gas. I have endeavoured to show that the view taken in this volume is supported by a large amount of direct evidence and that it affords a direct and simple explanation of the electrical properties of gases.

The pressure of my other duties has caused this book to be a considerable time in passing through the press, and some important investigations have been published since the sheets relating to the subjects investigated were struck off. I have given a short account of these in a few Supplementary Notes.

My thanks are due to Mr C. T. R. Wilson, F.R.S., for the assistance he has given me by reading the proofs and I am indebted to Mr Hayles of the Cavendish Laboratory for the preparation of the diagrams.

J. J. THOMSON.

CAVENDISH LABORATORY, CAMBRIDGE.

August, 1903.

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#### CHAPTER I.

#### ELECTRICAL CONDUCTIVITY OF GASES IN A NORMAL STATE.

- 1. A GAS in the normal state conducts electricity to a slight, but only to a very slight, extent, however small the electric force acting on the gas may be. So small however is the conductivity of a gas when in this state, and so difficult is it to eliminate spurious effects, that there have been several changes of opinion among physicists as to the cause of the leakage of electricity which undoubtedly occurs when a charged body is surrounded by gas. It was thought at first that this leakage took place through the gas; later, as the result of further experiments, it was attributed to defective insulation of the rods or threads used to support the body, and to the dust present in the gas; quite recently however it has been shown that there is a true leak through the gas which is not due to the dust or moisture the gas may happen to contain.
- 2. The escape of electricity from an insulated charged body has attracted the attention of many physicists. Coulomb\*, whose experiments were published in 1785, from his investigations on the loss of electricity from a charged body suspended by insulating strings, came to the conclusion that after allowing for the leakage along the strings there was a balance over, which he attributed to a leakage through the air. He explained this leakage by supposing that the molecules of air when they come into contact with a charged body receive a charge of electricity of the same sign as that on the body and are then repelled from it carrying off some of the charge. We shall see later on that this explanation is not tenable.

<sup>\*</sup> Coulomb, Mémoires de l'Académie des Sciences, 1785, p. 612.

Matteucci\* experimenting on the same subject in 1850 also came to the conclusion that there was a leakage of electricity through the gas; he was the first to prove that the rate at which this leak takes place is less when the pressure of the gas is low than when it is high. He found also that the rate of leak was the same in air, carbonic acid and hydrogen. On the other hand Warburg tound that the rate of leak through hydrogen was only about half of that through air and carbonic acid, he agreed with Matteucci with regard to the equality of the rate of leak through the other two gases and could detect no difference between the leaks through dry and moist air; he confirmed Matteucci's observations on the effect of pressure on the rate of leak. Warburg seemed inclined to suspect that the leak was due to dust in the gases. The belief in dust being the carrier of the electricity was strengthened by an experiment made by Hittorf; in which a small carefully insulated gold leaf electroscope was placed in a glass vessel filled with filtered gas; the electroscope was found to have retained a charge even after the lapse of four days. We know now from recent experiments that the smallness of the leak observed in this case was due to the smallness of the vessel in which the charged body was placed rather than to the absence of dust.

Further experiments on this subject were made by Nahrwold§ and by Narr|| who showed that the rate of leak from a charged hollow sphere was not increased when the temperature of the sphere was raised by filling it with hot water. Boys¶ made an experiment which showed very clearly, that whatever the cause of the leak might be, it was not wholly due to want of insulation in the supports of the charged body; in this experiment he attached the gold leaves of an electroscope first to a short and thick quartz rod and then to a long and thin one, and found that the rate of leak of electricity from the gold leaves was the same in the two cases; if the leak had been along the supports it would have

<sup>\*</sup> Matteucci, Annales de Chimie et de Physique, xxviii. p. 390, 1850.

<sup>+</sup> Warburg, Pogg. Ann. exlv. p. 578, 1872.

<sup>‡</sup> Hittorf, Wied. Ann. vii. p. 595, 1879.

 $<sup>\</sup>$  Nahrwold,  $Wied.\ Ann.\ v.\ p.\ 460,\ 1878$ ; xxxi. p. 448, 1887.

 $<sup>\</sup>parallel$  Narr, Wied. Ann. v. p. 145, 1878; viii. p. 266, 1879; xi. p. 155, 1880; xvi. p. 558, 1882; xxii. p. 550, 1884; xliv. p. 133, 1892.

<sup>¶</sup> Boys, Phil. Mag. xxviii. p. 14, 1889.

been much greater in the first case than in the second. Boys also confirmed Warburg's observation that the rate of leak was the same in dry and moist air.

3. The subject of the electric conduction through air is evidently of considerable importance in relation to Meteorology and Atmospheric Electricity. Experiments especially bearing on this point were made by Linss\* on the loss of electricity from charged bodies placed in the open air; he found there was an appreciable loss of charge which control experiments showed was not due to leakage along the supports of the charged body.

An extensive series of open air measurements were made by Elster and Geitel† in many different localities and in different states of the weather. They found that the rate of leak varied much from time to time and from place to place, that it was very much smaller in mist or fog than when the weather was bright and clear, that it was greater at high altitudes than at low ones, and that on the tops of mountains the rate of escape of negative electricity was much greater than that of positive. This is doubtless due to the negative charge on the earth's surface, a mountain top being analogous to a sharp point on a conductor and thus a place where the earth's electric force is much greater than it is on the plains, where they found the rate of leak to be the same for plus and minus charges. These points are brought out by the results of the observations given in Tables I. and II. Table I. gives the results of experiments made at Wolfenbüttel at different times. Table II. contains observations at different places.

TABLE I.

Weather	Rate of leak for + charge	Rate of leak for – charge
Fog, wind S.E. Clear, air very transparent Fine rain, mist Sky half overcast, air very transparent	3.18	2.64 9.82 3.02 13.83

<sup>\*</sup> Linss, Meteorol. Zeitschr. iv. p. 352, 1887; Elektrotechn. Zeitschr. i. 11, p. 506, 1890.

<sup>+</sup> Elster and Geitel, Drudes Ann. ii. p. 425, 1900.

TABLE II.

Place and altitude	Weather	Rate of leak + charge	Rate of leak - charge	
Brocken,	Sunshine, hazy Sunshine, air clear Sunshine, air very clear Sunshine, air very clear Sunshine No clouds, air clear	6.67 9.66 8.95 3.28 21.02 8.45	10·28 9·52 35·04 31·26 20·78 9·20	

4. Further experiments on the rates of leak from a charged body placed in a closed vessel filled with air were made almost simultaneously by Geitel\* and by Wilson†. The apparatus used by Wilson for this purpose is represented in Fig. 1. Since the

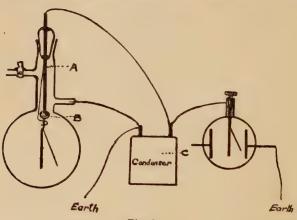


Fig. 1.

quantity of electricity which escapes from the charged body is very small it is necessary that the capacity of the instrument used to measure it should be small; this condition makes it advisable to use a small gold leaf electroscope rather than a quadrant electrometer. To prevent the leakage from the supports vitiating the experiments the brass strip which carries the gold leaf is attached to and insulated from a metal rod A by a piece of

<sup>\*</sup> Geitel, Physikalische Zeitschr. ii. p. 116, 1900.

<sup>+</sup> Wilson, Proc. Camb. Phil. Soc. xi. p. 32, 1900; Proc. Roy. Soc. lxviii. p. 151, 1901.

sulphur B, A being insulated by a plug of sulphur from the vessel containing the gas under examination, and connected with a condenser C formed of parallel plates of metal imbedded in a block of sulphur. The brass strip and gold leaf are initially charged to the same potential as the rod by making momentary contact between the rod and the strip; the rod being connected with a large capacity remains at almost constant potential, and thus if there is any leakage of electricity along the sulphur supporting the brass strip and gold leaf, it will tend to keep them charged and not to discharge them. The position of the gold leaf was read by means of a microscope provided with an eye-piece micrometer scale. The brass strip and gold leaf were used as the charged body and the rate at which the image of the gold leaf moved across the micrometer scale was a measure of the rate of leak through the gas. The following results were obtained by both Geitel and Wilson—the rate of escape of electricity in a closed vessel is much smaller than in the open and the larger the vessel the greater is the rate of leak. The rate of leak does not increase in proportion to the difference of potential between the gold leaves and the walls of the vessel; the rate soon reaches a limit beyond which it does not increase however much the potential difference is increased (provided of course that this is not great enough to cause sparks to pass).

It follows from Wilson's experiments that in dust-free air at atmospheric pressure the maximum quantity of electricity which can escape in one second from a charged body in a closed space whose volume is V cubic centimetres is about  $10^{-8} V$  electrostatic units. Rutherford and Allen\* working in Montreal obtained results in close agreement with this.

As the result of a series of experiments made at pressures ranging from 43 to 743 millimetres of mercury Wilson came to the conclusion that the maximum rate of leak is very approximately proportional to the pressure, thus at low pressures the rate of leak is exceedingly small: this result is illustrated in a striking way by an observation of Crookes† that a pair of gold leaves could retain an electric charge for months in a very high vacuum. The rate of leak is about the same in the dark as it is in the light, it is thus

<sup>\*</sup> Rutherford and Allen, Physikalische Zeitschr. iii. p. 225, 1902.

<sup>+</sup> Crookes, Proc. Roy. Soc. xxviii. p. 347, 1879.

not due to light, and that it can be caused by some invisible form of radiation is rendered improbable by the observation of Wilson that the rate of leak in a closed vessel is the same when the vessel is inside a railway tunnel as when it is outside; in the former case any radiation reaching the gas from outside must have travelled through many feet of solid rock. Wilson\* has recently investigated the greatest rates of leak through different gases and has obtained the following results.

C	Thelet's and a file 1	Relative rate of leak		
Gas	Relative rate of leak	Specific gravity		
air	1.00	1.00		
$H_{\circ}$	·184	2.7		
$\tilde{\mathrm{CO}}_2$	1.69	1.10		
$SO_2^*$	2.64	1.21		
$egin{array}{c} H_2 \\ CO_2 \\ SO_2 \\ CHCl_3 \end{array}$	4.7	1.09		

5. Geitel (loc. cit.) made the very interesting observation that the rate of leak in a closed vessel increases, after the refilling of the vessel with fresh air, for some days, when it reaches a constant value at which it remains for an indefinitely long time. The most obvious explanation of this result is that it is due to the settling down of the dust, as Elster and Geitel (loc. cit.) have shown that the presence of dust, fog, or mist diminishes the rate of leak. This explanation is however rendered doubtful by some later experiments+ made by the same physicists, in which they found that the period required for the gas to attain its maximum conductivity was not appreciably diminished by filtering the dust out of the air by sending it through water, or by extracting the moisture from the gas: thus if the increase in the rate of leak is due to the settling down of some foreign matter from the gas, this matter must be something which can not be got rid of by filtering the gas through water traps or plugs of glass-wool: we shall find later on when we study the diselectrification of gases that there are cases in which foreign matter present in gases is not removed by such treatment, and the case of the discharge of negative electricity from a point (vide infra) shows that under certain conditions the admixture of a very small amount of foreign matter to a gas produces a great diminution in the rate of escape of electricity through it.

<sup>\*</sup> Wilson, Proc. Roy. Soc. lxix. p. 277, 1901.

<sup>†</sup> Elster and Geitel, Physikalische Zeitschr. ii. p. 560, 1901.

6. Another aspect of this phenomenon is the very interesting fact discovered by Elster and Geitel\* that the rate of leak in caves, and cellars where the air is stagnant and only renewed slowly, is very much greater than in the open air: thus in some experiments they made in a cave—the Baumannshöhle in the Harz Mountains—they found that in the cave the electricity escaped at seven times the rate it did in the air outside even when this was clear and free from mist. They found too that in a cellar whose windows had been shut for eight days the rate of leak was very considerably greater than it was in the air outside. These experiments suggest that gas having abnormally great conductivity slowly diffuses from the walls surrounding the gas, and that this diffusion goes on so slowly that when fresh gas is introduced it takes a considerable time for the gas from the walls to again diffuse through the volume. The reader should compare with this phenomenon the results described in the Chapter on Induced Radioactivity.

The experiments we have described show that the rate of leak of electricity through gas in a normal state is influenced by a great variety of circumstances, such as the pressure of the gas, the volume of gas in the electric field, and the amount of dust or fog held in suspension by it; all these effects receive a ready explanation on the view to which we are led by the study of the effects shown on a larger scale by gases whose conductivity has been increased by artificial means, and we shall return to the subject of the leak through normal air after the study of gases whose conductivity has been abnormally increased. We may however at once point out that the increase of the rate of leak with the size of the vessel containing the charged body shows that the conduction is not due, as Coulomb thought, to particles of gas originally uncharged striking against the charged body and receiving a charge which they deliver up to the sides of the vessel; if this were the method by which the electricity escaped the rate of leak would not increase with the size of the vessel.

<sup>\*</sup> Elster and Geitel, Physikalische Zeitschr. ii. p. 560, 1901.

## CHAPTER II.

## PROPERTIES OF A GAS WHEN IN THE CONDUCTING STATE.

- 7. The electrical conductivity of gases in the normal state is so small that as we have seen the proof of its existence requires very careful and elaborate experiments. Gases may however in various ways be put into a state in which they conduct electricity with so much facility that the detection and investigation of this property becomes a comparatively easy matter; as the study of the properties of a gas when in this state is of the highest importance from the light which it throws on the general phenomena of electric discharge through gases we shall find it useful to discuss the subject at some considerable length.
- There are many ways in which gases may be made to possess considerable conductivity or, as we shall express it, be put into the conducting state. They are for instance put into this state when their temperature is raised above a certain point; again, gases drawn from the neighbourhood of flames or electric arcs or which have recently been in contact with glowing metals or carbon, or have diffused from a space through which an electric discharge is passing or has recently passed, are in this state. A gas is put into the conducting state when Röntgen, Lenard or Cathode ravs pass through it, the same effect is produced by the rays from uranium, thorium, or the radioactive substances, polonium, radium, actinium, obtained from pitch-blende by Curie, Curie and Bemont and Debierne respectively, and also as Lenard has recently shown by a very easily absorbed kind of ultra-violet light. mann has shown that electric sparks give out rays, called by him Entladungstrahlen, which produce the same effect. Air which has passed over phosphorus or which has bubbled through water is also in this state and remains so for some time after it has

left the phosphorus or water. We shall have later on to discuss the action of each of these agents in detail, but we shall begin by studying some of the general properties possessed by a gas when in this state, the experimental methods by which these properties may be investigated, and a theory of this state by which they may be explained.

9. A gas when in the conducting state possesses characteristic properties. In the first place it retains its conductivity for some little time after the agent which made it a conductor has ceased to act; its conductivity however always diminishes, in some cases very rapidly, after the agent is removed, and finally it disappears. The duration of the conductivity may be shown very simply by having a charged electroscope screened off from the direct action of Röntgen rays, the electrostatic field due to the electroscope being screened off from the region exposed to the rays by covering the electroscope with a cage made of wire gauze with a very large mesh; if the air is still the electroscope will retain its charge even when the rays are in action, but if we blow some of the air traversed by the rays towards the electroscope the latter will begin to lose its charge, showing that the air has retained its conductivity for the time taken by it to travel to the electroscope from the place where it was exposed to the rays. A somewhat more elaborate form of this experiment, which enables us to prove several other interesting properties of the conducting gas, is to place the electroscope in a glass vessel A in which there are two tubes, one leading to a water-pump while the end of the other is in the region traversed by the Röntgen rays. The tube used to produce the rays

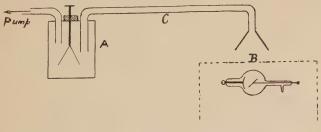


Fig. 2.

is placed in a box covered with lead with the exception of a window at B to let the rays through: this shields the electroscope from the direct action of the rays: if the water-pump be worked slowly so as to make a slow current of air pass from the region traversed by the rays into the vessel A the electroscope will gradually lose its charge whether this be positive or negative: if the pump be stopped and the current of air ceases, the discharge of the electroscope will cease.

The conducting gas loses its conductivity if it is sucked through a plug of glass-wool or made to bubble through water\*. This can readily be proved by inserting in the tube B a plug of glass-wool or a water-trap and working the water-pump a little harder so as to make the rate of flow of air through the tube the same as in the previous experiment; it will now be found that the electroscope will retain its charge, the conductivity has thus been taken out of the gas by filtering it through glass-wool or water. The conductivity is very much more easily removed from gases made conducting by the various rays, Röntgen, Lenard, Cathode, &c., than from the conducting gases derived from flames and arcs; the latter as we shall see require a great deal of filtering to remove their conductivity. If we replace the tube B by a metal tube of fine bore we shall find that the gas loses its conductivity by passing through it, and the finer the bore the more rapidly does the conductivity disappear. The conductivity may also be removed from the gas by making it traverse a strong electric field so that a current of electricity passes through it +. To show this, replace the glass tube C by a metal tube of fairly wide bore and fix along the axis of this tube an insulated metal wire; if there is no potential difference between the wire and the tube, then the electroscope in A will leak when a current of air is sucked through the apparatus; if however a considerable difference of potential is established between the wire and the tube, so that a current of electricity passes through the gas during its passage to A, the leak of the electroscope will cease, showing that the conductivity of the gas has been removed by the electric field.

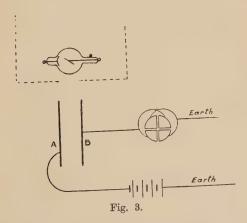
10. The removal of the conductivity by filtering through glass-wool or water and by transmission through narrow metal tubes, shows that the conductivity is due to something mixed

† Ibid.

<sup>\*</sup> J. J. Thomson and E. Rutherford, Phil. Mag. xlii. p. 392, 1896.

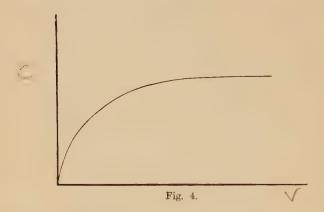
with the gas, this something being removed from the gas in the one case by filtration in the other by diffusion to the walls of the tube. Further the removal of the conductivity by the electric field shows that this something is charged with electricity and moves under the action of the field; since the gas when in the conducting state shows as a whole no charge of electricity, the charges removed must be both positive and negative. We are thus led to the conclusion that the conductivity of the gas is due to its having mixed with it electrified particles, some of these particles having charges of positive electricity others of negative. We shall call these electrified particles ions, and the process by which a gas is made into a conductor the ionisation of the gas. We shall show later on how the masses and charges of the ions may be determined, when it will appear that the ions in a gas are not identical with those met with in the electrolysis of solutions.

11. The passage of a current of electricity through a conducting gas does not follow Ohm's law unless the electromotive force acting on the gas is small. We may investigate the relation between the current and potential difference by taking two parallel metal plates A and B (Fig. 3) immersed in a gas, the gas between the



plates being exposed to the action of some ionising agent such as Röntgen rays or the radiation from a radioactive substance. One of the plates A is connected with one of the pairs of quadrants of an electrometer, the other pair of quadrants being put to earth. The other plate B is connected with one of the terminals of a

battery of several storage cells, the other terminal of the battery being connected with the earth; initially the two pairs of quadrants of the electrometer are connected together, then the connection between the quadrants is broken and as a current of electricity is passing across the air space between A and B, the plate B gets charged up and the needle of the electrometer is deflected; the rate of deflection of the electrometer measures the current passing through the gas. By making a series of observations of this kind we can get the means of drawing a curve such that the ordinates represent the current through the gas and the abscissæ the potential difference between the plates: such a curve is represented in Fig. 4\*. We see that when the difference of



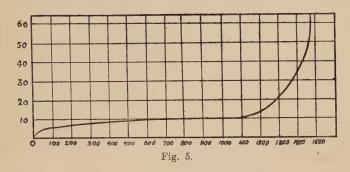
potential is small the curve is a straight line, in this stage the conduction obeys Ohm's law; the current however soon begins to increase more slowly than the potential difference and we reach a stage where there is no appreciable increase of current when the potential difference is increased: in this stage the current is said to be saturated. When the potential difference is increased to such an extent that the electric field is strong enough to ionise the gas, another stage is reached in which the current increases very rapidly with the potential difference; curves showing this effect have been obtained by von Schweidler† and by Townsend‡, one of these is shown in Fig. 5. The potential gradient required

<sup>\*</sup> J. J. Thomson, Nature, April 23, 1896.

<sup>+</sup> von Schweidler, Wien. Bericht, cviii. p. 273, 1899.

<sup>‡</sup> J. S. Townsend, Phil. Mag. vi. 1, p. 198, 1901.

to reach this stage depends upon the pressure of the gas, it is directly proportional to the pressure; for air at atmospheric pressure



it is about 30,000 volts per centimetre, so that in air at a pressure of one millimetre a potential gradient of about 40 volts per centimetre would be sufficient to reach this stage.

- 12. The saturation current between two parallel plates of given area depends upon the amount of ionisation between the plates; if the ionisation takes place throughout the whole volume of gas between the plates, then the greater the distance between the plates the greater is the saturation current, so that if we use constant potential differences large enough to produce saturation, the greater the distance between the plates the larger is the current. Thus the behaviour of the conducting gas is very different from that of a metallic or liquid electrolytic conductor, for if such conductors were substituted for the gas the greater the distance between the plates the smaller would be the current. Under very small potential differences however the three classes of conductors would behave in the same way.
- 13. The peculiarities shown by the conduction through gases are very easily explained on the assumption that the conduction is due to ions mixed with the gas. Let us for example take the case of saturation. Suppose that in the gas between the plates the ionising agent produces in one second q positive and q negative ions and let e be the magnitude of the electric charge on an ion, then if an electric current i passes between the plates i/e positive ions are driven against the negative electrode, and the same number of negative ions are driven against the positive electrode in one

second; thus in each second i/e positive and negative ions are taken out of the gas by the current. When the gas is in a steady state the number of ions taken out of it in a given time cannot be greater than the number of ions produced in it in the same time, hence i/e cannot be greater than q, and thus i cannot be greater than qe: qe is thus the value of the saturation current. If the ions are produced uniformly throughout the gas, and if  $q_0$ is the number of ions produced in one second in unit volume, then since the volume of gas between the plates is equal to Al, where A is the area of one of the plates and l the distance between the plates, q the number of ions produced in the gas in one second is equal to  $q_0Al$ ; hence the saturation current is equal to  $q_0Ale$ , and is thus proportional to the distance between the plates. This relation between the saturation current and the distance between the plates has been verified by measurements of the saturation currents through gases exposed to Röntgen rays\*.

14. Even when there is no current of electricity passing through the gas and removing some or all of the ions, the number of ions present in the gas does not increase indefinitely with the time which has elapsed since the gas was first exposed to the ionising agent; the number of ions in the gas and therefore its conductivity acquire after a time steady values beyond which they do not increase however long the ionising agent may act. This is due to the recombinations that take place between the positive and negative ions; these ions moving about in the gas sometimes come into collision with each other and in a certain fraction of such cases of collision the positive and negative ions will remain together after the collision, and form an electrically neutral system the constituents of which have ceased to be free ions. The collisions will thus cause the ions to disappear, and the steady state of a gas which is not carrying an electric current will be reached when the number of ions which disappear in one second as the result of the collisions is equal to the number produced in the same time by the ionising agent. Starting from this principle it is very easy to investigate the relation between the number of free ions when the gas is in a steady state, the strength of the ionising agent. the rate at which the ions increase on the first exposure to the

<sup>\*</sup> J. J. Thomson and E. Rutherford, Phil. Mag. v. 42, p. 392, 1896.

ionising agent and the rate at which they die away when the ionising agent is cut off.

For let q be the number of ions (positive or negative) produced in one cubic centimetre of the gas per second by the ionising agent;  $n_1$ ,  $n_2$  the number of free positive and negative ions respectively per cubic centimetre of the gas. The number of collisions per second between positive and negative ions is proportional to  $n_1n_2$ . If a certain fraction of the collisions result in the formation of a neutral system the number of ions which disappear per second in a cubic centimetre will be equal to  $\alpha n_1 n_2$ , where  $\alpha$  is a quantity which is independent of  $n_1$  and  $n_2$ ; hence we have

$$\frac{dn_1}{dt} = q - \alpha n_1 n_2$$

$$\frac{dn_2}{dt} = q - \alpha n_1 n_2$$
(1).

Thus  $n_1 - n_2$  is constant, so that if the gas is uncharged to begin with  $n_1$  is always equal to  $n_2$ . Putting  $n_1 = n_2 = n$  the preceding equation becomes

$$\frac{dn}{dt} = q - \alpha n^2 \dots (2),$$

the solution of which is, if  $k^2 = q/\alpha$ ,

$$n = k \frac{(\epsilon^{2kat} - 1)}{\epsilon^{2kat} + 1} \dots (3);$$

 $n_0$  the value of n when the gas is in a steady state is obtained by putting t equal to infinity in equation (3) and is given by the equation

 $n_{\scriptscriptstyle 0} = k = \sqrt{\frac{q}{\alpha}} \,.$ 

We see from equation (3) that the gas will not approximate to a steady state until t is large compared with  $1/2k\alpha$ , that is with  $1/2n_0\alpha$  or  $1/2\sqrt{q\alpha}$ . We may thus take  $1/2\sqrt{q\alpha}$  as the measure of the time taken by the gas to reach the steady state under exposure to the ionising agent; as this time varies inversely as  $\sqrt{q}$  we see that when the ionisation is feeble it may take a very considerable time for the gas to reach the steady state.

Thus at some distance, say a metre, from an ordinary Röntgen bulb it may require an exposure of a minute or two to bring the gas into a steady state. We may use equation (2) to determine the rate at which the number of ions diminishes when the ionising agent is removed, putting q = 0 in that equation we have

$$\frac{dn}{dt} = -\alpha n^2 \dots (4),$$

hence

$$n = \frac{n_0}{1 + n_0 \alpha t} \dots (5),$$

where  $n_0$  is the value of n when t = 0. Thus the number of ions falls to one-half its initial value in the time  $1/n_0\alpha$ . We may regard equation (4) as expressing the fact that a free ion lasts for a time which on the average is equal to  $1/\alpha n$ .

Equation (4) has been verified by Rutherford for gases exposed to Röntgen rays\* and to the radiation from uranium+, by McClungt for gases exposed to Röntgen rays, and by McClelland for the case of gases drawn from the neighbourhood of flames and arcs. Two methods have been employed for this In one method air exposed to rays at one end of a long tube is slowly sucked through the tube, and the saturation currents measured at different parts along the tube. These currents are proportional to the value of n at the place of observation, and knowing the velocity of the air and the distance of the place of observation from the end of the tube, we know the time which has elapsed since the gas was ionised; we can thus find the values of n corresponding to a series of values of t; values determined in this way were found by Rutherford to agree well with those given by equation (5). This method can only be used when a large quantity of gas is available. Another method also used by Rutherford can be employed even for gases of which only small quantities can be procured. In this method gas confined in a vessel is exposed to the action of an ionising agent such as the Röntgen rays. Inside the vessel are two parallel metal plates A and B between which the ionisation is to be measured, (in some of Rutherford's experiments one of these plates was replaced by the case of the vessel which was made a conductor by lining it

<sup>\*</sup> Rutherford, Phil. Mag. v. 44, p. 422, 1897.

<sup>†</sup> Rutherford, Phil. Mag. v. 47, p. 109, 1899.

<sup>#</sup> McClung, Phil. Mag. vi. 3, p. 283, 1902.

 $<sup>\</sup>$  McClelland, Phil. Mag. v. 46, p. 29, 1898.

with wire gauze, the other plate was replaced by an insulated wire running down the middle of the vessel). One of these plates A can be connected with an electrometer, the other B with one terminal of a large storage battery the other terminal of which is kept to earth. A pendulum interrupter is arranged so that as a heavy pendulum swings it strikes against levers, and by this means makes or breaks various connections. While the vessel is under the influence of the rays, A and B are connected together and to earth, then A is disconnected from both earth and electrometer and left insulated, and B is disconnected from the earth; the pendulum is then let go: as it falls it first breaks the current going through the primary of the induction coil used to excite the rays, it thus stops the ionisation, then after an interval t (which can easily be varied) it strikes against another lever which has the effect of connecting B with the high potential pole of the battery, thus producing a strong electric field between the plates A and B: this field, if B is charged positively, drives in a very small fraction of a second all the positive ions which exist between A and B against A, so that A receives a positive charge proportional to n; the pendulum in its swing then goes on to disconnect B from the battery and connects it to earth. The plate A is now connected with the electrometer the needle of which is deflected by an amount proportional to the charge on the plate A, i.e. to n. By adjusting the apparatus so as to alter the time which elapses between cutting off the rays and connecting B with the battery we find a series of corresponding values of n and t; these were found by Rutherford to fit in well with the relation indicated by equation (5). The following table shows the rate at which the ionisation dies away in a special case, the rate of course depends upon the intensity of the ionisation, the figures may however serve to give an idea of the order of magnitude of the rate of decay in air under strong Röntgen radiation.

Time in seconds after	Deflection of
stoppage of rays	Electrometer
·004	184
·08	183
•45	106 37
4	19

Thus after 4 seconds there was still a very appreciable amount of ionisation in the gas. The duration is still more marked in the following example when the radiation was much weaker. The electrometer was not equally sensitive in the two series of experiments.

Time	Deflection
·004	174
·45	139
2	107
4	54
8	30
16	16

Thus after 16 seconds in this case the gas retained more than 10 per cent. of its ionisation.

Rutherford measured the rate of decay in various gases exposed to Röntgen rays of as nearly as possible the same intensity. The results are shown in the following table, the first column contains the name of the gas, the second T the time taken for the ionisation to sink to one-half of its original value, we have seen that  $T = 1/n_0 \alpha = 1/\sqrt{q\alpha}$ ; the third column contains relative values of q, and the fourth column the relative values of  $\alpha$  calculated from the values of T and q.

Gas	T	q	α
Hydrogen	·65	*5	4·8
	·3	1	11
	·35	11	·75
	·51	1.2	3·3
	·45	4	1·25
	·18	18	2

16. Rutherford showed that the value of T was very much diminished when any dust was present in the gas, the dust did not however affect the saturation current. Thus for example when chlorine was first admitted to the testing vessel the value of T was '19 seconds, after standing for an hour T rose to about '3 seconds

although there was no change in the saturation current. Again for air which had been standing overnight T was about 1 second, when a little dusty air was blown into the vessel T fell to 15 seconds, rising to about '5 seconds in about 10 minutes; it took several hours for T to rise to its original value. Again T was found to be increased by filtering the gas through cotton-wool. The effect produced by dust is easily explained, as the dust particles are in all probability very large compared with the ions, thus if a positive ion strikes against a dust particle and sticks to it, it forms a large system which is much more likely to be struck by a negative ion and neutralised than if the positive ion had remained free; in this way the presence of dust will facilitate the recombination of the ions. The presence of dust in Rutherford's experiments probably explains the discrepancy between his results and Townsend's\*, who used dust-free gases and determined α by the first of the methods described, care being taken that the tubes through which the ionised gases were sucked were so large that the loss of ions from diffusion to the sides of the tube could be neglected in comparison with those lost by recombination. Townsend found that for air, oxygen, carbonic acid, and hydrogen α had the values, 3420e, 3380e, 3500e, and 3020e, where e is the charge on the ion in electrostatic units. We shall see that e is about  $3.5 \times 10^{-10}$  so that  $\alpha$  for air, oxygen, and carbonic acid is about  $1.2 \times 10^{-6}$  while for hydrogen it is about 15 per cent, less. In Rutherford's experiments the value of α for air was about three times that for carbonic acid but it is probable that the gases in this case were not really dust-free.

17. A series of careful measurements of  $\alpha$  under different conditions would give us valuable information as to the nature of the ions; from some preliminary experiments made by Dr Nabl at the Cavendish Laboratory it would seem that  $\alpha$  is but little if at all affected by changes in pressure. Some recent experiments by M°Clung† have shown that  $\alpha$  is independent of the pressure, the pressures investigated varying from 125 to 3 atmospheres. The values found for  $\alpha$  are for air and carbonic acid 3384 × e and for hydrogen 2938 × e; no experiments seem to have yet been made on the variation of  $\alpha$  with temperature.

<sup>\*</sup> Townsend, Phil. Trans. A. 193, p. 129, 1900.

<sup>†</sup> McClung, Phil. Mag. vi. 3, p. 283, 1902.

## Diffusion of Ions.

In addition to the loss of ions arising from the recombination of the positive and negative ions there will be a further loss due to the diffusion of ions to the sides of the vessel. Thus suppose the ionised gas is contained in a metal vessel, then when the ions come in contact with the sides of the vessel their charges are neutralised by the opposite charge induced on the metal and they thus cease to act like ions; the layer of gas next the sides of the vessel is thus denuded of ions, which exist in finite numbers in the gas in the interior; a gradient in the concentration is thus established and the ions diffuse from the interior to the boundary. The problem is closely analogous to that of the absorption of water vapour in a vessel whose sides are wet with sulphuric acid. We shall begin by considering the theory of a very simple case, that of ionised gas contained between two parallel metal plates at right angles to the axis of x. Let n be the number of positive ions per cubic centimetre, q the number of ions produced by the ionising agent per second in a cubic centimetre of the gas, D the coefficient of diffusion of the positive ions through the gas, m the number of negative ions per cubic centimetre, then we see that in consequence of diffusion the rate of increase in the number of positive ions per cubic centimetre is equal to  $D\frac{d^2n}{dx^2}$ : assuming that the surfaces of equal density of the ions are planes at right angles to the axis of x. Thus taking recombination and external ionisation into account as well as diffusion we have

$$\frac{dn}{dt} = q + D \frac{d^2n}{dx^2} - \alpha nm,$$

and when things are in a steady state,

$$q + D\frac{d^2n}{dx^2} - \alpha nm = 0.$$

Let us consider the special case when the plates are so near together that the loss of ions from diffusion far exceeds that from recombination, then we have

$$q + D \frac{d^2n}{d\sigma^2} = 0$$
 .....(1).

If we take the plane midway between the metal plates as the plane x = 0, and if l is the distance between the plates, then the conditions to be satisfied by n are n = 0 when  $x = \pm l$ ; the solution of equation (1) with these conditions is

$$n = \frac{1}{2} \frac{q}{D} (l^2 - x^2) \dots (2).$$

The total number of free positive ions between the plates is equal to

 $\int_{-l}^{+l} n \, dx,$ 

and this by equation (2) is equal to

 $\frac{2}{3}\frac{q}{\bar{D}}l^3$ .

We see from this result how we can measure D. For, if we cut off the rays and apply a strong electric field between the plates, we shall drive all the positive ions against the plate at the lower potential, so that this plate will receive a charge of electricity equal to  $\frac{2}{3} \frac{q}{D} l^3 e$ , where e is the charge on an ion; if this plate is connected with an electrometer we can measure its charge, which will be proportional to the deflection  $\delta_1$  of the electrometer. If the rays are kept on and the field is intense enough to produce the saturation current, the charge received by the plate in one second is equal to 2qle, hence if  $\delta_2$  is the deflection of the electrometer in one second in this case, we see that

$$\delta_1 = \frac{1}{3} \frac{l^2}{\overline{D}} \delta_2,$$

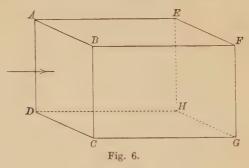
an equation which enables us to determine D.

We have in this investigation neglected the effect of recombination; it is necessary to verify that the plates are sufficiently close together to make this justifiable. An easy way of doing this is as follows: the total number of ions on the hypothesis that the only source of loss of ions is recombination is equal to  $2l\sqrt{q/\alpha}$ , (see p. 15); the number on the assumption that the loss is entirely due to diffusion is as we have just seen  $\frac{2}{3}\frac{q}{D}l^3$ , hence

if  $\frac{2}{3}\frac{q}{D}l^3$  is small compared with  $2l\sqrt{\frac{q}{a}}$  the loss of ions from

diffusion will be large compared with the loss by recombination, and we shall be justified in neglecting the latter.

19. The coefficients of diffusion of the ions in air, oxygen, hydrogen and carbonic acid gas have been determined by Townsend\* by a different method; ionised air being sucked through very narrow tubes and the loss of ions suffered in passing through a known length of tubing determined. The theory of the method is as follows: ionised gas is sent through a metal tube the axis of which is taken as the axis of z, the gas moving parallel to z and being free from the action of any ionising agent in its course through the tube. Consider the state of things in a small volume ABCDEFGH: this volume loses ions by diffusion, and gains them by the gas entering the volume through the face ABCD



being richer in ions than that leaving it through the face EFGH, when the gas is in a steady state the rates of loss and gain of ions must be equal. If n is the number of ions per cubic centimetre, D the coefficient of diffusion of the ions through the gas, the rate of loss of ions from diffusion is equal to

$$-D\left(\frac{d^2n}{dx^2} + \frac{d^2n}{dy^2} + \frac{d^2n}{dz^2}\right).$$

If v is the velocity of the gas, the rate of gain of ions from the second cause is equal to

 $-\frac{d}{dz}(vn),$ 

or, since v does not depend upon z, to

$$-v\frac{dn}{dz}$$
.

<sup>\*</sup> Townsend, Phil. Trans. A. 193, p. 129, 1900.

Hence equating the loss and the gain we get

$$D\left(\frac{d^2n}{dx^2} + \frac{d^2n}{dy^2} + \frac{d^2n}{dz^2}\right) = v \frac{dn}{dz} \dots (1).$$

In the experiments the term  $D\frac{d^2n}{dz^2}$  was very small compared with  $v\frac{dn}{dz}$ ;  $\frac{1}{n}\frac{dn}{dz}$  being of the order 1/20, v of the order 100 and D about 03 so that vn was about 70,000 times  $D\frac{dn}{dz}$ . Neglecting  $D\frac{d^2n}{dz^2}$  and taking the case of a cylindrical tube of radius a symmetrical about the axis

$$\frac{d^2n}{dx^2} + \frac{d^2n}{dy^2} = \frac{d^2n}{dr^2} + \frac{1}{r}\frac{dn}{dr},$$

where r is the distance of a point from the axis of the tube. Now  $v = \frac{2V}{a^2}(a^2 - r^2)$ , where  $V\pi a^2$  is the volume of gas passing per second through each cross-section of the tube; substituting these values in equation (1) and neglecting  $d^2n/dz^2$  we get

$$\frac{d^{2}n}{dr^{2}} + \frac{1}{r}\frac{dn}{dr} - \frac{2V}{Da^{2}}(a^{2} - r^{2})\frac{dn}{dz} = 0 \quad \dots (2).$$

The conditions to be satisfied by n are that n=0 when r=a for all values of z, and that if the ionised gas enters the tube at z=0,  $n=n_0$  a constant, when z=0, for all values of r.

To solve this equation put  $n = \phi e^{-\frac{\theta D a^2 z}{2V}}$  where  $\phi$  depends only upon r and  $\theta$  is a constant to be subsequently determined; substituting this value of n in equation (2) we get

$$\frac{d^2\phi}{dr^2} + \frac{1}{r}\frac{d\phi}{dr} + \theta (a^2 - r^2) \phi = 0 \dots (3).$$

$$\phi = 1 + B_1 r^2 + B_2 r^4 + B_3 r^6 + \dots,$$

and we get from (3)

Put

$$4B_1 + \theta a^2 = 0,$$

$$16B_2 + \theta a^2 B_1 - \theta = 0,$$

$$36B_3 + \theta a^2 B_2 - \theta B_1 = 0,$$

thus the first three terms in  $\phi$  are

$$1 - \frac{\theta a^2}{4} r^2 + \frac{1}{16} \left( \theta + \frac{\theta^2 a^4}{4} \right) r^4 \dots (4).$$

We have to choose such values of  $\theta$  that  $\phi = 0$  when r = a, let these values be  $\theta_1, \theta_2...$  and let  $\phi_1, \phi_2$  be the values of  $\phi$  when these values of  $\theta$  are substituted in equation (4); then we may write

$$n = c_1 \phi_1 \epsilon^{-\frac{\theta_1 D \alpha^2 z}{2V}} + c_2 \phi_2 \epsilon^{-\frac{\theta_2 D \alpha^3 z}{2V}} + c_3 \phi_3 \epsilon^{-\frac{\theta_3 D \alpha^2 z}{2V}} + \dots (5).$$

To find the values of  $c_1$ ,  $c_2$ ,  $c_3$ ... we have the condition  $n = n_0$  a constant when z = 0. Hence

$$n_0 = c_1 \phi_1 + c_2 \phi_2 + c_3 \phi_3 + \dots (6).$$

Now from the differential equation (3) we can easily prove the following relations

$$\int_{0}^{a} \phi_{n} \phi_{m} (a^{2} - r^{2}) r dr = 0 \text{ when } n \text{ and } m \text{ are different } \dots (7),$$

$$\int_{0}^{a} \phi_{n^{2}} (a^{2} - r^{2}) r dr = a \left[ \frac{d\phi_{n}}{d\theta_{n}} \frac{d\phi_{n}}{dr} \right]^{r=a} \dots (8),$$

$$\int_{0}^{a} \phi_{n} (a^{2} - r^{2}) r dr = -\frac{a}{\theta_{n}} \left[ \frac{d\phi_{n}}{dr} \right]^{r=a} \dots (9).$$

Multiplying both sides of equation (6) by  $\phi_n(a^2 - r^2)r$  and integrating from r = 0 to r = a we obtain by the aid of equations (7), (8) and (9)

$$c_n = -\frac{n_0}{\theta_n \left[\frac{d\phi_n}{d\theta_n}\right]^{r=a}},$$

hence

$$n = -n_0 \left\{ \frac{\phi_1}{\theta_1 \left[ \frac{d\phi_1}{d\theta_1} \right]^{r=a}} e^{-\frac{\theta_1 D a^2 z}{2V}} + \frac{\phi_2}{\theta_2 \left[ \frac{d\phi_2}{d\theta_2} \right]^{r=a}} e^{-\frac{\theta_2 D a^2 z}{2V}} + \ldots \right\} \dots (10).$$

The number of ions which pass across the section of the tube when z=0 is  $n_0\pi a^2V$ , the quantity which pass across a section of the tube at a distance z from the origin is equal to

$$\int_0^a n \frac{2V}{a^2} (a^2 - r^2) r \, dr,$$

this by equations (7), (9) and (10) is equal to

$$\frac{4\pi \, V n_0}{a} \left\{ \frac{1}{\theta_1^2} \left[ \frac{\frac{d\phi_1}{dr}}{\frac{d\phi_1}{d\theta_1}} \right]^{r=a} e^{-\frac{\theta_1 D a^2 z}{2\, V}} + \frac{1}{\theta_2^2} \left[ \frac{d\phi_2}{\frac{dr}{d\phi_2}} \right]^{r=a} e^{-\frac{\theta_2 D a^2 z}{2\, V}} + \ldots \right\}.$$

The two smallest roots of the equation  $\phi = 0$  were found by Townsend to be  $\theta_1 a^4 = 7.313$  and  $\theta_2 a^4 = 44.56$ , corresponding to these roots we have

$$\begin{split} &\frac{1}{\theta_1 a^3} \left[ \frac{d\phi_1}{dr} \right]^{r=a} = \cdot 1321 \; ; \quad \frac{1}{\theta_2 a^3} \left[ \frac{d\phi_2}{dr} \right]^{r=a} = \cdot 0302 ; \\ &\frac{1}{a^4} \left[ \frac{d\phi_1}{d\theta_1} \right]^{r=a} = \cdot 0926 \; ; \quad \frac{1}{a^4} \left[ \frac{d\phi_2}{d\theta_2} \right]^{r=a} = \cdot 0279 . \end{split}$$

Hence substituting these values we find that the ratio of the number of ions which pass a cross-section of the tube at a distance z from the origin to the number which pass through the tube at the origin is equal to

$$4 \left\{ 1952 e^{-\frac{7 \cdot 313 Dz}{2a^2 V}} + 0243 e^{-\frac{44 \cdot 56 Dz}{2a^2 V}} + \ldots \right\}.$$

If  $c_1$  is the saturation current through the gas after leaving a tube of length  $l_1$ ,  $c_2$  that after leaving a tube of length  $l_2$ , then since the saturation currents are proportional to the numbers of ions given to the gas per second, we have

$$\frac{c_1}{c_2} = \frac{\cdot 1952\epsilon^{-\frac{7\cdot313Dl_1}{2a^2V}} + \cdot 0243\epsilon^{-\frac{44\cdot56Dl_1}{2a^2V}}}{\cdot 1952\epsilon^{-\frac{7\cdot313Dl_2}{2a^2V}} + \cdot 0243\epsilon^{-\frac{44\cdot56Dl_2}{2a^2V}}}....(11).$$

Now  $c_1/c_2$  can be determined by experiment, and hence from equation (11) the value of D can be determined. The method used by Townsend to solve this equation was a graphical one; putting  $y = c_1/c_2$ ,  $x = \frac{7 \cdot 313 D l_1}{2a^2 V}$ , the curve representing the relation

(11) between y and x was drawn by calculating a number of corresponding values: when this curve had been obtained the value of  $7.313Dl_1/2a^2V$  corresponding to any value of  $c_1/c_2$  obtained by experiment could be found, and hence D determined as l, a and V are known.

The apparatus used to measure the value of  $c_1/c_2$  is represented in Fig. 7. A is a brass tube 50 cm. long, 3·2 cm. in diameter, provided with an aluminium window W through which the Röntgen rays which ionise the gas pass. C is another brass tube 17 cm. long fitting accurately into A and able to slide along it. E is an electrode which is connected to a metal rod F passing through an ebonite plug. A series of fine wires were soldered parallel to one another and 2 mm. apart across the end of the

tube C. The gas entered the apparatus through the glass tube G and then before reaching the electrode passed through the tubes T.

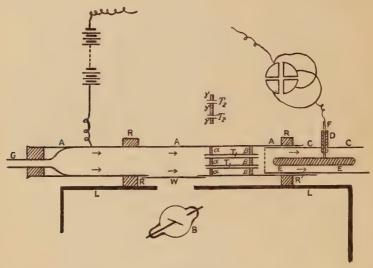


Fig. 7.

These were twelve tubes 10 cm. long and 3 cm. in diameter, arranged at equal intervals and all at the same distance from the axis of the tube A; they were soldered into holes bored into two brass discs  $\alpha$  and  $\beta$  which fitted so closely into Athat gas could not pass between the disc and the tube. Another set of twelve tubes only 1 cm. long and 3 cm. in diameter were fused into another disc y. The tube A was insulated by the two ebonite rings R, R'. The potential of the tube was raised to 80 volts by connecting it with one of the terminals of a battery of small storage cells, the other terminal of which was connected with the earth. The electrode E was connected with one pair of quadrants of an electrometer, the other pair of quadrants being kept to earth. A uniform and measurable stream of gas was supplied by a gasometer, this gas was ionised by the Röntgen rays as it passed through the tube, some of the ions were lost by diffusion to the sides, all the positive ones which escaped were driven against the electrode E; thus the charge on the electrometer measured the number of positive ions which got through the tubes. charging the tube A up negatively, the negative ions could be driven against the electrode, and the number of those which get through the tubes determined. After a series of measurements had been made with the long tubes, these were replaced by the short ones, and a similar series of measurements gone through. These measurements, as was explained in the preceding theory, give us the data for calculating the coefficient of diffusion of the ions. For gases other than air, a somewhat different form of apparatus was used, for a description of which we must refer to the original paper.

The loss of ions even in the narrow tubes is not entirely due to diffusion to the sides of the tube, a part, though only a small part, of the loss will be due to the recombination of the ions. To estimate how much was due to this effect, the small tubes T were removed and the deflection of the electrometer observed when the tube C was placed at different distances from the place where the gas is ionised; in a wide tube such as A the loss from diffusion to the sides is negligible, and the smaller deflection of the electrometer when the electrode E is moved away from the place of ionisation is due to the loss of ions by recombination. By making measurements at different distances and knowing the velocity of the gas we can measure in this way the amount of recombination taking place in a given time and hence determine the value of a, the constant of recombination. It was in this way that the values of α given on page 19 were determined. Knowing α it is easy to calculate the loss of ions from recombination in their passage through the narrow tubes, and then to apply a correction to the observations so as to get the loss due to diffusion alone.

The following tables give the velocities of the coefficients of diffusion on the c.g.s. system of units as deduced by Townsend from his observations.

TABLE I. COEFFICIENTS OF DIFFUSION IN DRY GASES.

Gas	D for + ions	D for - ions	$\begin{array}{c} \text{Mean value} \\ \text{of } D \end{array}$	Ratio of D for - to D for + ions
Air	·028	*043	·0347	1·54
Oxygen	·025	*0396	·0323	1·58
Carbonic acid	·023	*026	·0245	1·13
Hydrogen	·123	*190	·156	1·54

TABLE II. COEFFICIENTS OF DIFFUSION IN M	Moist	GASES.
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Gas	D for + ions	D for - ions	$\begin{array}{c} \text{Mean value} \\ \text{of } D \end{array}$	Ratio of D for - to + ions
Air	·032	*035	*0335	1·09
	·0288	*0358	*0323	1·24
	·0245	*0255	*025	1·04
	·128	*142	*135	1·11

We see from these tables that the coefficient of diffusion for the negative ions is greater than that for the positive, the difference being much more marked in dry than in damp gases. The superior mobility of the negative ions was first observed by Zeleny\* who measured by a method which we shall shortly describe the velocity of the ions when placed in an electric field, and found that the negative ions moved faster than the positive ones. The more rapid diffusion of the negative ions explains why in certain cases ionised gas, originally electrically neutral, acquires a charge of positive electricity. Thus, for example, if such a gas is blown through metal tubes, the gas emerging from the tubes will be positively electrified, as in the passage through the tubes it has lost more negative than positive ions. Zeleny (loc. cit.) has shown that this effect does not occur with carbonic acid gas in which the velocities of the two ions are very nearly equal. Some experiments made by Rutherford† seem to show that in addition to the effect produced by diffusion, there is a specific effect due to the metal, as he found that the excess of positive over negative ions was greater when the ionised gas passed through zinc tubes than when it passed through copper. The difference in the rate of diffusion of the positive and negative ions causes a certain amount of electrical separation to take place when a gas is ionised; as the negative ions diffuse more rapidly than the positive ones, the region where ionisation takes place will have an excess of positive ions and be positively electrified, while in consequence of the diffusion of the negative ions the surrounding regions will have an excess of these ions and will therefore be negatively electrified.

<sup>\*</sup> Zeleny, Phil. Mag. v. 46, p. 120, 1898.

<sup>†</sup> Rutherford, Phil. Mag. v. 43, p. 241, 1897.

The results given in Tables I. and II. show that the excess of the velocity of diffusion of the negative ions over that of the positive is much greater when the gas is dry than when it is moist; the effect of moisture on the velocity of diffusion is very remarkable, the results quoted in the table show that with the exception of ions in carbonic acid (where there is but little difference between the velocities of diffusion of positive or negative ions in either wet or dry gas) the effect of moisture is to produce a very considerable diminution in the rate of diffusion of the negative ions, while on the other hand it tends to increase the rate of diffusion of the positive ions, though the change produced in the positive ions is not in general as great as that produced in the negative. We shall see later on that water vapour condenses more readily on negative ions than on positive ones, so that it is probable that the negative ions in a damp atmosphere get loaded with moisture and so are retarded in their movements through the surrounding gas.

The preceding experiments relate to ions produced by the Röntgen rays. Townsend\* subsequently applied the same method to the determination of the coefficients of diffusion of ions produced by radio-active substances, by ultra-violet light and by discharges from electrified needle points; the results of these experiments are shown in the following table.

Coefficients of Diffusion of Ions produced in Air by different Methods.

	Dry Air		Moist Air	
Method	+ ions	- ions	+ ions	- ions
Röntgen rays	·028 ·032	·043 ·043 ·043	032	·035 ·041 ·037
Ultra-violet light Point Discharge	·0247 ·0216	·037 ·032	·028 ·027	·039 ·037

From these numbers we conclude that the ions produced by Röntgen rays, by radio-active substances and by ultra-violet light

<sup>\*</sup> Townsend, Phil. Trans. A. 195, p. 259, 1900.

are identical, a conclusion which we shall find confirmed by several other courses of reasoning.

Townsend\* also investigated the coefficients of diffusion of ions produced by radio-active substances at a series of pressures ranging from 772 millimetres of mercury to 200 mm. and found that within this range the coefficient of diffusion was inversely proportional to the pressure; the Kinetic Theory of Gases shows that this would be true in a system where the diffusing systems do not change character with the pressure; as this result holds for ions we conclude that down to a pressure of at least 200 mm. the ions do not change. We shall see that at very low pressures the negative ions are very much smaller than at these high pressures.

20. It is of interest to compare the rates of diffusion of ions through a gas with those of the molecules of one gas through another. In the following table taken from Winkelmann's *Handbuch der Physik*, vol. I. pp. 645, 647, the coefficients of diffusion into each other for hydrogen, air, carbonic acid, and carbonic oxide, and for some vapours are given; it appears from the table that the gases diffuse very much more quickly than the ions, but that there are vapours whose coefficients of diffusion are of the same order as those of the ions.

Gas	$D  cm.^2/sec.$	Gas	$\frac{D}{\mathrm{cm.}^2/\mathrm{sec.}}$	Gas	$D  cm.^2/sec.$
CO—CO <sub>2</sub> air—CO <sub>2</sub> O <sub>2</sub> —CO <sub>2</sub> H <sub>2</sub> —CO <sub>2</sub> air—O <sub>2</sub>	·13142 ·13433 ·13569 ·53409 ·17778	$\begin{array}{c} \text{CO-O}_2\\ \text{H}_2\text{-O}_2\\ \text{H}_2\text{-air}\\ \text{etherH}_2\\ \text{ether-air} \end{array}$	·18717 ·66550 ·63405 ·296 ·0775	$\left.\begin{array}{c}\text{ether}\text{CO}_2\\\text{isobutylic}\\\text{amide}\end{array}\right\}\text{H}_2\\\text{"}-\text{-air}\\\text{"}-\text{CO}_2$	·0552 ·1724 ·0426 ·0305

The most probable explanation of the slow diffusion of the ions seems to be that the charged ion forms a nucleus round which the molecules of the gas condense, just as dust collects round a charged body, thus producing a complex system which diffuses slowly: this explanation is supported by the fact discovered by McClelland+ that the coefficients of diffusion of the ions in the flame gases depend very much on the temperature of the flame

<sup>\*</sup> Townsend, Phil. Trans. A. 195, p. 259, 1900.

<sup>+</sup> McClelland, Camb. Phil. Soc. Proc. x. p. 241, 1899.

and the distance of the ions from it; a comparatively small lowering of temperature producing a great diminution in the rate of diffusion of the ions, as if precipitation had occurred upon them. The view is also supported by the ability of the ions to act as nuclei for the precipitation of water vapour. It must be remembered also that an ion differs from an ordinary molecule in being charged with electricity and thus being surrounded by a strong electric field.

Rutherford\* has recently shown that the vapour of alcohol or ether, like that of water, produces a great diminution in the mobility of the negative ion.

# Velocity of the Ions in an Electric Field.

directly proportional to the speed with which the ions travel through the gas under the action of an electric field of given strength. The connection between this speed and the coefficient

The coefficient of diffusion of the ions through a gas is

of diffusion can be established as follows. From the definition of the coefficient of diffusion D it follows that if n is the number of ions per cubic centimetre, the number of ions which in unit time cross unit area of a plane at right angles to x is equal to  $D\frac{dn}{dx}$ . We may thus regard the ions as moving parallel to the axis of x with the average velocity  $\frac{1}{n}D\frac{dn}{dx}$ . The ions being in the gaseous state will produce a partial pressure p which when the temperature is constant is proportional to the number of ions, we see therefore that the average velocity of the ions parallel to x is equal to  $\frac{1}{p}D\frac{dp}{dx}$ . Now dp/dx is the force acting parallel to the axis of x on unit volume of the gas, we may thus interpret the preceding expression as meaning that when the force acting parallel to the axis of x on the ions in unit volume is unity, the

ions move parallel to the axis of x with a mean velocity of translation equal to D/p. Suppose now that the ions are placed in an electric field when the electric intensity parallel to the axis of x

is equal to X, then the force on the ions in unit volume is equal

\* Rutherford, Phil. Mag. vi. 2. p. 210, 1901.

to Xen, hence if u is the average velocity of translation of the ions parallel to the axis of x

 $u = Xen \frac{D}{p}$ .

Now n/p is the same for all gases at the same temperature, hence if N is the number of molecules of air in a c.c. at this temperature and at the atmospheric pressure  $\Pi$ , since  $n/p = N/\Pi$ , we have

 $u = XeD \frac{N}{\Pi}$ ,

or  $u_0$  the velocity of the ions in a field of unit intensity is given by the equation

 $u_0 = D \frac{Ne}{\Pi}.$ 

Thus  $u_0$  is directly proportional to D, so that a knowledge of one of these quantities enables us at once to calculate the other.

22. Measurements of the velocity of the ions under an electric field were made some time before those of the coefficients of diffusion. The earliest systematic measurements of the velocity of the ions in an electric field were made in the Cavendish Laboratory in 1897 by Rutherford\*. Two different methods were used in these experiments. The first method is as follows: suppose that the current is passing through ionised gas between two parallel plates A and B; then if there are n positive ions and n negative ions in each cubic centimetre of the gas and  $u_1$ ,  $u_2$  are respectively the velocities of the positive and negative ions, the current i passing through each unit area of cross-section between the plates is given by the equation

$$i = n \left( u_1 + u_2 \right) e,$$

where e is the charge on an ion. Now i can easily be measured if one of the plates A is connected to one pair of quadrants of an electrometer, the other pair of which is connected to earth, and if the other plate B is connected to one terminal of a battery of known electromotive force, the other terminal of which is to earth. For if the quadrants are at first connected together and then disconnected, i will be the charge communicated in one second to the plate connected with the electrometer.

<sup>\*</sup> Rutherford, Phil. Mag. v. 44, p. 422, 1897.

The value of ne can be determined in the following way; after the gas has been exposed to the ionising agent, say Röntgen rays, sufficiently long for it to get into a steady state, the rays are suddenly cut off, and simultaneously with the extinction of the rays a large electromotive force is suddenly switched on between the plates; then if B is the positive plate all the positive ions between the plates are driven against the plate A before they have time to recombine with the negative ions, and thus A receives a positive charge equal to that on the whole of the positive ions between the plates, i.e. each unit area of A receives a charge of positive electricity equal to nle, where l is the distance between the plates. This charge can be measured by the electrometer, let it equal q; then since  $i = n(u_1 + u_2)e$ , we have

$$\frac{i}{q} = \frac{u_1 + u_2}{l} \dots (1),$$

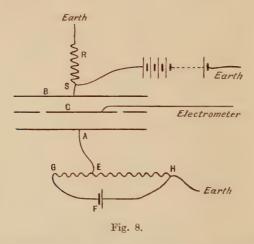
a relation which enables us to determine  $u_1 + u_2$ . Now let E be the potential difference between the plates when the current is i. Then  $u_1 + u_2$  is the sum of the velocities of the ions when the electric intensity is E/l; hence, since as we shall see the velocity of an ion is proportional to the electric intensity, the sum of the velocities of the positive and negative ions when the electric intensity is unity is  $(u_1 + u_2) l/E$ , or  $l^2i/Eq$ . For this method to give accurate results, the ionisation and the electric field must be uniform between the plates; this condition requires, as the investigation in Chapter III. shows, that the current should be so small that the conduction is in the stage represented by the first part of the curve, Fig. 4, when the curve is straight and the current is proportional to the electric intensity. Again, when the ionisation is produced by Röntgen rays or the rays from a radioactive substance, the rays should be arranged so that they pass tangentially between the plates and do not strike against them; the reason for this precaution is that when the rays strike against a metallic surface, there is an abnormally great ionisation of the gas close to the surface of the plates and the ionisation between the plates is not uniform.

The values for the sum of the velocities of the positive and negative ions under a potential gradient of one volt per centimetre obtained by Rutherford by this method are given in the following table.

Gas	Sum of velocities of + and - ions	(+oc	Sum of velocities of + and - ions
Hydrogen Oxygen Nitrogen	3.2 cm./sec.	Carbonic acid Sulphur dioxide Chlorine Hydrochloric acid	2·15 cm./sec. ·99 cm./sec. 2 cm./sec. 2·55 cm./sec.

In these experiments the gases were not specially dried.

23. The method in this form can only be used when there is a considerable volume of gas between the plates and when the ionisation is large, in other cases the deflection of the electrometer obtained when the large electromotive force is applied between the plates is so small that accurate determinations of q are not possible; thus if the distance between the plates is 3.2 cm. we see from equation (1) that the deflection of the electrometer, when the large electromotive force is applied, is only that produced in one second by the steady leak caused by a potential difference of 3.2 volts between the plates; this with a fairly sensitive electrometer and not very weak ionisation, would often not exceed 2 or 3 scale divisions, while the percentage error with such small deflections would be very large. I have used a modification of this method



which is not subject to these disadvantages. The arrangement is represented diagrammatically in Fig. 8. C is the plate con-

nected with the electrometer, it is provided with a guard ring so as to avoid difficulties connected with irregularities in the electric field: this plate is placed between two parallel plates A and B and the whole region between A and B is exposed to the ionising agent. The plates are adjusted so that the rate of leak to the plate C, when A is charged to a potential V and B connected with earth, is the same as that to C, when B is charged to the potential V and A is connected with earth.

A is connected to a point E in a high resistance GH which is traversed by the current from the voltaic cell F, H is connected with earth, and by moving the point of attachment E the plate A can be raised to any potential from zero up to the electromotive force of the battery; if G is the positive pole of the battery positive electricity will flow into the plate C (this plate is initially connected with earth). B is connected with the earth through a large resistance R, the point S is touched at regular intervals by a rotating brush which connects it for a very short time with the negative terminal of a large battery of small storage cells the other terminal of which is to earth. The contact lasts long enough for the electric field to drive all the negative ions between B and C on to the plate C, but not long enough for any appreciable quantity of fresh ions to be produced while the field is on. The plate C is thus receiving positive ions from one side and negative from the other, and by moving the point E about we can make the positive charge balance the negative so that there is no deflection of the electrometer. When this is the case we can easily prove by the same reasoning as before that  $u_1 + v_1$ , the sum of the velocities of the positive and negative ions when the potential difference between the plates A and C is equal to that between E and H, is equal to ml where l is the distance between the plates B and C, and m is the number of contacts per second made by the rotating brush with S. As in this case the experiment may be made to last while a large number of contacts occur, the method is much more sensitive than when only one contact is made.

To prevent the potential of C changing appreciably in the interval between the contacts, C is connected with one of the plates of a parallel plate condenser of large capacity. When the final test is made as to whether C has or has not received a charge

the plates of the condenser are pulled apart so as to diminish its capacity and thus increase the deflection of the electrometer due to any charge that might be on the plate C. Care must be taken to allow sufficient time to elapse between successive contacts at S to permit of the gas getting into a steady state before the next contact is made. When the ionisation is very weak it may require an interval of several seconds for this condition to be fulfilled.

24. Another method used by Rutherford\* is represented in Fig. 9. Two large metal plates A and B were placed parallel to

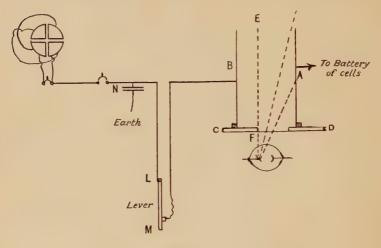


Fig. 9.

one another and 16 cms. apart on the insulating blocks C and D. The Röntgen rays were arranged so as to pass through only one half of the gas included between the plates, thus no direct radiation reached the air to the left of the line EF which is half-way between the plates. The plate A was connected with one terminal of a battery of a large number of small storage cells giving a potential difference of 220 volts, the other terminal of the battery being connected with the earth. The plate B was connected through a contact lever LM, mounted on an insulating block, to one pair of quadrants of an electrometer, the other pair being connected with the earth.

<sup>\*</sup> Rutherford, Phil. Mag. v. 44, p. 422, 1897.

A pendulum interrupter was arranged so as first to make the current in the primary of the induction coil used to produce the rays, then after a known interval to break the electrometer circuit by knocking away the lever LM, and then to break the battery circuit shortly afterwards. N is a condenser connected to the electrometer to increase its capacity. With this arrangement the ions have to travel over a distance of 8 cm. before they reach the plate B, and the object of the experiment was to find the time occupied by the rays in passing over this distance. It was found that there was only a very small deflection of the electrometer when the interval between putting on the rays and breaking the electrometer circuit was less than 36 sec., but when the interval exceeded this value the deflection of the electrometer increased rapidly. Thus 36 sec. was taken as the time required for the ions to pass over a distance of 8 cm. under a potential gradient of 220/16 volts per centimetre. This corresponds to a velocity 1.6 cm./sec. for the gradient of a volt per centimetre, and no difference was detected between the velocities of the positive and negative ions. This makes the sum of the velocities of the positive and negative ions in air under a potential gradient of a volt a centimetre equal to 3.2 cm./sec. which is exactly the velocity found by Rutherford using the first method.

25. The difference between the velocities of the positive and negative ions was discovered by Zeleny\*, who has made very valuable determinations of the velocities of the ions in an electric field. The method by which he discovered the difference of the velocities was by finding the electric force required to force an ion against a stream of gas moving with a known velocity parallel to the lines of electric force. Thus suppose A and B, Fig. 10, represent two parallel plates made of wire gauze and that between these plates we have a stratum of ionised gas, let the gas be moving through the plates from A to B with the velocity V, and let the potential gradient between the plates be n volts per centimetre, B being the positive plate. Then if the velocity of the positive ion under a potential gradient of 1 volt per centimetre be u, the velocity of the positive ion in the direction from B to A is nu - V and this is proportional to the number of ions giving up their charges

<sup>\*</sup> Zeleny, Phil. Mag. v. 46, p. 120, 1898.

or

to A in unit time. Suppose now that we make B the negative plate, then if the potential gradient between the plates is n' volts

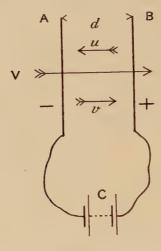


Fig. 10.

per centimetre and the velocity of the negative ion under a potential gradient of 1 volt per centimetre is v, the velocity of the negative ion from B to A is n'v - V, and this is proportional to the number of negative ions giving up their charges to A in unit time. If we adjust the potential gradients so that the rate at which A receives a positive charge when B is positive is equal to the rate at which it receives a negative charge when B is negative, we have

$$nu - V = n'v - V,$$

$$\frac{u}{v} = \frac{n'}{n}.$$

Thus from the measurement of the potential gradients we can determine the ratio u:v.

The apparatus used by Zeleny for carrying out this method is shown in Fig. 11. P and Q are brass plates 9 centimetres square. They are bored through their centres and to the openings thus made the tubes R and S are attached, the space between the plates being covered in so as to form a closed box; K is a piece of wire gauze completely filling the opening in the plate Q; T is an

insulated piece of wire gauze nearly but not quite filling the opening in the plate P and connected with one pair of quadrants of an

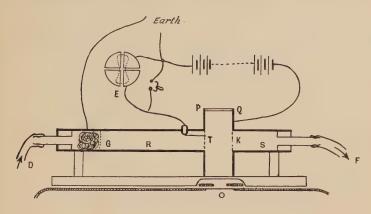


Fig. 11.

electrometer E. A plug of glass-wool G filters out the dust from a stream of gas which enters the vessel by the tube D and leaves it by F; this plug has also the effect of making the velocity of flow of the gas uniform across the section of the tube. Röntgen rays to ionise the gas were produced by a bulb at O, the bulb and coil being in a lead-covered box fitted with an aluminium window through which the rays passed. Q is connected with one pole of a battery of cells and P and the other pole of the battery connected with earth. When the rays are entering PQ and the ions are travelling in opposite directions in the box the charges they give to P, Q and K are conducted to earth, while those they give to T gradually change its potential at an approximately uniform rate, as long as this potential is small compared with that of Q. When the distribution of free charges in the gas has assumed a steady state all the changes in the potential of T are due to the charges given up by the ions striking against it.

The nature of the readings obtained with this apparatus are indicated by the curves shown in Fig. 12 where the ordinates represent the deflection of the electrometer in a given time and the abscissæ the potential difference in volts between the plates P and Q. Curve I. is for the case when the negative ions, Curve II. when the positive ions, are driven against the plate. It will be seen that after a point about B the curves are for some distance

straight lines, but that there is a curved portion to the left of B, indicating that some ions are delivered up to the gauze under smaller

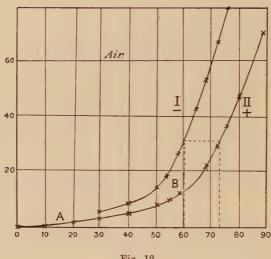


Fig. 12.

voltages than we should expect. This may possibly be explained by irregularities in the air blast, the deflections corresponding to the part of the curve about A arriving in the lulls of the blast. One way of treating the observations would be to produce the straight portion of the curves until they cut the horizontal axis; in the figure this would happen for Curve I. at about 50 volts and for Curve II. at about 60; we might then take 50 volts as the potential difference between the plates which would give to the negative ions a velocity equal to that of the blast, while 60 volts would be required to give the same velocity to the positive ions, so that under fields of equal strength the velocity of the negative ion would be to that of the positive as 6 to 5. The method actually adopted was different; the curves were regarded as merely a preliminary part of the experiment indicating about the values of the potential differences to employ in the final observations. Thus from the curves in Fig. 12 it is clear that to get the same deflection with the positive ions, as is got with the negative ions for a potential difference of 60 volts, would require a potential difference of between 72 and 74 volts; a careful series of measurements with differences of potential between these values is taken and the true

value of the potential difference found by interpolation. When this value, suppose for example 73.2, had been found, the ratio of the velocities of the negative to the positive ions was taken as 73.2:60.

The potential gradient between the plates was found to be not quite uniform owing to the accumulation of ions between the plates. The actual potential gradient was measured and a correction applied for the want of uniformity, this correction amounted to about 2 per cent. The results obtained by Zeleny are given in the following table.

RATIO OF VELOCITIES OF IONS.

Gas	Velocity of negative ion	
Air	1·24 1·24 1·23 1·14 1·15 1·00 1·045 0·985 1·105	

Thus acetylene is the only gas in which the velocity of the negative ion is less than that of the positive and here the difference is so small that it is within the limits of error of the experiment. The gases in this experiment were not specially dried; we have seen that moisture has a great effect in reducing the velocity of the negative ion.

26. In some later experiments Zeleny\* has determined the absolute values of the velocity of both the positive and negative ions. The method he employed was a blast method, though in these experiments the blast was at right angles to the lines of electric force instead of along them. A method similar to the one just described was tried for a considerable time (it is evident that if we know the velocity of the blast and the points where

<sup>\*</sup> Zeleny, Phil. Trans. A. 195, p. 193, 1900.

the straight portions of the Curves I. and II. cut the horizontal axis we can deduce the velocity of both the positive and negative ions), but it had to be abandoned owing to the disturbance in the distribution of the velocity of the blast caused by the wire gauze which in this method has to be used for the electrodes.

The theory of the method finally used is as follows. A stream of gas flows between two concentric metal cylinders which are kept at different potentials, the gas at one place is traversed by a beam of Röntgen rays at right angles to the axis of the cylinder; the ions thus produced are carried by the stream of gas parallel to the axis of the cylinder, while a velocity at right angles to this axis is imparted to them by the electric field. Let CC', Fig. 13, represent a section of the outer cylinder, DB that of the inner one,

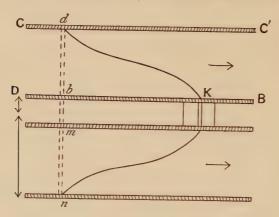


Fig. 13.

dbmn the beam of Röntgen rays ionising the gas. If CC' is at a higher potential than DB, then a positive ion starting from d will move along a curved path between the cylinders, finally reaching the inner cylinder at a point K whose horizontal distance from d is one of the quantities measured in these experiments. This distance, X, can easily be expressed in terms of the velocity of the ion under unit electric force. For let b and a be respectively the radii of the outer and inner cylinders, A the potential difference between the cylinders, then the radial electric force R at a distance r from the common axis of the cylinders is given by the equation

$$R = \frac{A}{r \log_{\epsilon}(b/a)};$$

thus if v is the velocity of the ion under unit electric force, then on the assumption that the velocity is proportional to the electric force we have, if V is the radial velocity of the ion at a distance r from the axis of the cylinders,

$$V = \frac{Av}{r\log_{e}(b/a)}.$$

If u is the velocity of the gas parallel to the axis of the cylinders which we shall take as the axis of x, then the differential equation to the path of the ion is

$$\begin{split} \frac{dx}{dr} &= \frac{u}{V} \\ &= \frac{\log_{\epsilon}\left(b/a\right)ur}{Av}; \end{split}$$

hence X the horizontal distance from d at which the ion strikes the inner cylinder is given by the equation

$$X = \frac{\log_{\epsilon}(b/a)}{Av} \int_{a}^{b} ur dr.$$

Now  $2\pi \int_a^b ur dr$  is the volume of gas which passes in unit time between the cylinders. We shall denote this quantity, which is easily measured, by Q, then we have

or

Thus if we know X we can easily determine v. The time T taken by the ion to pass from one cylinder to the other is given by the equation

$$T = \int_a^b \frac{dr}{V} = \frac{\log_e (b/a)}{A v} \int_a^b r dr$$

$$= \frac{\log_e (b/a)}{2A v} (b^2 - a^2)$$

$$= \pi \frac{(b^2 - a^2) X}{Q} \dots (2).$$

These equations apply to ions starting from the inner surface of the outer cylinder. In practice the production of ions is not

confined to the surface of the cylinder but extends throughout a layer db reaching from one cylinder to the other. The ions which start from a point in db, nearer to the surface of the inner cylinder than d, will evidently not be carried so far down the tube by the stream as an ion starting from d. Thus the preceding equations give us the position of the furthest point down the inner cylinder which is reached by the ions. In order to determine this point the inner cylinder is divided at K into two parts insulated from each other, the part D to the left being connected with the earth, while the part B to the right is connected with one pair of quadrants of an electrometer. If a constant stream of gas is sent between the cylinders, then when the potential of CC' is above a certain value, all the ions from the volume dd which move inwards will reach DB to the left of K and will not affect the electrometer. By gradually diminishing the potential of CC' we reach a value such that the ions starting from the outer edge of d reach DB just to the left of K; when this stage is reached the electrometer begins to be deflected. If then in equation (1) we put for A the difference of potential corresponding to this stage, and for X the horizontal distance of K from d, we shall be able to deduce the value of v.

Corrections. In consequence of the diffusion of the ions, all the ions starting from d will not follow exactly the line dK, and some of the ions will be found to the right of the line. The consequence of this is that the electrometer will begin to be deflected even when the potential difference A is theoretically sufficient to bring all the ions to the left of K; thus the observed potential difference when the deflections begin is slightly too large, and therefore the values of v determined by equation (1) are a little too small. Similar effects to those due to diffusion will be produced by the mutual repulsion of the ions. It is evident that the magnitude of these effects will depend upon the time it takes the ion to travel between the cylinders; if this time were zero, neither diffusion nor repulsion would have time to produce any effect, thus the longer the time taken by the ions to travel between the cylinders, the smaller would be the value of v as determined by this method. The time T, as we see from equation (2), depends upon the velocity of the air blast and the strength of the field; by altering these quantities it is possible to determine the values of v for a considerable range of values of T; the values so found decrease as was to be expected slightly as T increases, the relation between v and T being found by experiment to be a linear one. Curves in which the ordinates were the ionic velocities and the abscissæ the time T were drawn, and the curve (which was found to be a straight line) prolonged until it cut the line T=0; the corresponding value of v was taken as the ionic velocity. An example of such curves is given in Fig. 14, the o's and v's are the points determined by

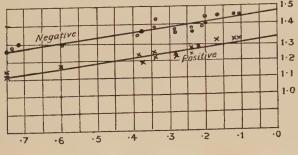


Fig. 14.

actual experiments. The points at which the lines intersect the line T=0 give 1.48 cm./sec. for the velocity of the negative ion and 1.34 for the velocity of the positive, when the potential gradient is one volt per cm.

Smaller corrections have to be applied for the disturbance in the electric field produced by the presence of an excess of ions of one sign over those of the other in different parts of the field. It was proved by direct experiment that the effects due to surface ionisation were not appreciable.

The apparatus used to carry out this method is represented in section in Fig. 15. AA' was the outer cylinder; it had an internal diameter of 5·1 cm. and a total length of 142 cm. The parts to the right of V' and to the left of V were made of brass tubing; the part between VV' was aluminium tubing of the same diameter; this piece was inserted so as to permit the Röntgen rays to pass through. The tubes were fastened together by airtight joints and placed on insulating supports.

The inner cylinder BB' was an aluminium tube; in one set of experiments it was 1 cm. in diameter, in another it was 2.8 cm.;

the ends of this tube were closed by conical pieces. The tube was divided at C and the two portions separated by 5 mm. and

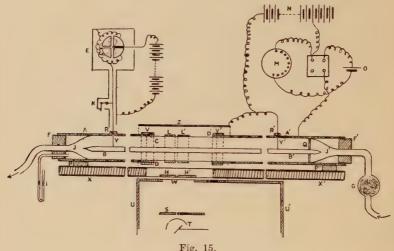


Fig. 15.

insulated by ebonite plugs. The tube was supported by the ebonite rod Q and by the stiff brass wires Y and Y' which passed through ebonite plugs in the outer cylinder, and served to connect B' with the earth, and B with one pair of quadrants of the electrometer. The electrometer was a very sensitive one giving a deflection of 500 scale divisions for a potential difference of one volt. The narrow vertical beam of rays was adjusted and kept definite by the slits in the lead plates S, HH' and LL'. A constant and measurable supply of gas was sent through the tube by a gasometer. Experiments were made with gases carefully dried and with gases saturated with water vapour. Two series of experiments were made, one with an inner tube 1 cm. in diameter. the other with an inner tube 2.8 cm. in diameter; the results obtained in the one series agreed very well with those obtained in the other.

The values of the ionic velocities obtained by this method are given in the following table; they have been reduced to the uniform pressure of 760 mm, of mercury on the assumption (see p. 30) that the ionic velocity under a given potential gradient is inversely proportional to the pressure.

#### IONIC VELOCITIES.

Gas .	under a poter of one vo	cm. per sec. ntial gradient lt per cm.	Ratio of velocities of negative and positive ions	Tempera- ture degrees centigrade
Air dry	1·29 ·76 ·82 6·70	1·87 1·51 1·80 1·52 ·81 ·75 7·95 5·60	1·375 1·10 1·32 1·18 1·07 ·915 1·19 1·05	13·5 14 17 16 17·5 17 20 20

The intensity of ionisation was altered by causing the Röntgen rays to pass through aluminium plates of different thicknesses, the ionic velocities were found to be independent of the intensity of the rays.

The results obtained by Zeleny agree well with those obtained for the sum of the velocities obtained by Rutherford (see page 34) for air, oxygen, and hydrogen, allowing for the uncertainty as to the amount of moisture in the gases used by Rutherford; for carbonic acid however there is considerable discrepancy, as 2.15 cm./sec., the value of the sum of the velocities obtained by Rutherford, is nearly 40 per cent. greater than the value 1.57 obtained by Zeleny, and as Zeleny found that this sum was the same whether the gases were dry or moist the discrepancy cannot be explained as due to the excess or defect of moisture in Rutherford's gases.

Method of determining the velocity by measuring the number of ions sent by a radial electric field to the sides of a tube of given length when traversed by a current of gas.

27. The principle of this method which has been used by Rutherford\* to measure the velocities of the ions produced by uranium radiation is as follows. Suppose that ionised air is blown through a tube along the axis of which there is a wire charged positively,

<sup>\*</sup> Rutherford, Phil. Mag. v. 47, p. 109, 1899.

the electric field around the wire will drag the negative ions into the wire and thus rob the gas of a certain proportion of these ions; the number of these ions thus abstracted from the gas will depend upon the relation between the velocity of an ion in the electric field and the velocity of the air blast; if the ionic velocity were infinitely greater than the velocity of the blast, all the ions would be abstracted, while if the velocity of the blast were infinitely greater than the ionic velocity, they would all escape.

We see from equation (2), page 43, that t, the time taken by an ion to reach the wire, is given by the expression

$$t = \frac{r^2 - a^2}{2A u_2} \log_{\epsilon} \frac{b}{a}....(1),$$

where r is the distance from the axis of the tube of the point from which the ion starts, b the internal radius of the tube, a the external radius of the wire, A the difference of potential between the wire and the tube (the wire being at the higher potential), and  $u_2$  the velocity of the negative ion under unit electric force. If in equation (1) we put t equal to the time taken by the air blast to pass from one end of the tube to the other, we see that all the ions whose distance from the axis of the tube is less than the value of r given by equation (1) will be dragged into the wire; hence if  $\rho$  is the ratio of the number of ions dragged from the gas to the whole number of ions, we have, assuming that the ions are uniformly distributed over the cross-section of the tube,

$$\rho = \frac{r^2 - a^2}{b^2 - a^2} = \frac{2Au_2t}{(b^2 - a^2)\log_{\epsilon}(b/a)},$$

$$u_2 = \frac{\rho(b^2 - a^2)\log_{\epsilon}(b/a)}{2At}....(2).$$

or

The arrangement used by Rutherford is represented in Fig. 16.

A paper tube coated with uranium oxide was fitted into a metal tube T 4 cm. in diameter. A blast of air from a gasometer after passing through a plug of cotton-wool C to remove the dust passed through a long metal tube AB connected with the earth; into this tube cylindrical electrodes A and B were fastened by insulating supports so as to be coaxial with the tube. The electrode A was charged up by a battery, and the electrode B was connected with one pair of quadrants of an electrometer. If B

were charged initially to a potential of the same sign as A (suppose positive) large enough to saturate the gas, then the rate

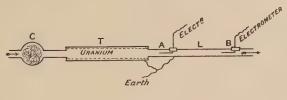


Fig. 16.

of leak of the electrometer when the air blast was passing would measure the number of negative ions which escaped being dragged into the electrode A; by comparing the rate of leak when the electrode A is not charged with the rate when it is charged to a known potential, we can determine the value of  $\rho$  in equation (2). Rutherford did not use this arrangement to measure directly the velocity of the ions produced by the uranium radiation, but proved by means of it that the velocities of these ions were the same as those of the ions produced by Röntgen rays. For this purpose, after measurements of  $\rho$  had been made with the uranium cylinder in place, this cylinder was removed and replaced by an aluminium one exposed to Röntgen rays, the strength of these rays being adjusted so that the amounts of ionisation in the two cases were approximately equal; measurements of  $\rho$  were then made with the Röntgen rays on and were found to be identical with those obtained when the ionisation was produced by uranium radiation, thus proving that the ionic velocities are the same in the two cases.

28. A method which is the same in principle as this was first used by McClelland to measure the velocities of the ions produced by flames\*, and by arcs and incandescent wires+: the results of these experiments showed that the velocity of the ions diminishes very greatly when they get into the cooler parts of the flame, suggesting that there is a rapid condensation round the ions of some of the products of combustion of the flame. The

<sup>\*</sup> McClelland, Phil. Mag. v. 46, p. 29, 1898.

<sup>+</sup> McClelland, Proc. Camb. Phil. Soc. x. p. 241, 1899.

diminution of velocity is clearly shown in the following table given by McClelland.

Distance of point where velocity was measured from the flame	Temperature at this point	Velocity of ion under a force of one volt per centimetre
5·5 cm.	230° C.	•23 cm./sec.
10 cm.	160° C.	•21 cm./sec.
14·5 cm.	105° C.	•04 cm./sec.

These velocities are all of them small compared with the velocities of the ions produced by Röntgen rays or by radio-active substances. In the case of the ions from flames as in other cases the negative ions move faster than the positive. McClelland applied the same method to the determination of the velocities of the ions produced by arcs or incandescent wires; he found in these cases the same variability in the velocity as he had previously observed in the ions from flames; in the case of the arcs and wires, however, he found that the hotter the flame or wire the smaller the velocity of the ion. We shall return to the consideration of these phenomena when we discuss the electrical properties of flames and arcs.

Determination of the ionic velocities by means of an alternating electric field.

29. This method, which however can only be applied when we have the ionisation confined to a thin layer of gas, and when moreover all the ions are of one sign, is a very convenient and accurate one. It was used by Rutherford\* to determine the velocity of the negative ions which are produced close to a metallic plate when that plate is illuminated by ultra-violet light. The principle of the method is as follows. AB (Fig. 17) is a horizontal plate made of well polished zinc, it is carefully insulated, and can be moved vertically up and down by means of a screw; it is connected with one pair of quadrants of an electrometer, whose other quadrants are connected with the earth. CD is a base plate with a hole EF cut in it; this hole is covered in with

<sup>\*</sup> Rutherford, Proc. Camb. Phil. Soc. ix. p. 401, 1898.

fine wire gauze, ultra-violet light is sent through this gauze and falls on the plate AB. CD is connected with an alternating

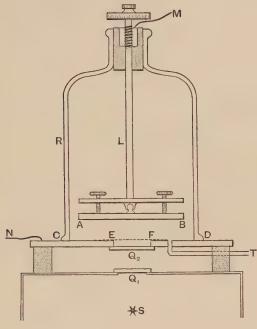


Fig. 17.

current dynamo or any other means of producing an alternating difference of potential proportional to a simple harmonic function of the time; the other pole of this instrument is put to earth. Suppose now that at any instant the potential of CD is higher than that of AB, the negative ions at  $\overline{AB}$  will be attracted towards CD, and will continue to move towards it as long as the potential of CD is higher than that of AB. If however the potential difference between CD and AB changes sign before the negative ions reach CD these ions will be driven back to AB, so that this plate will not lose any negative charge. AB will thus not begin to lose negative electricity until the distance between the plates AB and CD is less than the distance passed over by the negative ion during the time the potential of CD is greater than that of AB. The method consists in altering the distance between the plates until AB just begins to lose a negative charge, then if we know this distance and the frequency and maximum

value of the potential difference we can deduce the ionic velocity of the negative ion. For let the potential difference between CD and AB at the time t be equal to  $a \sin pt$ , then if d is equal to the distance between these plates, the electric force is equal to  $(a/d) \sin pt$ , and if u is the velocity of the ion under unit electric force, the velocity of the negative ion in this field will be

$$u(a/d)\sin pt$$
;

hence if x is the distance of the ion from the plate AB at the time t we have

$$\frac{dx}{dt} = \frac{ua}{d}\sin pt,$$

$$x = \frac{ua}{dp}(1 - \cos pt),$$

or

if x = 0 when t = 0.

Thus the greatest distance the ion can get from the plate AB is equal to 2ua/pd. If the distance between the plates is gradually reduced, the plate AB will begin to lose a negative charge when

$$d = \frac{2ua}{pd}$$
, or  $u = \frac{pd^2}{2a}$ .

Hence if we measure p, a and d we can determine u.

In this way Rutherford found for the velocities under a potential gradient of 1 volt per cm. of the negative ion produced by the incidence of ultra-violet light on a zinc plate, the following values, for dry gases.

Gas	Ionic velocity
Air	1.4 cm./sec.
Hydrogen	3.9 cm./sec.
Carbonic acid	.78 cm./sec.

These values differ but little from those obtained for Röntgen rays.

Rutherford found that the velocity of the ions was independent of the metal of which the plate AB was made: and he proved by this method that the velocity of the ions under a constant

potential gradient varies inversely as the pressure, at any rate down to pressures of 34 mm. of mercury which was the lowest pressure at which he worked.

Chattock's method of measuring the velocities of ions produced by the discharge of electricity from a sharp point.

30. The preceding methods would be very inconvenient in the case when the electric field is as strong and the velocities of the ions therefore as great as they are when electricity is discharging from a pointed conductor. For this case, in which the ions at some little distance from the point are all of one sign, Chattock\* has devised a very ingenious method by means of which he has been able to measure the velocities of these ions. The principle of the method is as follows. Let P represent a vertical needle discharging electricity from its point into the surrounding air; consider the force acting on the ions included between two horizontal planes A and B, Fig. 18. If Z is the vertical com-

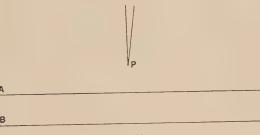


Fig. 18.

ponent of the electric intensity,  $\rho$  the density of the electrification; the resultant force F on the ions included between A and B is vertical and equal to

 $\iiint Z\rho\,dx\,dy\,dz.$ 

If the velocity of the ion under unit electric force is u, then w the vertical velocity of the ion is equal to uZ. If all the ions

<sup>\*</sup> Chattock, Phil. Mag. v. 48, p. 401, 1899; Chattock, Walker and Dixon, Phil. Mag. vi. 1, p. 79, 1901.

are of one sign so that u is the same for all the ions, we have, since Z = w/u,

$$F = \frac{1}{u} \iiint w \rho \, dx \, dy \, dz.$$

Since the ions are all of one sign  $\iint \rho w dx dy$  is the quantity of electricity streaming across a horizontal plane in unit time; this is the same for all horizontal planes, and is equal to i where i is the current of electricity flowing from the needle point, hence we have

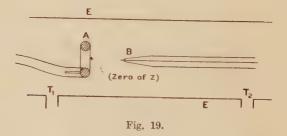
$$F = \frac{i}{u} \int dz = \frac{i}{u} (z_B - z_A),$$

where  $z_B - z_A$  is the vertical distance between the planes A and B. This force F must be balanced by the difference of the gaseous pressures over A and B, hence if  $p_B$  and  $p_A$  denote respectively the total pressures over the planes A and B we have

and hence

Thus, by the measurement of these pressures and of the current flowing from the point (the latter measurement is easily made by inserting a galvanometer in series with the needle point), we can deduce the value of u.

The apparatus used by Chattock to carry out this method is represented in Fig. 19. The discharging needle is supported in a



narrow sliding glass tube drawn out at the end B; it discharges to a ring A made of smooth metal; the needle and ring are enclosed in a wide glass tube E, the ends of which are connected by tubes  $T_1$  and  $T_2$  with the ends of a U tube pressure gauge containing

water; the ring A can be moved along the tube by means of a screw. In this apparatus, since there is no current to the left of the ring or to the right of the point, if we put  $z_B - z_A$  equal to the distance of the point from the ring, and if  $\omega$  is the difference of pressure in dynes per sq. cm. measured by the pressure gauge, A the area of cross-section of the tube, then

$$p_B - p_A = \omega A + p',$$

where p' is the part of the pressure which is borne by the ring. We have, by equation (1),

$$\omega = \frac{i}{Au}(z_B - z_A) + \frac{p'}{A}.$$

It was assumed that when the point was a considerable distance from the ring p' became independent of z; on this supposition we have, if  $\Delta \omega$ ,  $\Delta z$  are corresponding changes in  $\omega$  and z,

$$\frac{\Delta\omega}{\Delta z} = \frac{i}{Au},$$

and it was from this relation that u was calculated. Chattock found for the velocities of the negative and positive ions in air under a potential gradient of a volt per cm. the values 1.8 cm./sec. and 1.38 cm./sec., which agree well with those found for the ions produced by Röntgen rays, and we conclude that the ions in the two cases are the same. In the second paper Chattock extends the method to hydrogen, oxygen, and carbonic acid as well as air, and again finds close agreement between the velocities of the ions produced by the point discharge and those produced by radioactive substances. He points out that while the determination of the ionic velocities of the positive ions showed in all gases great consistency, considerable variations which could not be attributed to errors of experiment were found in the values of the velocities of the negative ions. This was especially the case in hydrogen, where the values of the ionic velocity of the negative ion varied from 6.8 to 8.5; in the other gases the variation is not so marked. Chattock ascribes this variation to the gases occluded by the discharging point; when this point is negative some of these occluded gases are given off and help to carry the discharge, and as the velocity of the hydrogen ions is very large compared with that of other ions, it is urged that a small admixture of other and more slowly moving ions might produce a considerable lowering of the average velocity. When the point is positive the occluded gas is supposed either not to be given off, or, if given off, not to take any part in carrying the discharge. This explanation is consistent with other phenomena connected with the discharge of electricity from metals; we shall see that in the electric discharge through gas at low pressures occluded gas is given off from the cathode, and that the amount of gas so given off has very considerable influence upon the phenomena. The values obtained by Chattock for the velocities of the ions produced by the point discharge are given in the following table, in which  $V_+$  denotes the velocity of the positive ion,  $V_-$  that of the negative, and  $\overline{V}$  the mean of these velocities. The gases were dry.

Gas	<i>V</i> <sub>+</sub>	v	P	V_/V_+
Hydrogen	5°4	7:43	6·41	1:38
	0°83	0:925	0·88	1:11
	1°32	1:80	1·55	1:36
	1°30	1:85	1·57	1:42

### Charges on the ions.

31. We saw on page 32 that the coefficient of diffusion D of an ion through a gas was connected with the velocity u of the same ion through the same gas under unit electric force by the equation

$$\frac{u}{D} = \frac{Ne}{\Pi}$$
,

where N is the number of molecules in a c.c. of gas at a pressure of  $\Pi$  dynes per square cm. It is to be remembered that this relation is obtained on the supposition that a number of ions in a given volume produce the same pressure as the same number of molecules of a perfect gas at the same temperature; in other words, that the ions behave like a perfect gas with respect to pressure. As we have seen that the ions in a gas at atmospheric pressure are probably aggregations of considerable complexity as compared with the molecules of a perfect gas, we must regard this assumption as only an approximation to the truth, and one which would cease to be even that when the ions are as large as those which occur in the colder parts of flames or near an incandescent wire.

or

Taking the values of D given by Townsend and (1) the values of u given by Rutherford, (2) those given by Zeleny, we get the following values for  $Ne \times 10^{-10}$ , e being expressed in electrostatic units.

From Rutherford's experiments on the mean velocities of the ions in gases, and the mean of the coefficients of diffusion given by Townsend we get

- Gas	$Ne  imes 10^{-10}$
Air	1·35
Oxygen	1·25
Carbonic acid	1·30
Hydrogen	1·00

From Zeleny's values for the velocities of the ions and Townsend's for the coefficients of diffusion we get

II.

	Mois	t Gas	Dry Gas	
AirOxygenCarbonic acidHydrogen	Positive ions  1.28 1.34 1.01 1.24	1:29 1:27 87 1:18	Positive ions  1.46 1.63 .99 1.63	1:31 1:36 :93 1:25

Since one electromagnetic unit or  $3 \times 10^{10}$  electrostatic units of electricity when passing through acidulated water liberates 1·23 c.c. of hydrogen at the temperature of 15° C. and pressure of 760 mm. of mercury, and since in 1·23 c.c. of gas there are 2·46 N atoms of hydrogen, we have, if E is the charge in electrostatic units on the atom of hydrogen in the electrolysis of solutions,

$$2.46 NE = 3 \times 10^{10}$$
,

 $\overline{NE} = 1.22 \times 10^{10}.$ 

The mean of all the values of Ne in Tables I. and II. is  $1.24 \times 10^{10}$ .

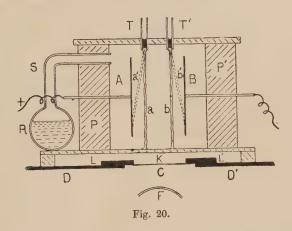
We conclude then (1) that the charges carried by the gaseous ions are the same whether the ions are produced in air, oxygen, hydrogen or carbonic acid, (2) that this charge is equal to the charge carried by the hydrogen atom in the electrolysis of solutions.

The proof of the equality of the charges on the ions in different gases was first obtained by the author by direct measurements of the charges carried by the gaseous ions. Though the variations in the value of Ne given in Tables I. and II. are greater than we should have expected from the accuracy with which the experiments were made, they are not sufficiently regular to enable us to draw any conclusions; thus for example in Table I. Ne for carbonic acid is considerably greater than for hydrogen, while in Table II. it is very much less. We must remember too that these results have been obtained on the supposition that the complex vapours the values obtained on this supposition would be somewhat too large.

Currents in the gas caused by the motion of ions through it.

32. Since the charged ions when in an electric field settle down to a state of steady motion in which they have no acceleration the force exerted by the field on the ions is transferred to the gas. Thus when in any region there is an excess of the ions with charges of one sign over those having the opposite sign there will be a resultant force acting on the gas in this region which may start currents in the gas. Thus to take the case of a current passing through ionised gas between parallel metal plates, there is, as we shall see in the next paragraph, an excess of positive ions in the layer of gas near the negative plate and of negative ions in the layer next the positive plate; thus these layers will be acted on by forces tending to make them move towards their respective plates. If these plates were infinite these forces would be balanced by an excess of pressure next the plate, but if the plates are finite this excess of pressure will relieve itself by the gas moving round to the back of the plate and a system of air currents will be set up.

These currents have been observed by Zeleny\* by means of the apparatus represented in Fig. 20. A and B are the two parallel metal plates, connected to the opposite poles of a battery of storage cells. The plates are enclosed in a box of which the



sides P and P' are made of blocks of paraffin, while the other two sides are glass to enable the observer to see what is going on inside. The bottom of the box is made of wood, Röntgen rays pass through this and ionise the gas between the plates. vessel R contains liquid ammonia, from which ammonia gas passes through the tube S into the box. The tubes T and T' contain drops of hydrochloric acid. The particles of ammonium chloride formed at the lower ends of the tube, where the acid is in contact with the ammonia, fall slowly, producing well-defined vertical whitish streams a and b near the plates A and B. These streams are vertical so long as the Röntgen rays and the electric field are not on together. If, however, when the electric field is on, the gas is exposed to the rays, the streams are deflected towards the plates as indicated by the dotted lines in the figure. In order to show that this was not due to any charge on the solid particles of ammonium chloride the experiment was repeated with streams of carbonic acid gas, the difference of refractive index between this gas and air being sufficient to render the streams visible; it was found that these streams, like those of the ammonium chloride, were deflected towards the plate.

<sup>\*</sup> Zeleny, Proc. Camb. Phil. Soc. x. p. 14, 1898.

33. For convenience of reference we give a table containing the results of the measurements of the ionic velocities made up to 1902. The velocities are expressed in cms. per second and are for a potential gradient of 1 volt per cm.  $V_+$ ,  $V_-$ , denote respectively the velocities of the positive and of the negative ions, V the mean of these velocities.

# VELOCITIES OF IONS.

# Ions from Röntgen Rays.

Gas	$V_{+}$	V	V	Observer
Air dry Air moist Oxygen Oxygen dry Oxygen moist. Carbonic acid dry Carbonic acid moist Hydrogen Hydrogen dry Hydrogen moist Nitrogen Sulphur dioxide Hydrochloric acid Chlorine	1.36 1.37  1.36 1.29   6.70 5.30 	1.87 1.51  1.80 1.52  .81 .75  7.95 5.60	1.6 1.61 1.44 1.4 1.58 1.405 1.07 .78 .78 5 7.2 5.45 1.6 .5 1.27 1.0	Rutherford Zeleny Zeleny Rutherford Zeleny Zeleny Rutherford Zeleny Zeleny Zeleny Rutherford Zeleny Rutherford Zeleny Rutherford Rutherford Rutherford Rutherford

### Ions from Ultra-Violet Light.

Air Hydrogen Carbonic acid	•••	1·4 3·9 ·78	•••	Rutherford Rutherford Rutherford
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#### Ions from Flames.

Velocities varying from '04 to '23 ...... McClelland

## Ions from point discharge.

Hydrogen	0.83 1.32	7·43 0·925 1·80 1·85	6·41 0·88 1·55 1·57	Chattock Chattock Chattock Chattock
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Potential gradient between two parallel plates immersed in an ionised gas and maintained at different potentials.

34. It was shown first by Zeleny\*, and then independently by Child+, that when electricity is passing between two plates immersed in ionised gas, the potential gradient between the plates is not uniform, but is greatest in the neighbourhood of the electrodes. The difference of potential between one of the plates and any point in the gas may be measured by having a water or mercury dropper at the point; the most convenient way, however, is to place at the point a fine wire, which will ultimately assume the potential of the point. When the wire is used it is necessary however to take several precautions: in the first place, if the number of ions in the gas is small, the wire will only take up the potential very slowly, and it is important that the instrument used for measuring the capacity of the wire should have very small capacity. This circumstance often makes it desirable to measure the potential of the wire by means of a small gold leaf electroscope instead of a quadrant electrometer, which though more sensitive to differences of potential has yet a very much greater capacity. Another point to be remembered is that if a wire is placed in a region where the ions are all of one sign, its potential can only change one way. Thus if it is a region where there are only positive ions, its potential can increase but cannot decrease, and thus if the potential of the wire gets by some accident too high, it cannot sink to its true value.

A characteristic curve for the distribution of potential between the plates, due to Zeleny, is given in Fig. 21. It will be seen that the gradient near the centre of the field is uniform, but that near the plates the gradients get much steeper and that they are steeper at the negative than at the positive plate.

From the equation  $\frac{d^2V}{dx^2} = -4\pi\rho$ , where V is the potential at a distance x from the plate and  $\rho$  the density of the electrification,

<sup>\*</sup> Zeleny, Phil. Mag. v. 46, p. 120, 1898.

<sup>+</sup> Child, Wied. Ann. lxv. p. 152, 1898.

we can, if we know the distribution of potential, calculate the density of the electrification at any point between the plates.

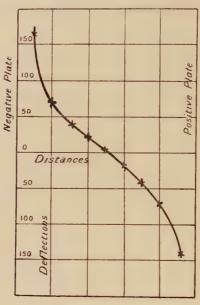


Fig. 21.

The density corresponding to the potential curve in Fig. 21 is shown in Fig. 22.

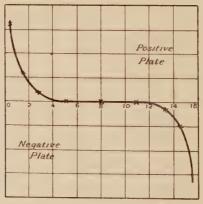


Fig. 22.

We see that next the positive plate there is an excess of

negative electricity and an excess of positive near the negative plate. With the small potential differences used in this experiment the regions where there is an excess of one kind of electricity over the other are in the immediate neighbourhood of the plates, the density of the free electricity being exceeding small in the central portion of the field. If a larger potential difference had been applied to the plates, the regions of free electricity would have expanded, and with very large potential differences these regions would fill the whole of the space between the plates. In the example given, the greatest density of the electrification is about  $2 \times 10^{-4}$  electrostatic units; as the charge on an ion is about  $3.5 \times 10^{-10}$  such units the number of positive ions in a cubic centimetre would exceed that of negative by about 6 × 105. Taking the number of molecules in a cubic centimetre of the gas as  $3.5 \times 10^{19}$ , the ratio of the excess of ions of one sign to the number of molecules is only  $1.6 \times 10^{-14}$ . As most of the negative ions would be driven away from the negative plate, this will approximately represent the ratio of the number of free ions to the number of molecules, and from it we learn what a very small amount of ionisation is sufficient to account for many of the phenomena of the conduction of electricity through gases.

#### CHAPTER III.

# MATHEMATICAL THEORY OF THE CONDUCTION OF ELECTRICITY THROUGH A GAS CONTAINING IONS.

35. We shall now proceed to develop the theory of electric conduction through an ionised gas on the basis that the velocities of the ions are proportional to the electric force acting upon them. We shall take the case of two infinite parallel metal plates maintained at different potentials and immersed in an ionised gas; the lines of electric force are everywhere at right angles to the plates; they are thus always parallel to a line which we shall take as the axis of x.

Let  $n_1$ ,  $n_2$  be respectively the number of positive and negative ions per unit volume at a place fixed by the coordinate x, let q be the number of positive or negative ions produced in unit time per unit volume at this point by the ionising agent; let X be the electric intensity at this point,  $R_1$ ,  $R_2$  the velocities of the positive and negative ions under unit electric intensity, so that the velocities of these ions at this point are respectively  $R_1X$ ,  $R_2X$ ; let e be the charge on an ion. The volume density of the electrification, supposed due entirely to the presence of the ions, is  $(n_1 - n_2)e$ ; hence we have

$$\frac{dX}{dx} = 4\pi (n_1 - n_2) e$$
 .....(1).

If i is the current through unit area of the gas, and if we neglect any motion of the ions except that caused by the electric field, we have

$$n_1 e R_1 X + n_2 e R_2 X = i_2 (2)$$

From equations (1) and (2) we get

$$n_1 e = \frac{1}{R_1 + R_2} \left\{ \frac{i}{X} + \frac{R_2}{4\pi} \frac{dX}{dx} \right\} \dots (3),$$

$$n_2 e = \frac{1}{R_1 + R_2} \left\{ \frac{i}{X} - \frac{R_1}{4\pi} \frac{dX}{dx} \right\} \dots (4).$$

If we measure the distribution of electric force between the plates, we can from these equations, if we know  $R_1$  and  $R_2$ , determine  $n_1$  and  $n_2$ , or if in addition to the distribution of electric force, we measure, by the methods previously given,  $n_1$ ,  $n_2$  at various points in the field, we can use these equations to determine  $R_1$  and  $R_2$ , the velocities of the ions.

When the gas is in a steady state, the number of negative and of positive ions in each unit of volume must remain constant with respect to the time, thus the loss of these ions must be balanced by the gains. Now ions are lost in consequence of the recombination of the positive and negative ions: these ions will come into collision with each other, and a certain fraction of the whole number of collisions will result in the positive and negative ions combining to form a single system which is electrically neutral and which no longer acts as an ion; the number of collisions in unit volume in unit time is proportional to  $n_1 n_2$ . We shall suppose that the number of positive or negative ions which recombine in unit volume in unit time is  $\alpha n_1 n_2$ : this is the rate at which unit volume is losing positive and negative ions in consequence of recombination; in consequence of ionisation it is gaining them at the rate q, and in consequence of the motion of the ions it is losing positive ions at the rate  $\frac{d}{dx}(n_1R_1X)$  and negative ones at the rate

 $-\frac{d}{dx}(n_2R_2X)$ : hence when the gas is in a steady state we have

$$\frac{d}{dx}(n_1R_1X) = q - \alpha n_1 n_2 \dots (5),$$

$$-\frac{d}{dx}(n_2R_2X) = q - \alpha n_1n_2 \dots (6).$$

If  $R_1$  and  $R_2$  are constant at all parts of the field, we have from (1), (5) and (6)

$$\frac{d^2X^2}{dx^2} = 8\pi e \left( q - \alpha n_1 n_2 \right) \left( \frac{1}{R_1} + \frac{1}{R_2} \right) \dots (7).$$

From this equation, if we measure the distribution of  $X^2$  between the plates, we can determine whether ionisation or recombination is in excess at any point, for from (7)  $q - \alpha n_1 n_2$  and  $d^2 X^2 / dx^2$  have the same sign, hence when ionisation is in excess of recombination, i.e. when  $q - \alpha n_1 n_2$  is positive,  $d^2 X^2 / dx^2$  is positive and the curve whose ordinate is  $X^2$  is convex to the axis of x; when recombination is in excess of ionisation the curve for  $X^2$  is concave to the axis of x.

Substituting in equation (7) the values of  $n_1$ ,  $n_2$  given by equations (3) and (4) we get

$$\begin{split} \frac{d^2X^2}{dx^2} &= 8\pi e \left(\frac{1}{R_1} + \frac{1}{R_2}\right) \left\{ q - \frac{\alpha}{e^2X^2 \left(R_1 + R_2\right)^2} \right. \\ & \times \left(i + \frac{R_2}{8\pi} \frac{dX^2}{dx}\right) \left(i - \frac{R_1}{8\pi} \frac{dX^2}{dx}\right) \right\} .....(8). \end{split}$$

I have not been able to get a general solution of this differential equation except when q is constant and  $R_1 = R_2$ ; in that case put-

ting  $X^2 = y$  and  $\frac{dy}{dx} = p$  we get, writing R for either  $R_1$  or  $R_2$ ,

$$p\frac{dp}{dy} = \frac{16\pi e}{R} \left\{ q - \frac{\alpha}{4e^2 R^2 y} \left( i^2 - \frac{R^2 p^2}{64\pi^2} \right) \right\} \dots (9).$$

Integrating this we get

$$\frac{R^{2}p^{2}}{64\pi^{2}} - i^{2} = \frac{qeR}{2\pi \left(1 - \frac{\alpha}{8\pi eR}\right)} y + Cy^{\frac{\alpha}{8\pi eR}} \dots (10),$$

where C is a constant of integration. From this equation we can find the ratio of  $X_0$ , the electric intensity midway between the plates, to  $X_1$ , the electric intensity close to a plate. For when  $R_1 = R_2$  the distribution of electric force is symmetrical and midway between the plates dX/dx and p = 0; let us further assume that we are dealing with a case like that in Fig. 22, where there is no free electricity for some distance from the middle of the plate, so that here  $d^2X/dx^2$  also vanishes; hence from (9) and (10) we have

Now at the positive plate  $n_1 = 0$  and at the negative plate  $n_2 = 0$ ; hence at either plate  $n_1 n_2 = 0$ , but

$$n_{1}n_{2} = \frac{1}{4R^{2}e^{2}X^{2}}\left(i^{2} - \frac{R^{2}p^{2}}{64\pi^{2}}\right);$$

hence if  $X_1$  is the value of X at either plate, we have

$$\frac{-X_1^2 \frac{qeR}{2\pi}}{1 - \frac{\alpha}{8\pi eR}} = CX_1^{\frac{\alpha}{4\pi eR}} \dots (12).$$

Hence by (11) and (12)

$$\frac{8\pi Re}{\alpha} = \left(\frac{X_{\scriptscriptstyle 0}}{X_{\scriptscriptstyle 1}}\right)^{\frac{\alpha}{4\pi eR}-2} \ , \label{eq:Repair}$$

or writing  $\beta$  for  $8\pi Re/\alpha$  we get

$$\frac{X_0^2}{X_1^2} = \beta^{\frac{\beta}{1-\beta}}.$$

We see from this equation that  $X_0/X_1$  is never greater than

unity since  $\beta^{\frac{\beta}{1-\beta}}$  diminishes from unity to zero as  $\beta$  increases from  $\beta=0$  to  $\beta=$  infinity. Since  $\beta$  does not involve either q or i, the ratio of the electric intensities does not depend upon either the intensity of the ionisation or of the current between the plates. For air at atmospheric pressure R=480 (since unit electrostatic force is 300 volts per centimetre),  $\alpha$  is about  $1.2 \times 10^{-6}$ , (see page 19), and  $e=3.5 \times 10^{-10}$ ; substituting these values we find  $\beta=3.9$  for air at atmospheric pressure. Since R is inversely proportional to the pressure,  $\beta$  is inversely proportional to the pressure, and thus is very large at the pressure of a few millimetres of mercury. Putting  $\beta=4$  we find

$$\frac{X_1}{X_0} = 4^{\frac{2}{3}} = 2.51$$
 approximately.

At low pressures  $\beta$  is large, in this case  $X_1/X_0 = \beta^{\frac{1}{2}}$  approximately, and thus the ratio of  $X_1$  to  $X_0$  varies inversely as the square root of the pressure.

The experiments we have described on the distribution of electric force between the plates show that when the current is small, the regions where X differs appreciably from  $X_0$  are confined to two layers near the plates, the distribution of X between the plates being represented by a curve like that shown in Fig. 23.

We can very easily find an inferior limit to  $\lambda$  the thickness of one of these layers. For let P be a point on the boundary of the

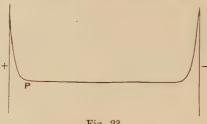


Fig. 23.

layer next the electrode, then since X becomes constant at P, there are as many positive as negative ions in this region and if the velocities of the ions are the same, half the current must be carried by the positive and half by the negative ions. Thus if i is the current through unit area, and e the charge on an ion, i/2epositive ions must cross unit area of a plane through P in unit time; and all these positive ions must be produced in the region between P and the positive plate. But if  $\lambda$  is the thickness of the layer, the number of positive ions produced in unit time corresponding to each unit area of the plate is  $q\lambda$ , the number that cross unit area at P cannot therefore be greater than  $q\lambda$ , and can only be as great when there is no recombination of the ions between P and the positive plate, hence

$$q\lambda > \frac{i}{2e}$$
,

or  $\lambda > i/2eq$ ; thus i/2eq is an inferior limit to  $\lambda$ . If I is the maximum current, l the distance between the plates, I = qle; hence i/2I is an inferior limit to  $\lambda/l$ .

Though we cannot find a general solution of the equations (1), (2), (5), (6) when  $R_1$  is not equal to  $R_2$ , we see at once that a particular solution of these equations is given by the relations

$$\begin{split} n_1 &= n_2 = (q/\alpha)^{\frac{1}{2}}, \\ R_1 n_1 X e &= \frac{R_1}{R_1 + R_2} i, \\ R_2 n_2 X e &= \frac{R_2}{R_1 + R_2} i, \\ X &= \left(\frac{\alpha}{q}\right)^{\frac{1}{2}} \frac{i}{e\left(R_1 + R_2\right)}. \end{split}$$

This solution corresponds to a constant value of the electric force between the plates, and indicates that the proportion of the current carried by the positive and negative ions respectively is the same as the ratio of the velocities of these ions. This solution though it may apply to the central portion of the field, cannot however hold right up to the plates. For suppose P is a point between the plates at which this solution applies. Then across unit area at P,  $iR_1/(R_1 + R_2)e$  positive ions pass in unit time, and these must come from the region between P and the positive plate; if the distance of P from this plate is  $\lambda$  this region cannot furnish more than  $q\lambda$  positive ions in unit time, and can only do this when there is no recombination; hence the preceding solution cannot hold at a distance from the positive plate less than

$$\frac{R_{\scriptscriptstyle 1}}{R_{\scriptscriptstyle 1}+R_{\scriptscriptstyle 2}}\frac{i}{qe}\,.$$

Similarly it cannot hold at a distance from the negative plate less than

 $rac{R_2}{R_1+R_2}rac{i}{qe}$  .

We shall assume that the preceding solution does hold at distances from the plates greater than the preceding values: and further that in the layers in which the solution does not hold there is no recombination of the ions.

Let us consider the state of things at the positive plate between x = 0 and  $x = \lambda_1$ , where

 $\lambda_{\rm l} = \frac{R_{\rm l}}{R_{\rm l} + R_{\rm l}} \, \frac{i}{qe} \, . \label{eq:lambda_lambda_lambda}$ 

Then, since in this region there is no recombination, equations (1), (5), (6) become

$$\begin{split} \frac{dX}{dx} &= 4\pi \left( n_1 - n_2 \right), \\ \frac{d}{dx} \left( R_1 n_1 X \right) &= q, \\ \frac{d}{dx} \left( R_2 n_2 X \right) &= -q. \end{split}$$

If q is constant we have

$$R_1 n_1 X = qx,$$
  

$$R_2 n_2 X = \frac{i}{e} - qx,$$

where the constant of integration has been chosen so as to make  $n_1 = 0$  when x = 0: substituting these values for  $n_1$ ,  $n_2$  in the equation giving dX/dx we get

$$\begin{split} X\,\frac{dX}{dx} &= 4\pi e\,\left\{qx\left(\frac{1}{R_1} + \frac{1}{R_2}\right) - \frac{i}{eR_2}\right\}\,,\\ X^2 &= 8\pi e\,\left\{\frac{1}{2}\,qx^2\left(\frac{1}{R_1} + \frac{1}{R_2}\right) - \frac{ix}{eR_2}\right\} + C.....(13), \end{split}$$

or

where C is a constant which may be determined from the condition that when  $x = \lambda_1$ 

$$X^2 = \frac{\alpha}{q} \frac{i^2}{e^2(R_1 + R_2)^2};$$

from this we find

$$C = \frac{\alpha}{q} \, \frac{i^2}{e^2 \, (R_1 + R_2)^2} \left\{ 1 \, + \frac{4 \pi e}{\alpha} \, \frac{R_1}{R_2} \, (R_1 + R_2) \right\} \, .$$

C is the value of  $X^2$  when x = 0, *i.e.* at the positive plate; if we call this value  $X_1$ , and if  $X_0$  is the constant value of X between the layers, we have

$$X_{1} = X_{0} \left\{ 1 + \frac{4\pi e}{\alpha} \frac{R_{1}}{R_{2}} (R_{1} + R_{2}) \right\}^{\frac{1}{3}};$$

thus  $X_1$  is always greater than  $X_0$  and the ratio  $X_1/X_0$  does not depend upon the amount of ionisation or the strength of the current between the plates.

If  $X_2$  is the value of X at the negative plate, we can prove in a similar way that

$$X_{\rm B} = X_{\rm B} \left\{ 1 + \frac{4\pi e}{\alpha} \frac{R_{\rm B}}{R_{\rm B}} (R_{\rm B} + R_{\rm B}) \right\}^{\frac{1}{3}}.$$

Thus if  $R_2$ , the velocity of the negative ion, is very large compared with  $R_1$ , the velocity of the positive ion, the value of X at the negative plate is large compared with its value at the positive, and the thickness of the layer in which X is variable, is greater at the negative than it is at the positive plate. A curve representing the distribution of electric intensity between the plates in this case is represented in Fig. 24.

If we put

$$\beta_1 = \frac{4\pi e}{\alpha} \frac{R_1}{R_2} (R_1 + R_2) : \beta_2 = \frac{4\pi e}{\alpha} \frac{R_2}{R_1} (R_1 + R_2),$$

we have

$$X_1 = X_0 (1 + \beta_1)^{\frac{1}{2}} : X_2 = X_0 (1 + \beta_2)^{\frac{1}{2}};$$

when  $\beta_1$  and  $\beta_2$  are large we have approximately

$$X_1 = X_0 \beta_1^{\frac{1}{2}} : X_2 = X_0 \beta_2^{\frac{1}{2}}.$$

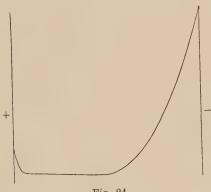


Fig. 24.

In the special case when the velocities of the positive and negative ions are equal  $\beta_1 = \beta_2$  and  $X_1/X_0 = (8\pi e R/\alpha)^{\frac{1}{2}}$ , this agrees when  $\beta$  is large with the result found by the independent investigation of this case given on p. 67.

The fall of potential  $V_1$  across the layer next the positive plate whose thickness is  $\lambda_i$  is equal to

$$\int_0^{\lambda_1} X dx;$$

substituting the value of X given by equation (13) and integrating we find

$$\begin{split} V_1 &= \frac{1}{2} \, X_1 \lambda_1 + \frac{1}{2} \frac{X_0 \lambda_1}{\sqrt{\beta_1}} \log \left( \sqrt{\beta_1} + \sqrt{1 + \beta_1} \right) \\ &= \frac{1}{2} \, X_0 \lambda_1 \left\{ (1 + \beta_1)^{\frac{1}{2}} + \frac{1}{\sqrt{\beta_1}} \log \left( \sqrt{\beta_1} + \sqrt{1 + \beta_1} \right) \right\}. \\ &\text{Since } X_0 &= \left\{ \frac{\alpha}{q} \right\}^{\frac{1}{2}} \frac{i}{e \, (R_1 + R_2)}, \text{ and } \lambda_1 &= \frac{R_1}{R_1 + R_2} \frac{i}{qe}, \\ V_1 &= \frac{1}{2} \, \frac{\alpha^{\frac{1}{2}}}{q^{\frac{3}{2}}} \, \frac{i^2 R_1}{e^2 \, (R_1 + R_2)^2} \left\{ (1 + \beta_1)^{\frac{1}{2}} + \frac{1}{\sqrt{\beta_1}} \log \left( \sqrt{\beta_1} + \sqrt{1 + \beta_1} \right) \right\} \dots (14). \end{split}$$

Thus the fall of potential across this layer is proportional to the square of the current.

If  $V_2$  is the change in potential in crossing the layer next the negative electrode we find similarly

$$V_2 = \frac{1}{2} \frac{\alpha^{\frac{1}{2}}}{q^{\frac{2}{3}}} \frac{i^2 R_2}{e^2 (R_1 + R_2)^2} \left\{ (1 + \beta_2)^{\frac{1}{3}} + \frac{1}{\sqrt{\beta_2}} \log{(\sqrt{\beta_2} + \sqrt{1 + \beta_2})} \right\}.$$

If  $\beta_1$  and  $\beta_2$  are very large we have approximately

$$V_{\scriptscriptstyle 1} = \frac{1}{2} \, \frac{\alpha^{\frac{1}{2}}}{q^{\frac{3}{2}}} \, \frac{i^{\scriptscriptstyle 2}}{e^{\scriptscriptstyle 2}} \frac{R_{\scriptscriptstyle 1}}{(R_{\scriptscriptstyle 1} + R_{\scriptscriptstyle 2})^{\scriptscriptstyle 2}} \, \beta_{\scriptscriptstyle 1}{}^{\frac{1}{2}},$$

$$V_2 = \frac{1}{2} \, \frac{\alpha^{\frac{1}{2}}}{q^{\frac{3}{2}}} \, \frac{i^2}{e^2} \frac{R_2}{(R_1 + R_2)^2} \, \beta_2^{\frac{1}{2}}.$$

Substituting the values of  $\beta_1$ ,  $\beta_2$  we find

$$\frac{V_{1}}{V_{2}} = \frac{R_{1}^{2}}{R_{2}^{2}},$$

or the falls of potential at the positive and negative plates are proportional to the squares of the velocities of the positive and negative ions.

Let us consider how the fall of potential varies with the pressure of the gas: if p is the pressure,  $R_1$  and  $R_2$  are inversely proportional to p, and q is directly proportional to p, hence we see that for a given current  $V_1$  and  $V_2$  vary inversely as p.

37. The relation between the potential difference between the plates and the current.

The fall of potential between the plates is made up of the fall of potential at the layers which we have already calculated and the fall of potential in the space between the layers where the electric intensity is uniform and equal to  $X_0$ ; the breadth of this space is  $l - (\lambda_1 + \lambda_2)$  where l is the distance between the plates, and since  $\lambda_1 + \lambda_2$  is equal to i/qe the fall of potential in this space is equal to

$$X_{_0}\left(l-rac{i}{qe}
ight),$$
 or to  $\left(rac{lpha}{q}
ight)^{rac{1}{2}}rac{i}{e\left(R_1+R_2
ight)}\!\left(l-rac{i}{qe}
ight);$ 

adding to this the values for the fall of potentials across the layers we get, if V is the potential difference between the plates,

$$V = \frac{1}{2} \frac{\alpha^{\frac{1}{2}}}{q^{\frac{3}{2}}} \frac{i^{2}}{e^{2}(R_{1} + R_{2})^{2}} \left\{ R_{1} (1 + \beta_{1})^{\frac{1}{2}} + \frac{R_{1}}{\sqrt{\beta_{1}}} \log (\sqrt{\beta_{1}} + \sqrt{1 + \beta_{1}}) + R_{2} (1 + \beta_{2})^{\frac{1}{2}} + \frac{R_{2}}{\sqrt{\beta_{2}}} \log (\sqrt{\beta_{2}} + \sqrt{1 + \beta_{2}}) \right\} + \frac{\alpha^{\frac{1}{2}}}{q^{\frac{1}{2}}} \frac{i}{e(R_{1} + R_{2})} \left( l - \frac{i}{qe} \right) \dots (15).$$

This equation is of the form

$$V = Ai^2 + Bi,$$

thus the curve whose ordinate is i and abscissa V is a parabola. This equation ceases to be an approximation to the truth when the two layers touch, i.e. when  $\lambda_1 + \lambda_2 = l$  or i = qel; in this case the current is the greatest that can be carried by the ionised gas. The minimum value of the potential difference required to produce this current is got by putting i = qel in equation (15); we see that the potential difference required to produce saturation is proportional to the square of the distance between the plates and to the square root of the intensity of ionisation.

38. The study of the distribution of electric intensity between the plates when the maximum current is passing leads to an easy way of finding the ratio of the velocities of the positive and negative ions, for as in this case there is no recombination, equations (5) and (6), p. 65, give

$$R_1 n_1 X = qx.....(16),$$
  
 $R_2 n_2 X = q (l - x) .....(17),$ 

where x is measured from the positive plate. At the point between the plates where the force is a minimum

$$\frac{dX}{dx} = 0 = 4\pi \left(n_1 - n_2\right)e,$$

hence at this point  $n_1 = n_2$ , so that if x is the distance of the point P where X is a minimum from the positive plate we have by equations (16) and (17)

$$\frac{R_1}{R_2} = \frac{x}{l-x};$$

thus the ratio of the velocities of the positive and negative ions is equal to the ratio of the distances of P from the positive and negative plates, so that if we have determined P by measuring

the distribution of potential between the plates we can at once deduce the ratio of the velocities.

39. Case when the ionisation is confined to a thin layer.

In the preceding investigation we have supposed that the ionisation is uniformly distributed between the plates, there are however many very important cases when the region in which the ionisation takes place is a thin layer of gas, the rest of the space between the plates being free from the action of the ionising agent. We proceed now to the consideration of this case, beginning with the one where the ionised layer is close to one of the plates A. Let us suppose that A is the positive plate, then all the ions in the space between the plates must have been dragged by the action of the electric field from the layer, hence these ions must be all positive, so that the current is carried entirely by positive ions. Let there be  $n_1$  of these ions per cubic centimetre and let X be the electric force, i the current, then using the same notation as before our equations are now

$$\frac{dX}{dx} = 4\pi n_1 e,$$

$$R_1 n_1 X e = i;$$

from these equations we get

$$\frac{XdX}{dx} = \frac{4\pi i}{R_1},$$

$$X^2 = \frac{8\pi ix}{R_1} + C....(18),$$

or

where C is the constant of integration; it is evidently the value of  $X^2$  close to the positive plate.

If V is the potential difference between the plates, and l their distance apart, we have

$$V = \int_0^l X dx = \frac{R_1}{12\pi i} \left[ \left( \frac{8\pi i l}{R_1} + C \right)^{\frac{3}{2}} - C^{\frac{3}{2}} \right] \dots (19).$$

To find an expression for C we must turn our attention to the layer of ionised gas; let us suppose that the current is small compared with that required to saturate this layer, then the number of free positive or negative ions in unit volume of the layer  $=(q/\alpha)^{\frac{1}{2}}$ , if q as before measures the intensity of ionisation; if

there is no great change in the electric force as we pass from the gas into the layer the sum of the velocities of the positive and negative ions will be of the order  $(R_1 + R_2)$   $C^{\frac{1}{2}}$ , and as i the current equals the number of ions multiplied by the sum of the velocities of the ions,  $e(R_1 + R_2)$   $C^{\frac{1}{2}}(q/\alpha)^{\frac{1}{2}}$  will be of the same order as i; hence C is comparable with

$$\frac{i^2\alpha}{qe^2\left(R_1+R_2\right)^2}.$$

Hence C will be small compared with  $8\pi il/R_1$  if

$$8\frac{i\alpha R_1}{8\pi q e^2 \left(R_1+R_2\right)^2 l}$$

is a small quantity.

If  $\delta$  is the thickness of the ionised layer, I the saturation current,

 $I = qe\delta$ ;

thus the preceding quantity will be small if

 $rac{1}{2}rac{i}{l}rac{\delta}{l}rac{R_{2}}{(R_{1}+R_{2})}rac{1}{eta_{2}} ext{ is small,}$ 

where

$$\beta_{2} = \frac{4\pi e}{\alpha} \frac{R_{2}}{R_{1}} (R_{1} + R_{2}).$$

If  $\delta/l$ , i/I are small, then since  $\beta_2$  is greater and  $R_2/(R_1 + R_2)$  less than unity, we see that the quantity under consideration will be small. When this is the case we can, in equation (19), neglect

C in comparison with  $\frac{8\pi il}{R_1}$ , and the equation becomes

$$V^2 = \frac{32\pi}{9R_1} il^3 \dots (20).$$

We see that in this case the current is proportional to the square of the potential difference, and thus increases more rapidly with the electromotive force than if it obeyed Ohm's law. We shall see examples of this when we consider the passage of electricity through metals immersed in hot gases. In this case by far the greater part of the ionisation occurs in the layer next the metal and, as Pringsheim\* has shown, the current increases more rapidly than the potential difference. The current is proportional to  $R_1$  the velocity of the ion which carries it; thus since the

<sup>\*</sup> Pringsheim, Wied. Ann. 55, p. 507, 1895.

velocity of the negative ion is greater than that of the positive, the current for the same difference of potential between the plates is greater when the ionisation takes place next the negative plate than when next the positive, in other words the current is greater in one direction than in the opposite; this unipolar conductivity as it is called is very marked indeed in conduction through hot gases and flames containing salts. Rutherford\* has observed it when the ionisation was due to Röntgen or radium radiation. We see from (20) that for a given potential difference the current is independent of q, the intensity of ionisation; the maximum currents between the plates will of course depend upon the intensity of the ionisation, but as long as the currents are only a small fraction of the maximum corresponding to the smallest ionisation, the currents will be independent of the amount of ionisation next the plate; we see too that the current does not depend on the charge carried by the ion.

The current for a given difference of potential varies inversely as the cube of the distance between the plates; as the current varies as the square of the potential difference, if we keep the average electric intensity between the plates constant as the distance diminishes the current will vary inversely as the distance between the plates.

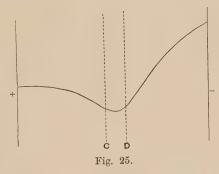
When the ionisation is confined to a layer next the plate A, we can stop the flow of ions and therefore of electricity to the plate B by interposing between the plates a third plate, and the passage of electricity will be stopped just as effectually by a plate of metal as by a non-conductor; thus we get the somewhat paradoxical effect of completely stopping a current between two plates by interposing between them an excellent conductor of electricity. An example of this effect will be considered when we discuss the passage of electricity through very hot gases.

If the layer of ionised gas is situated between the plates at a distance  $l_1$  from the positive and  $l_2$  from the negative plate, then if V is the potential difference between the plates, we can easily prove by the same method as we have used when the layer was next the plate that

$$V = \frac{2}{3} \sqrt{8\pi i} \left\{ \frac{l_1^{\frac{3}{2}}}{R_2^{\frac{1}{2}}} + \frac{l_2^{\frac{3}{2}}}{R_1^{\frac{1}{2}}} \right\},$$

<sup>\*</sup> Rutherford, Phil. Mag. vi. 2, p. 210, 1901.

where  $R_1$  and  $R_2$  are respectively the velocities of the positive and negative ions. We see that if  $R_1$  is not equal to  $R_2$  the current for the same potential difference will not, unless  $l_1 = l_2$ , be the same in one direction as in the opposite. If the velocity of the negative ion is greater than that of the positive, the current will be greatest when its direction is such that the negative plate is nearer to the ionised layer than the positive. From this we conclude that want of symmetry in the distribution of ionisation will give rise to unipolar conductivity. The distribution of electric intensity when the ionised layer is between the plates is represented in Fig. 25.



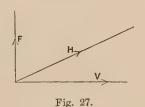
The preceding results are only true when the electric intensity close to the ionised layer is small compared with its value some distance away, a result which we have shown will be the case when the current is not approaching saturation, provided there is not a great increase in the value of the electric intensity as we pass from the inside of the layer to a point just outside. There are cases, of which the best known is that of ultra-violet light falling on a metal plate, where this condition is not fulfilled. If the illuminated plate is made the negative one, a current of electricity will pass from it to a neighbouring plate, but in this case the electric field between the plates will be approximately uniform and the preceding results do not apply. We may explain this as follows: we shall see that a metal plate exposed to ultra-violet light emits negative ions, and these ions like cathode rays ionise the gas through which they pass. Consider an insulated piece of metal in air, it cannot go on indefinitely losing negative electricity, for observation proves that its potential does not go on increasing indefinitely; it must reach a stage in which it receives as much negative electricity from the air as it loses by the action of the light. We can see how this can be brought about: suppose A is the surface of the metal, next this we have a layer of ionised gas; the metal loses negative electricity and gets a positive charge, while the negative electricity accumulates and forms a layer at some little distance from the plate. The layers of positive and negative electricity produce

an electric field which tends to drive the negative ions in the ionised gas between them into the metal, the stronger this field the more negative ions go to the metal; the electrification in the layers will accumulate until the strength of the field is such that as many negative ions are driven by it from the gas into the metal as the metal loses by the action of the light. In passing however from the inside to the outside of the layer of ionised gas we have to pass across a layer of electricity, this will produce a discontinuity in the electric intensity equal to  $4\pi\sigma$ , where  $\sigma$  is the surface density of the electrification; there may thus be a great difference between the electric intensity inside the layer and that just outside, so that the reasoning which we used to prove  $X_0$  in equation (19) small compared with  $8\pi i l/R$  need not apply in this case.

#### CHAPTER IV.

# EFFECT PRODUCED BY A MAGNETIC FIELD ON THE MOTION OF THE IONS.

40. When a charged ion is moving in a magnetic field it experiences a mechanical force whose direction is at right angles to the direction of motion of the ion, at right angles also to the magnetic force and equal in magnitude to  $HeV\sin\theta$ , where H is the magnetic force, V the velocity of the ion, e its charge, and  $\theta$  the angle between H and V; H and e are to be expressed in the electromagnetic system of units. The relation between the direction of this force F, V and H, for a positively charged ion, is shown in Fig. 27.



Now suppose that we have an ion moving through a gas, the viscosity of the gas causing the velocity of the ion to be proportional to the force acting upon it. Then if X, Y, Z, are the components of the electric intensity,  $\alpha$ ,  $\beta$ ,  $\gamma$  those of the magnetic force, u, v, w those of the velocity, the mechanical force exerted on the ion by the magnetic field has for components

$$e(\beta w - \gamma v), \quad e(\gamma u - \alpha w), \quad e(\alpha v - \beta u),$$

while the components of the mechanical force due to the electric

field are Xe, Ye, Ze. Thus as the velocity of the ion is proportional to the mechanical force acting upon it we have

$$\begin{aligned} u &= R \left( X + \beta w - \gamma v \right) \\ v &= R \left( Y + \gamma u - \alpha w \right) \\ w &= R \left( Z + \alpha v - \beta u \right) \end{aligned} ....(1),$$

R is evidently the velocity of the ion under unit electric intensity when there is no magnetic field. Solving equations (1) we find

$$u = \frac{RX + R^{2} (\gamma Y - \beta Z) + R^{3} \alpha (\alpha X + \beta Y + \gamma Z)}{1 + R^{2} (\alpha^{2} + \beta^{2} + \gamma^{2})}$$

$$v = \frac{RY + R^{2} (\alpha Z - \gamma X) + R^{3} \beta (\alpha X + \beta Y + \gamma Z)}{1 + R^{2} (\alpha^{2} + \beta^{2} + \gamma^{2})}$$

$$w = \frac{RZ + R^{2} (\beta X - \alpha Y) + R^{3} \gamma (\alpha X + \beta Y + \gamma Z)}{1 + R^{2} (\alpha^{2} + \beta^{2} + \gamma^{2})}$$
.....(2).

The first term in the numerator of these expressions represents a velocity parallel and proportional to the electric force; the second term a velocity at right angles both to the electric and magnetic forces and proportional to  $R^2HF\sin\phi$ ; where H, F, and  $\phi$  represent respectively the magnetic and electric forces and the angle between them; the third term represents a velocity parallel to the magnetic force and proportional to  $R^3H^2F\cos\phi$ . relative importance of these terms depends upon the value of RH, if this quantity is small the first term is the most important and the ion moves parallel to the electric force, if on the other hand RH is large the last term is the most important and the ion moves parallel to the magnetic force. Since R is the velocity of the ion under unit electric force, and the unit force on the electromagnetic system is  $10^{-8}$  of a volt per cm., the value of R for an ion moving through air at atmospheric pressure would be  $1.5 \times 10^{-8}$ . since the velocity of the ion under a volt per cm. is about 1.5 cm./sec. Thus at atmospheric pressure it would not be feasible to get a magnetic field strong enough to make RH large. As R varies inversely as the pressure of a gas through a considerable range of pressures it might at very low pressures be possible to make RH large and thus make the ions travel along the lines of magnetic force.

Let us take the case of an ion placed in a field in which both the electric and magnetic forces are uniform; let the electric force be parallel to the axis of x and let the magnetic force be in the plane of xz, then Y=0, Z=0,  $\beta=0$ , and equations (2) become

$$\begin{split} u &= \frac{RX\left(1 + R^2\alpha^2\right)}{1 + R^2\left(\alpha^2 + \gamma^2\right)} = RX \text{ approximately, if } R^2\left(\alpha^2 + \gamma^2\right) \text{is small,} \\ v &= -\frac{R^2\gamma X}{1 + R^2\left(\alpha^2 + \gamma^2\right)} = -R^2\gamma X, \\ w &= \frac{R^3\alpha\gamma X}{1 + R^2\left(\alpha^2 + \gamma^2\right)} = R^3\alpha\gamma X. \end{split}$$

Thus the effect of the magnetic force is to give the ion a velocity  $-R\gamma u$  at right angles to both the electric and magnetic forces and a velocity  $R^2\gamma (\alpha^2 + \gamma^2)^{\frac{1}{2}}u$  in the plane of xz at right angles to the magnetic force.

If both positive and negative ions are present and if  $R_1$  is the value of R for the positive and  $R_2$  that for the negative ion, and if  $u_1, v_1, w_1; u_2, v_2, w_2$  are respectively the velocities of the positive and negative ions, then if there are n positive and negative ions per unit volume the current parallel to y will be equal to  $ne(v_1-v_2)$  or, substituting the values of  $v_1$  and  $v_2$ , to

$$ne(R_2^2 - R_1^2)\gamma X = (R_2 - R_1)\gamma I,$$

if I is the main current parallel to x; thus if the velocities of the positive and negative currents are unequal the magnetic field will give rise to a side current proportional to the main one and the direction of the current will be deflected through an angle whose tangent is  $(R_2 - R_1) \gamma$ . If we retain terms proportional to  $(RH)^2$ , where H is the magnetic force, we see that there will be an additional current proportional to  $(R_1^2 + R_2^2 - R_1 R_2) \gamma (\alpha^2 + \gamma^2)^{\frac{1}{2}} I$  in the plane of xz at right angles to the magnetic force.

When the electric field is not uniform but, like that due to a charged particle, radiates from a point we can prove without difficulty that an ion in a uniform magnetic field will describe a spiral traced on a cone of revolution, the axis of the cone being parallel to the magnetic force.

## Motion of a free ion in a magnetic field.

41. If the ion instead of having to move through the molecules of a gas is moving in a vacuum, the path it describes in a uniform magnetic field is readily found. We shall first of all take the case when no electric forces act upon the ion, then, since the only force

acting on the ion is that due to the magnetic field and this force is always at right angles to the path of the ion, the velocity of the ion will be constant; again since the force is at right angles to the magnetic force, there will be no acceleration parallel to this force, thus when the magnetic field is uniform the component of the velocity parallel to the magnetic force is constant. As the resultant velocity is constant this implies that the direction of motion of the ion makes a constant angle with the magnetic force. If  $\rho$  is the radius of curvature of the path of the ion, m its mass, v its velocity, the force along the normal is equal to  $\frac{mv^2}{\rho}$ , but this force is equal to  $Hev\sin\theta$ , where H is the magnetic force and  $\theta$  the angle between v and H, e the charge on the ion, thus

$$\frac{mv^2}{\rho} = Hev \sin \theta,$$

$$\rho = \frac{mv'}{eH \sin \theta}.$$

or

Thus as v and  $\theta$  are constant the radius of curvature of the path is constant, the path of the particle is therefore a helix wound on a circular cylinder whose axis is parallel to the lines of magnetic force, the radius of the cylinder is  $\rho \sin^2 \theta$  or  $mv \sin \theta / eH^*$ . If the particle is projected at right angles to the lines of magnetic force, the helix shrinks into a circle whose radius is mv/eH: as the path in this case is a closed one the ion never travels more than a finite distance from its point of projection. If the velocity of the ion has a component parallel to the magnetic force, this component remains constant and the ion goes on describing equal spaces parallel to the magnetic force in equal times, while in a direction at right angles to the magnetic force the velocity of the ion is sometimes in one direction and sometimes in the opposite, so that the ion. however long it moves, never travels more than a finite distance from the line of force. We may thus express the general features of the effect by saying that in the magnetic field the ions tend to follow the lines of magnetic force.

42. The preceding investigation relates to the case when the magnetic field is constant and the lines of magnetic force do not change their direction; it is of interest to see whether the ions will

<sup>\*</sup> G. G. Stokes, Proc. Roy. Soc. Mar. 30, 1876; Phil. Mag. v. 2, p. 359, 1876.

continue to follow the lines of magnetic force when these change their direction from point to point. We shall take the special case when the lines of magnetic force are circles round the axis of z, the field being that due to a current i flowing along this axis; in this case if  $\alpha$ ,  $\beta$ ,  $\gamma$  are the components of magnetic force at a point whose coordinates are x, y, z,

$$\alpha = \frac{2iy}{x^2 + y^2}, \quad \beta = -\frac{2ix}{x^2 + y^2}, \quad \gamma = 0,$$

and if m is the mass of the ion, e its electric charge, we have

$$\begin{split} m \, \frac{d^2 x}{dt^2} &= - \, e \, \frac{2 i x}{x^2 + y^2} \, \frac{dz}{dt} \,, \\ m \, \frac{d^2 y}{dt^2} &= - \, e \, \frac{2 i y}{x^2 + y^2} \, \frac{dz}{dt} \,, \\ m \, \frac{d^2 z}{dt^2} &= \frac{2 e i}{x^2 + y^2} \Big( x \, \frac{dx}{dt} + y \, \frac{dy}{dt} \Big) = e i \, \frac{d}{dt} \log (x^2 + y^2). \end{split}$$

From these equations we have

$$\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2 + \left(\frac{dz}{dt}\right)^2 = \text{a constant} = V^2,$$

where V is the velocity of projection of the ion;

$$y\frac{d^2x}{dt^2} - x\frac{d^2y}{dt^2} = 0.$$

Thus if  $\rho$  and  $\theta$  are the polar coordinates in the plane xy, of the ion,

 $\rho^2 \frac{d\theta}{dt} = h,$ 

where h is a constant;

$$\frac{dz}{dt} = \frac{2ei}{m}\log\rho + C,$$

where C is a constant: thus the orbit of the ion in the plane of xy is that of a particle of mass m acted on by a central attractive

force equal to  $\left(\frac{4e^2i^2}{m}\log\rho + 2ei\ C\right)\Big|\rho$ .

Since

$$\left(\frac{d\rho}{dt}\right)^2 + \rho^2 \left(\frac{d\theta}{dt}\right)^2 + \left(\frac{dz}{dt}\right)^2 = V^2,$$

we have

$$\left(\frac{d\rho}{dt}\right)^{\!\!2} = V^{\!\scriptscriptstyle 2} - \frac{h^{\!\scriptscriptstyle 2}}{\rho^{\!\scriptscriptstyle 2}} \!- \left(\frac{2ei}{m}\log\rho + C\right)^{\!\!2}.$$

6 - 2

Since  $\binom{d\rho}{dt}^2$  is essentially positive,  $\rho$  will always lie between the greatest and least roots of the equation

$$rac{2ei}{m}\log R = \left\{V^2 - rac{h^2}{R^2}
ight\}^{rac{1}{2}} - C,$$

so that the ion will always remain at a finite distance from the axis of z.

43. Let us consider some special cases. Let the ion be projected parallel to the lines of magnetic force from the point  $\rho = a$ : then since dz/dt = 0 when  $\rho = a$ , we have

$$\frac{dz}{dt} = \frac{2ei}{m} \log \frac{\rho}{a},$$

and

$$h = Va$$
,

hence

$$\left(rac{d
ho}{dt}
ight)^{2}=V^{2}\left(1-rac{a^{2}}{
ho^{2}}
ight)-\left(rac{2ei}{m}\lograc{
ho}{a}
ight)^{2};$$

from this equation we see that  $\rho$  can never be less than a, and thus the velocity parallel to the axis of z never changes sign: again  $\rho$  never exceeds the value R, given by the equation

$$\frac{2ei}{m}\log\frac{R}{a} = V\left(1 - \frac{a^2}{R^2}\right)^{\frac{1}{2}}....(1).$$

R=a satisfies this equation but there is another root greater than a; it is this root which is the maximum value of  $\rho$ .

Thus in the plane at right angles to the axis of z the ion circulates in an orbit included between the circles  $\rho = a$  and  $\rho = R$ ; and thus again the ion moves in the general direction of the lines of magnetic force, although in this case there is a drift of the ions parallel to the axis of symmetry of the magnetic field. If V is small compared with 2ei/m, the solution of the equation (1) is

$$R = a (1 + \xi),$$
  
 $\xi = \frac{V^2}{2e^2i^2/m^2}.$ 

where

In this case the maximum velocity parallel to z is V.(V|eim) and is thus small compared with V. Thus the smaller the velocity of projection and the stronger the field the more nearly does the path of the ion coincide with a line of magnetic force.

44. In the next case the ion is projected from  $\rho = a$  in a direction parallel to z, in this case h = 0 and the path of the ion is in the plane through the axis of z and the point of projection; if V is the velocity of projection, then

$$\frac{dz}{dt} = \frac{2ei}{m}\log\frac{\rho}{a} + V;$$

now dz/dt can never be greater numerically than V, hence if V and 2ei/m are of the same sign  $\rho$  can never be greater than a.

The values between which  $\rho$  oscillates are a and  $ae^{\frac{ei/m}{ei/m}}$ ; the orbit is a closed one and its dimensions are very small if V is small compared with ei/m. If V and ei/m are of opposite signs then we can show that  $\rho$  is never less than a and varies between a and  $ae^{\frac{V}{ei/m}}$ .

**45**. A third case we shall consider is when the particle is projected with velocity V parallel to  $\rho$  from  $\rho = a$ , in this case again h = 0, but

 $\frac{dz}{dt} = \frac{2ei}{m} \log \frac{\rho}{\alpha}.$ 

Since dz/dt can never be greater numerically than V we see that  $\rho$  must lie between the limits  $\rho = a\epsilon^{\frac{mV}{2ei}}$  and  $\rho = a\epsilon^{-\frac{mV}{2ei}}$ ; the orbit is in the plane through the axis of z and the point of projection. If the magnetic field is very strong and therefore mV/2ei small,  $\rho$  is always very nearly equal to a, let it equal  $a(1+\xi)$ , our equations are then approximately

$$\begin{split} \frac{d^2\xi}{dt^2} &= -\left(\frac{2ei}{m}\right)^2\frac{\xi}{a^2}\,,\\ \frac{dz}{dt} &= \frac{2ei}{m}\,\xi\,, \end{split}$$

the solution of which is

$$\xi = A \sin\left(\frac{2i}{a} \frac{e}{m} t\right),$$
$$z = aA \cos\frac{2i}{a} \frac{e}{m} t.$$

Since  $V = a \frac{d\xi}{dt}$  when t = 0,  $aA = V \frac{m}{e} \frac{a}{2i} = \frac{Vm}{He}$  when H is the magnetic force at the point of projection. Thus, as we might

have expected, the path in this case is a circle whose radius aA is equal to (V/H)(m/e).

We see from the consideration of the variable field as well as from that of the constant one that the ion will tend to follow the lines of magnetic force, except in the very special case when the circumstances of projection are such that the ion during its motion always cuts the lines of magnetic force at right angles.

Motion of an ion under the joint action of electric and magnetic forces.

46. We shall now investigate the motion of an ion when it is acted on simultaneously by both electric and magnetic forces; we shall take the case when both these forces are constant. Let the axis of z be parallel to the direction of the magnetic force, and the plane of xz parallel to the direction of the electric force. Let H be the magnetic force, X, 0, Z the components of the electric force, then if m is the mass of an ion, e its charge, and x, y, z its coordinates the equations of motion are

$$m \frac{\dot{d}^2 x}{dt^2} = Xe - He \frac{dy}{dt} \qquad (1),$$

$$m \frac{d^2 y}{dt^2} = He \frac{dx}{dt} \qquad (2),$$

$$m \frac{d^2 z}{dt^2} = Ze \qquad (3).$$

From equation (3) we have

$$z = \frac{1}{2} \frac{Ze}{m} t^2 + w_0 t$$
 .....(4),

where  $w_0$  is the velocity of projection parallel to z, the origin of coordinates being supposed to be taken at the point of projection.

From equations (1) and (2) we have

where a, c, A and B are arbitrary constants and  $\omega = He/m$ . Writing equations (5) and (6) in the form

$$y - c = \frac{X}{\omega H} \omega t + A' \cos(\omega t - \alpha),$$
  
$$x - a = -A' \sin(\omega t - \alpha);$$

we see that the projection of the path of the ion on the plane of xy is a trochoid, generated by a circle whose radius is  $X/\omega H$  rolling on a line perpendicular to the electric force, the distance of the tracing point from the centre of the rolling circle being A'. Since the average value of the periodic terms tends to vanish when the time over which the average extends is large compared with  $1/\omega$  we see, from equations (5) and (6), that the equations

$$y = c + \frac{X}{H}t,$$
$$x = a,$$

give the average positions of the ion, and that the average velocity parallel to y is X/H while that parallel to x vanishes. As the velocity parallel to z at the time t is  $\frac{Ze}{m}t+w_0$  we see that if Z is finite the velocity parallel to z will ultimately become infinite compared with the components parallel to the other axes, thus in this case the ions will ultimately move along the lines of magnetic force; we must remember however that this reasoning only applies when the electric field has a finite component in this direction.

If we determine the constants in (5) and (6) in terms of  $v_0$ ,  $u_0$ , the initial values of the components of the velocity of projection of the ion parallel to the axes of y and x respectively, we have, the origin being taken at the point of projection,

$$y = \frac{u_0}{\omega} (1 - \cos \omega t) + \frac{X}{H} t + \left( v_0 - \frac{X}{H} \right) \frac{1}{\omega} \sin \omega t \dots (7),$$
  
$$x = \left( \frac{X}{H} - v_0 \right) \frac{1}{\omega} (1 - \cos \omega t) + \frac{u_0}{\omega} \sin \omega t \dots (8).$$

If X = 0, i.e. if the directions of the electric and magnetic forces coincide, we have

$$\left(x + \frac{v_0}{\omega}\right)^2 + \left(y - \frac{u_0}{\omega}\right)^2 = \frac{v_0^2 + u_0^2}{\omega^2},$$

thus the projection of the path of the ion on the plane of xy is a circle and the path of the ion is a helix of gradually increasing pitch with its axis parallel to the lines of magnetic force.

If Z = 0, *i.e.* if the electric force is at right angles to the magnetic, and if in addition  $u_0$ ,  $v_0$ ,  $w_0$  all vanish, we have

$$y = \frac{X}{\omega H} (\omega t - \sin \omega t),$$
  
$$x = \frac{X}{\omega H} (1 - \cos \omega t).$$

This is the equation to a cycloid, the radius of the generating circle being  $X/\omega H$  or  $Xm/eH^2$ , the line on which it rolls is perpendicular to the electric force. The greatest distance which the particle can get from its point of projection measured in the direction of the electric force is  $2Xm/eH^2$ , the average velocity in this direction is zero while the average velocity parallel to y, i.e. in the direction at right angles both to the electric and magnetic forces, is finite and equal to X/H. If the ion were projected with the velocity w parallel to the axis of z it would retain this velocity unaltered and the average direction of motion of the ion would be at right angles to the electric force and along a line making an angle  $\tan^{-1} X/wH$  with the direction of the magnetic force.

47. If 
$$u_0 = 0$$
 and  $v_0 = X/H$  we have  $y = v_0 t$ ,  $x = 0$ .

Thus in this case the path of the ion in the plane of xy is the same as if there were neither electric nor magnetic forces acting upon it: the force Xe acting on the particle due to the electric field is in this case just balanced by the force Hev due to the magnetic field.

48. Returning to the general case represented by equations (7) and (8) we easily deduce that the maximum velocity V parallel to the plane of xy attained by the ion is given by the equation

$$V = \frac{X}{H} + \left\{ u_0^2 + \left( \frac{X}{H} - v_0 \right)^2 \right\}^{\frac{1}{2}},$$

thus until  $u_0$  and  $v_0$  are comparable with X/H, the maximum velocity attained is very approximately 2X/H and is independent of the velocity of projection, and the charge and the mass of the ion.

The maximum displacement  $\xi$  measured parallel to the direction of the electric force is given by the equation

$$\boldsymbol{\xi} = \left\{ \begin{matrix} \boldsymbol{X} \\ \boldsymbol{H} - \boldsymbol{v_0} \end{matrix} \right\} \frac{1}{\omega} + \frac{1}{\omega} \left\{ \boldsymbol{u_0}^2 + \left( \begin{matrix} \boldsymbol{X} \\ \boldsymbol{H} - \boldsymbol{v_0} \end{matrix} \right)^2 \right\}^{\frac{1}{2}},$$

and thus until  $u_0$  and  $v_0$  become comparable with X/H the distance travelled by the ion parallel to the lines of electric force will be very approximately independent of the velocity of projection of the ion.

It will be gathered from the preceding discussion that except in the special case when the electric and magnetic forces are at right angles to each other, the ions ultimately travel along lines of magnetic force.

49. The case when the electric and magnetic forces are at right angles to each other is however a very important one as it includes the fields produced by electric waves. In these waves the electric and magnetic forces are not constant but in the case of a simple harmonic wave may be taken as proportional to  $\cos pt$ . When the waves are all divergent the electric force is equal to V times the magnetic force, where V is the velocity with which the electric waves travel through the medium. Thus if the direction of propagation of the wave is parallel to the axis of y and if the magnetic force is parallel to the axis of y and if the magnetic force will be parallel to the axis of y and equal to y and y are equal to y. The equations of motion of a charged particle acted on by this electric wave are

$$\begin{split} m\,\frac{d^2x}{dt^2} &= e\left(V - \frac{dy}{dt}\right) H_0 \cos\,\theta, \\ m\,\frac{d^2y}{dt^2} &= e\,\frac{dx}{dt}\,H_0 \cos\,\theta. \end{split}$$

From these equations we have, if dx/dt and  $\theta$  vanish simultaneously,

$$\frac{dx}{dt} = -\frac{e}{m} \frac{V}{p} H_0 \sin \theta,$$

$$\frac{d^2 2\theta}{dt^2} + \frac{H_0^2 e^2}{m^2} \sin 2\theta = 0.$$

The character of the motion of the ions will depend upon the value of  $H_0e/pm$ ; if this quantity is large the average velocity of the ions parallel to x will vanish while that parallel to y will be equal to V: thus the wave will in this case carry the charged particles along with it. When however  $H_0e/pm$  is a small quantity the effect of the wave will be to superpose on the undisturbed motion a small vibratory motion parallel to the electric force in the wave and thus at right angles to its direction of propagation.

### CHAPTER V.

# DETERMINATION OF THE RATIO OF THE CHARGE TO THE MASS OF AN ION.

**50**. The value of e/m—the charge on an ion divided by its mass—has been determined by the application of some of the results discussed in the preceding chapter. The first case we shall consider is that of the ions in the cathode rays.

In the chapter on cathode rays we shall give the evidence which leads us to the conclusion that the cathode rays, i.e. the streams which in a highly exhausted tube through which an electric discharge is passing start from the cathode and produce a vivid phosphorescence when they strike against the glass of the tube, consist of negatively electrified particles starting from the neighbourhood of the cathode and moving with a very high velocity along straight lines. Assuming that this is the nature of the cathode rays we shall show here how to determine the velocity of the particles and the value of e/m. Suppose that we have a highly exhausted tube of the pattern shown in Fig. 28.

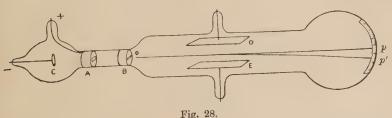


Fig. 28.

In this tube C is the cathode, A the anode, B is a thick metal disc connected with the earth, holes a millimetre or so in diameter are bored through the middle of the disc and through the anode; some of the cathode rays starting from the neighbourhood of the cathode pass through these holes, thus in the part of the tube to the right of the disc we have a pencil of negatively electrified particles travelling along straight lines parallel to the line joining the holes in the discs, the place where they strike the glass being marked by a patch of bright phosphorescence p. Suppose now that the tube is placed in a uniform magnetic field, the lines of force being at right angles to the path of the ions, the paths of the ions will now be circles, the radii of the circles being (see p. 82) mv/eH, where m is the mass of the ion, e its charge, v its velocity, and H the strength of the magnetic field. The place at which these particles strike the tube will no longer be at p but at some other point p', the direction of pp' being at right angles to the magnetic force. Since op' is an arc of a circle of which op is a tangent, we have

$$pp'(2R + pp') = op^2,$$

where R is the radius of the circle; hence

$$2R = \frac{op^2}{pp'} - pp',$$

or, since R = mv/eH, we have

$$2 \frac{mv}{eH} = \frac{op^2}{pp'} - pp'.$$

If the magnetic field is not uniform we may proceed as follows. Since  $\rho$  the radius of curvature at any point of the path of the ion is given by the equation

$$\frac{1}{\rho} = \frac{He}{vm}$$
,

and since, when the path of the ion is fairly flat  $1/\rho$  is very approximately equal to  $d^2y/dx^2$  where y and x are the coordinates of the ion, x being measured along the undisturbed path, and y at right angles to it. We have

$$\frac{d^2y}{dx^2} = \frac{He}{vm},$$

so that

$$pp' = \frac{e}{vm} \int_0^{op} \left[ \int_0^x H dx \right] dx \dots (1).$$

Hence if we measure pp' and know the distribution of the magnetic force H along the tube we can from this equation

determine the value of e/vm. This gives us a relation between vand m/e. We can determine v in the following way: two parallel metal plates D and E are placed in the tube, the plates being parallel to the lines of magnetic force and parallel also to the undisturbed path of the rays; these plates are maintained at a known difference of potential by connecting them to the terminals of a battery. Thus we have an electric field between the plates the lines of force of which are at right angles to the lines of magnetic force and to the direction of motion of the ions; this electrostatic force Y tends to deflect the ions, the force acting on an ion being Ye; the force due to the magnetic field acts in the same straight line and is equal to Hev. Adjust the sign of the difference of potential so that the electric and magnetic forces tend to oppose each other, then keeping one of the forces fixed, say the electric force, alter the value of the other until the two forces just balance, this stage can be ascertained by observing when the phosphorescent patch p' is restored to its undisturbed position. When this stage is reached we have

$$Ye = Hev,$$

$$v = \frac{Y}{H} \qquad \dots (2).$$

or

Thus by measuring Y/H we can determine the velocity of the ions composing the cathode rays. As we know e/vm from the experiments on the magnetic deflection we can in this way deduce the values of both e/m and v. Equation (2) depends upon the assumption that both the magnetic and electric fields are uniform, if this condition is not fulfilled we must proceed as follows. Suppose that p'' is the displaced position of p when the electric field alone is acting on the rays, then we can prove without difficulty that

 $pp'' = \frac{e}{v^2 m} \int_0^{op} \left[ \int_0^x Y dx \right] dx \dots (3),$ 

hence if we know the distribution of the electric field and the value of pp'' we can by equation (3) find the value of  $e/v^2m$  and since by equation (2) we can determine e/vm we have the data for determining both v and e/m.

In order to apply this method it is necessary that the pressure of the gas in the discharge tube in which the rays are produced should be very low; the passage of cathode rays through a gas makes it a conductor and thus as the rays are shielded from the electrostatic field by the gas through which they move the electrostatic repulsion is hardly appreciable; if, however, the pressure of the gas is very low the conductivity of the gas is so small that there is hardly any appreciable shielding effect and the deflection produced by the electric field is easily observed.

Using this method the author in 1897\* obtained the values for v and e/m given in the following table: the first column contains the name of the gas filling the tube: the different numbers given under one gas relate to experiments made at different pressures.

Gas	. v	m/e	Gas	v	m/e
Air	$2.8 \times 10^{9}$ $2.8 \times 10^{9}$ $2.3 \times 10^{9}$ $3.6 \times 10^{9}$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Air* Hydrogen Carbonic ) acid }	$2.8 \times 10^{9}$ $2.5 \times 10^{9}$ $2.2 \times 10^{9}$	$ \begin{array}{c}                                     $

The mean of the values of m/e is  $1.3 \times 10^{-7}$  or  $e/m = 7.7 \times 10^{6}$ . We see too that within the limits of the errors of the experiments the value of e/m is the same whether the tube be filled with air, hydrogen or carbonic acid, so that it does not depend upon the nature of the gas. This result was first obtained by the writer + by another method; the pressure in the discharge tube was adjusted so that the potential difference between the electrodes in the discharge tube was the same for all the gases tried, photographs were taken of the rays when deflected by a constant magnetic field and from these it was found that the deflected rays occupied the same position whether the gas in the tube was hydrogen, air, carbonic acid or methyl iodide; these gases give a wide range of densities as the density of methyl iodide is about 70 times that of hydrogen. The constancy of the value of e/m for the ions which constitute the cathode rays is in striking contrast to the variability of the corresponding quantity in the ions which carry the current through liquid electrolytes. Experiments were made on the effect of altering the metal of which the cathode was made, the experiments marked with an asterisk in the preceding

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 44, p. 293, 1897.

<sup>+</sup> J. J. Thomson, Proc. Camb. Phil. Soc. ix. p. 243, 1897.

table were made with platinum electrodes, all the others were made with aluminium electrodes; it will be seen that the values of e/m are the same in the two cases. A further series of experiments on this point has been made by H. A. Wilson\* who used cathodes made of aluminium, copper, iron, lead, platinum, silver, tin and zinc and found the same value for e/m in all cases.

If we compare the value of e/m viz.  $7.7 \times 10^6$  for the ions in the cathode rays with the value of the corresponding quantity for the ions which carry the current through liquid electrolytes we are led to some very interesting conclusions; the greatest value of e/m in the case of liquid electrolysis is when the ion is the hydrogen ion, in this case e/m is about  $10^4$ . When we discuss the electric charge carried by the ion in the cathode rays we shall find that it is equal in magnitude to the charge carried by the hydrogen ion, in liquid electrolysis; it follows then that the mass of the hydrogen ion must be 770 times that of the ion in the cathode rays; hence the carrier of the negative electricity in these rays must be very small compared with the mass of the hydrogen atom. We shall return to this point when we have studied other phenomena involving gaseous ions.

#### Ions in Lenard rays.

51. Lenard  $\dagger$  has determined by the method just described the velocity and the value of e/m for the Lenard rays; these are cathode rays which have escaped from the discharge tube through a window of very thin aluminium foil. In his experiments after escaping from the discharge tube they entered a highly exhausted vessel where they were deflected by electric and magnetic forces in the way described in the preceding article; the results of these experiments are given in the following table.

v cm./sec.	e/m		
$\begin{array}{c} 6.7 \times 10^{9} \\ 7 \times 10^{9} \\ 8.1 \times 10^{9} \end{array}$	$6.49 \times 10^{6}$ $6.32 \times 10^{6}$ $6.36 \times 10^{6}$		

<sup>\*</sup> H. A. Wilson, Proc. Camb. Phil. Soc. xi. p. 179, 1901.

<sup>+</sup> Lenard, Wied. Ann. xliv. p. 279, 1898.

The mean of the values of e/m is  $6.39 \times 10^6$  which agrees well with the value  $7.7 \times 10^6$  found above. It will be noticed that the velocities of the ions in this case are much greater than in the preceding, taking the two sets together we have velocities of the ions ranging from  $2.2 \times 10^9$  to  $8.1 \times 10^9$  cm./sec. without any indication of a change in the value of e/m.

Lenard\* has also made some very interesting experiments on the effect of an external electric field in accelerating or retarding the motion of the ions. The apparatus used for this purpose is shown in Fig. 29.

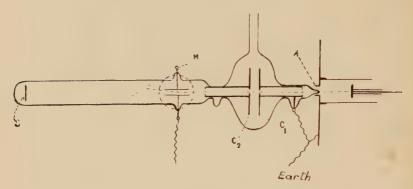


Fig. 29.

The rays after coming through the window A pass through small holes in two parallel circular metallic plates  $C_1$  and  $C_2$ ; of these  $C_1$  is always kept connected with the earth while  $C_2$  is charged positively or negatively by means of an electrical machine; after leaving this condenser the rays pass between two plates M, used for producing the electrostatic deflection, on to a screen S; the dotted circle round M represents the coil used for producing the magnetic deflection. The velocities of the ions were measured (1) when the plates of the condenser  $C_1C_2$  were at the same potential, (2) when they were maintained at different potentials; it was found that when the plate  $C_2$  was negatively electrified the velocity in case (2) was less than that in (1) while when the plate  $C_2$  was positively electrified it was greater; if  $v_1$  is the velocity of the ions in case (1),  $v_2$  that in case (2), then assuming that the

<sup>\*</sup> Lenard, Wied. Ann. xlv. p. 504, 1898.

whole change in the energy is due to the action of the electric field we have

$$\frac{1}{2}m\left(v_{2}^{2}-v_{1}^{2}\right)=eV.....(1),$$

where V is the potential difference between the plates, V being taken positive when  $C_2$  is at a higher potential than  $C_1$ . The results of Lenard's experiments are given in the following table, the fourth column contains the value e/m calculated by equation (1).

$v_1(\mathrm{cm./sec.})$	$v_2(\mathrm{cm./sec.})$	V (electromagnetic units)	e/m
$\begin{array}{c} .7 \times 10^{10} \\ .68 \times 10^{10} \\ .62 \times 10^{10} \\ .77 \times 10^{10} \\ .79 \times 10^{10} \\ .88 \times 10^{10} \end{array}$	$\begin{array}{c} 35 \times 10^{10} \\ 34 \times 10^{10} \\ 89 \times 10^{10} \\ 47 \times 10^{10} \\ 10 \times 10^{10} \\ 107 \times 10^{10} \end{array}$	$\begin{array}{c} -291\times 10^{10} \\ -210\times 10^{10} \\ +291\times 10^{10} \\ -291\times 10^{10} \\ +291\times 10^{10} \\ +291\times 10^{10} \\ +291\times 10^{10} \end{array}$	$6.2 \times 10^{6}$ $8.1 \times 10^{6}$ $6.9 \times 10^{6}$ $6.4 \times 10^{6}$ $6.6 \times 10^{6}$ $6.5 \times 10^{6}$

The constancy of the value of e/m is a strong confirmation of the truth of the theory that the rays are charged particles in rapid motion.

Method of determining the value of e/m and v by measuring the energy carried by the cathode rays.

52. Many other methods have been employed to measure e/m. One used by the writer\* was to measure the energy carried by the rays. To do this a narrow pencil of rays passed through a small hole in a metal cylinder and fell upon a thermo-couple, the couple was heated by the impact of the rays, and by measuring by means of a galvanometer the rate at which the temperature of the junction increased, the amount of heat communicated to the junction in unit time was determined, let us call this amount Q; then if we assume that all the energy possessed by the cathode rays is converted into heat we have

$$\frac{1}{2}Nmv^2 = Q,$$

where N is the number of ions which enter the cylinder through the hole in unit time, m is the mass and v the velocity of an ion.

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 44, p. 293, 1897.

If e is the charge of the ion, then in each unit of time Ne units of negative electricity will enter the cylinder; the rate at which the negative charge increases can easily be measured if the cylinder is insulated and connected with an electrometer, let E be the rate of increase of the negative electricity inside the cylinder, then we have

$$Ne = E$$
.

Eliminating N from these equations we get

$$\frac{1}{2} \frac{m}{e} v^2 = \frac{Q}{E}.$$

If we observe the magnetic deflection produced by a known magnetic field we determine mv/e, hence since we have just seen how to determine  $mv^2/e$  we can deduce the values of v and m/e.

The results of experiments made in this way are shown below.

Gas	v	e/m
Air	$2.4 \times 10^9$ $3.2 \times 10^9$ $2.5 \times 10^9$	$1.1 \times 10^{7}$ $1.4 \times 10^{7}$ $1.0 \times 10^{7}$

The mean of the values for e/m is  $1.17 \times 10^7$ : this value is considerably greater than the one previously found, the method however is not so reliable as the preceding one as three measurements have to be made, the magnetic deflection, the heating effect and the rate of increase of the charge in the cylinder, instead of two, the magnetic and the electric deflection; and it is not merely that the measurements are more numerous, they are also more difficult, as the measurement of the heating effect and the rate of increase of the charge are much more complicated than that of the electrostatic deflection. The conductivity given to the gas by the passage through it of the cathode rays allows some of the charge in the cylinder to leak away and thus tends to make the observed value of E smaller than the true one; in the experiments described above efforts were made to diminish this effect as much as possible by connecting the cylinder to a condenser of large capacity so that the negative charge on the rays should

only produce a small change in the potential of the cylinder. We may remark in passing that the charges of negative electricity carried by the rays are very large, thus with quite a small hole (about 1 mm. in radius) in the cylinder the potential of the cylinder would change sometimes as such as 5 volts per second when exposed to the rays, even though it was connected with a condenser having a capacity about 15 microfarad.

Methods of determining v and e/m from the magnetic deflection and potential difference between the electrodes of the discharge tube.

53. These methods which were first used by Schuster\* in 1890 are based on the following principles. If V is the potential difference between the terminals of the tube, then the work done on an ion in passing from one end of the tube to the other is Ve, hence the kinetic energy acquired by the ion can not be greater than Ve, so that

$$\frac{1}{2}mv^2 \Rightarrow Ve.$$

From the observation of the effect of the magnet on the discharge (Schuster measured the radii of the circles which are the path of the ions in a strong magnetic field) we know the value of mv/e, let us call this quantity q, then from the preceding equation we have

 $e/m \Rightarrow \frac{2V}{q^2}$ .

To find an inferior limit for e/m, Schuster took v equal to the velocity of mean square of the atoms of the gas in the tube; calling this velocity U we have

 $e/m \lessdot \frac{U}{q}$ .

Substituting the values of q and V found in his experiments Schuster found for air

 $e/m \geqslant 11 \times 10^5$ ,  $e/m \leqslant 10^3$ .

If we assume that the charge on the nitrogen atom is three times that on the atom of hydrogen in the electrolysis of liquids and if

<sup>\*</sup> Schuster, Proc. Roy. Soc. xlvii. p. 526.

m is the mass of the nitrogen atom, then e/m is equal to  $2 \times 10^3$ ; as this is within the limits for e/m previously found, Schuster concluded that the negatively electrified particles in the cathode rays in a tube filled with nitrogen are atoms of nitrogen. We have seen that more recent investigations have led to quite a different conclusion.

**54.** Several determinations of the values of e/m and v have been made on the assumption that the kinetic energy possessed by the ion is equal to the energy that would be acquired by the ion in falling through the potential difference V between the anode and the cathode; on this assumption we have

and if q or mv/e is determined by the magnetic deflection we have

$$\frac{e}{m} = \frac{2V}{q^2}.$$

Determinations of e/m on this principle have been made by Kaufmann\* and subsequently by Simon†. Kaufmann found by this method that

$$\frac{e}{m} = 1.86 \times 10^r.$$

And Simon, who made a very large number of experiments in which the potential difference between the cathode and anode ranged from 4860 to 11840 volts, found that

$$\frac{e}{m} = 1.865 \times 10^7.$$

The value of e/m was found to be independent of the potential difference. A Wimshurst machine was used to produce the discharge as this maintains a very much more uniform potential difference than an induction coil.

The values found for e/m by this method are larger than those found by the methods previously described; the method is however open to objection, for it assumes that the kinetic energy of the ion is equal to the work done on an ion starting in the cathode itself and thus experiencing the maximum fall of

<sup>\*</sup> Kaufmann, Wied. Ann. v. 61, p. 544; 62, p. 596, 1897; 65, p. 431, 1898.

<sup>+</sup> Simon, Wied. Ann. v. 69, p. 589, 1899.

potential possible in the tube, and also that all the work done by the electric field is spent in increasing the kinetic energy of the ion while none of this energy is lost by the collisions of the ion with the molecules of the gas through which it passes. Now we have no right to assume without proof that the ion starts from the cathode itself; we shall see that, at any rate when the pressure is not very low, large numbers of ions are produced at some little distance away from the cathode, and as the change of potential in the neighbourhood of the cathode is very rapid such ions would experience a notably smaller potential fall than those starting from the cathode itself. Nor is the fact that the values of e/m found by this method are independent of the potential difference a conclusive proof that the ions under observation started from the cathode. For suppose that the distance from the cathode of the place from which the greater part of the ions start is d, and that  $V\beta$  is the potential gradient, then the fall of potential experienced by these ions is  $V(1-\beta d)$ ; now  $\beta$  diminishes as the pressure of the gases diminishes while d increases, so that it is quite possible that  $\beta d$  is independent of the pressure of the gas (it would be so if for example  $\beta$  were directly and d inversely proportional to the pressure); in this case the fall of potential experienced by the ions would always be a constant fraction of the total fall of potential in the tube, so that the value of e/mdetermined by equation (1) would always bear a constant ratio to the true value. As the maximum potential difference used by Simon was only about 1100 volts the pressure could not have been very low in his experiments. When the pressure of the gas is exceedingly small the number of collisions with the molecules of a gas made by an ion in its journey down the tube may be so greatly reduced that but few fresh ions are produced by the collisions and in this case the greater number of the ions may come from the electrode itself, but even in this case the use of equation (1) is not legitimate, as part of the work may be spent in tearing the ions out of the metal and only the remainder is available for increasing the kinetic energy.

These considerations show that the use of equation (1) leads to an over-estimate of the kinetic energy of the ion and therefore, since  $e/m = mv^2/eq^2$ , the value of e/m calculated by this method will tend to be too large.

The method used by Lenard, and described on page 96, though it depends upon the same equations is not open to these objections, as in this method the potential difference which enters into the equations is applied to the ions after they have been produced and started on their path, and in this case the increase in the kinetic energy must equal the work done if we can neglect the loss of kinetic energy of the ions produced by collisions with the molecules of the gas; this effect can be eliminated by working at very low pressures and varying the length of path traversed by the ion under the electric field.

55. In January, 1897, Wiechert\* published a determination of the values between which e/m must lie. The principles on which this determination is based are as follows: by measuring the magnetic deflection in a field of known strength we can determine  $\frac{m}{e}v$ ; to get a second relation between m/e and v, Wiechert put

$$\frac{1}{2}\frac{m}{e}v^2 = kV....(1),$$

where V is the difference of potential between the electrodes in the discharge tube and k an unknown quantity which cannot be greater than unity. To get the maximum value of v, and therefore the maximum of e/m, k in equation (1) was put equal to unity. To get minimum values for v and e/m Wiechert assumed that the kinetic energy of the ions in the cathode rays was greater than that due to a fall through a potential difference equal to the 'cathode fall of potential.' The cathode fall of potential is the difference between the potential of the cathode and that of a point on the outer boundary of that dark space in the discharge which adjoins the cathode. Warburg has shown that this cathode fall of potential is independent of the magnitude of the current through the gas, of the pressure of the gas and, within certain limitations, of the nature of the electrodes. As its value in air is about 270 volts, Wiechert assumed that a minimum value for kV was 200 volts. The grounds for this assumption do not seem obvious; a priori it would seem more probable that the minimum value to take for kV should have been the potential difference.

<sup>\*</sup> Wiechert, Sitzungsber. d. Physikal, -ökonom. Gesellsch. zu Königsberg, i. Pr. 38, p. 1, 1897.

not between the cathode and the outer boundary of this dark space, but between this boundary and the place where the magnetic deflection of the rays was determined, for we know that the rays are fully developed at this boundary, and it is by no means so certain that at moderate pressures they all exist close to the cathode. Using these assumptions, however, Wiechert found for the maximum value of e/m the value  $4 \times 10^7$  and for the minimum value  $4 \times 10^6$ .

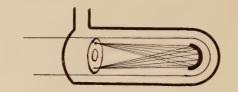
56. Wiechert\* has also determined by direct measurement the velocity of the ions in the cathode rays, using a method first applied by Des Coudres+ for this purpose. The principle of the method is as follows: suppose that ABCD, A'B'C'D' are two circuits traversed by very rapidly alternating currents, such as those produced by the discharge of a Leyden jar, let us suppose that the currents in the two circuits are in the same phase, and that these circuits are placed close to a tube along which cathode rays are passing. The currents in the circuits will give rise to electric and magnetic forces which will deflect the rays as they pass by the circuits. If the velocity of the rays were infinite, then the deflections produced by the two circuits on the rays would be equal and in the same direction; if however the rays take a finite time to travel from one circuit to the other, and if the distance between the circuits is adjusted so that this time is equal to half the period of vibration of the current, then the deflection produced by the first circuit will be equal and opposite to that produced by the second; or if the distance between the circuits is such that the time taken by the rays to pass from one circuit to the other is equal to one quarter of the period of the currents, then when the effect produced by the circuit  $\overline{ABCD}$  is a maximum that produced by A'B'C'D' will be zero.

The arrangement used to apply these principles to determine the velocity of the cathode rays is represented in Fig. 30; ABCD, A'B'C'D' are the circuits carrying the currents produced by the discharge of the jars, C is a concave cathode,  $B_1$ ,  $B_2$  metal diaphragms perforated at the centre, G a screen covered with some material which becomes phosphorescent when bombarded by the

<sup>\*</sup> Wiechert, Wied. Ann., 69, p. 739, 1899.

<sup>+</sup> Des Coudres, Verhandl. d. physikal. Gesellsch. zu Berlin, xiv. p. 86, 1895.

cathode rays. M is a horse-shoe magnet which deflects the rays from the hole in the diaphragm  $B_1$ , so that when no currents are



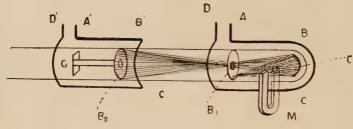


Fig. 30.

passing through ABCD, A'B'C'D' the cathode rays are stopped by the diaphragm and the phosphorescent screen remains dark. When a current passes through ABCD the pencil of cathode rays is deflected and swings backwards and forwards like a pendulum, if during the swing the pencil strikes the hole in  $B_1$  some of the rays will get through  $B_1$  and  $B_2$ , and the screen G will be illuminated. The brightness of the illumination will be greatest when the hole in  $B_1$  is just at the extremity of the swing caused by the current in ABCD, for in this case the pencil is momentarily at rest, and the time the pencil remains on the opening is therefore a maximum. If there is no current in A'B'C'D' the position of the phosphorescent spot on the screen will be on the line joining the holes in the two diaphragms; if a current in the same phase as that through ABCD is passing through A'B'C'D', then since the cathode rays that reach the diaphragm are displaced upwards by the current in ABCD, they will be similarly displaced by that in A'B'C'D', and the phosphorescent patch will be above the line joining the holes in the diaphragm, while if the current in A'B'C'D' is in the opposite phase the patch will be displaced

downwards, the direction of the displacement of the patch will be reversed by reversing the poles of the magnet. If however the phases of the currents in ABCD, A'B'C'D' differ by a quarter of a period, then when the vertical displacement due to  $\overrightarrow{ABCD}$  is a maximum that due to A'B'C'D' will be zero, and the vertical distribution of the light on the screen G will not be affected by reversing the magnet M. We can ensure that the rays which get through the opening in  $B_1$  are those which are passing when the vertical displacement due to the current in ABCD is greatest, by gradually increasing the deflection of the rays by moving the magnet M; when we have got M into such a position that any further increase in the deflection prevents any rays from reaching the screen, we know that only those which suffer the maximum deflection come under the action of A'B'C'D'; if then we move A'B C'D' into such a position that the vertical distribution of phosphorescence on the screen is not affected by reversing M, we know that when the rays are passing A'B'C'D' the current in this circuit differs in phase by a quarter period from the phase of the current in ABCD when the rays were passing that circuit. If the circuits ABCD, A'B'C'D' are arranged so that the currents in them are simultaneously in the same phase, we know that the rays must have taken a time equal to one quarter of a period of the currents to pass from ABCD to A'B'C'D'. The period of the currents can be determined by Lecher's method\*, hence knowing the distance between the circuits we can determine the velocity of the rays.

The arrangement used to carry out this method is represented in Fig. 31. CC are two pairs of parallel plates, the upper pair of plates are connected with the spark gap F, which is also connected with the terminals of an induction coil, the lower pair of plates are connected symmetrically with the circuits ABCD, A'B'C'D'. The cathode rays are produced by a system in electrical connection with that producing the alternating currents. L and L are two Leyden jars whose outer coatings are connected with the extremities of the spark gap F, the inner coatings of the jars are connected with the primary coil of a high tension transformer, the secondary coil of which is connected with the anode and cathode of the discharge tube. In order to prevent the rays being scattered to the walls of the tube during their passage

<sup>\*</sup> Lecher, Wied. Ann. 91, p. 850, 1890.

from one circuit to another a magnetising spiral was wound round the tube producing a magnetic force parallel to the length

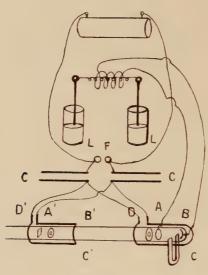


Fig. 31.

of the tube; this concentrated the rays along the axis of the tube and made the observations easier. With this contrivance it was found possible not merely to find a position of A'B'C'D', when the currents differed by a quarter of a period, when the rays passed through them, but to find the second position when they differed by three-quarters of a period.

If  $\lambda$  is the distance between the circuits when they differ by a quarter period, L the wave-length of the electrical waves passing through these circuits, v the velocity of the rays, and V the velocity of light, then

$$\frac{v}{\overline{V}} = \frac{\lambda}{L/4} \, .$$

Thus, in one experiment, L=940 cm.,  $\lambda=39$ , hence v is about  $5\times 10^{9}$ . The pressure was between  $\frac{1}{2}$  and  $\frac{1}{4}$  of a millimetre. v being determined, we get e/m from the value of mv/e, which is got by measuring the magnetic deflection of the rays. The determination of v by this method is difficult and we cannot expect a high degree of accuracy. As the result of his experi-

ments, Wiechert came to the conclusion that the value of e/m is between  $1.55 \times 10^7$  and  $1.01 \times 10^7$ . The most probable value he gives as  $1.26 \times 10^7$ .

Determination of e/m for the negative ions produced when ultraviolet light falls on a metal plate, the gas through which the ions pass being at a very low pressure.

57. The writer\* determined the values of e/m for the negative ions produced by the incidence of ultra-violet light on a metal plate by the following method. It is proved on page 88 that when an ion starts from rest from the plane x = 0, at the time t = 0, and is acted on by a uniform electric field of strength X, parallel to the axis of x, and by a uniform magnetic force H, parallel to z, the position of the particle at the time t is given by the equations

 $x = \frac{m}{e} \frac{X}{H^2} \left\{ 1 - \cos\left(\frac{e}{m} H t\right) \right\},$  $y = \frac{m}{e} \frac{X}{H^2} \left\{ \frac{e}{m} H t - \sin\left(\frac{e}{m} H t\right) \right\},$ 

where x and y are the coordinates of the ion. The path of the ion is thus a cycloid, and the greatest distance the ion can get from the plane x = 0 is equal to  $2mX/eH^2$ .

Suppose now that we have a number of ions starting from the plane x=0, and moving towards the parallel plane x=a, supposed to be unlimited in extent, if a is less than  $2mX/eH^2$  all the ions which start from x=0 will reach the plane x=a, while if a is greater than  $2mX/eH^2$  none of the ions will reach this plane. If x=0 is a zinc plate illuminated by ultra-violet light, and thus the seat of a supply of negative ions, and x=a a metal plate connected with an electrometer, then when a definite electric intensity is established between the plates, so that the number of ions which leave the plate in unit time is fixed, and if a is less than  $2Xm/eH^2$ , all the ions which start from x=0 will reach the plane x=a. Thus the rate at which the plate connected with the electrometer receives a negative charge will be the same when there is a magnetic force acting across the plate as when there is no such force. If however

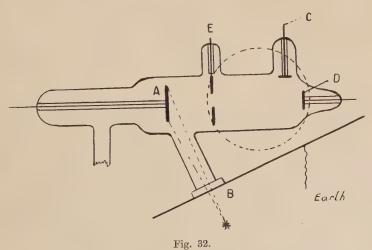
<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 48, p. 547, 1899.

a is greater than  $2Xm/eH^2$ , then no ion which starts from x=0will reach the plane x = a, and this plate will not receive any negative charge: so that in this case the magnetic field entirely stops the supply of negative electricity to the plate connected with the electrometer. Thus, on this theory, if the distance between the plates is less than a certain value, the magnetic force produces no effect on the rate at which the plate connected with the electrometer receives a negative charge, while when the distance is greater than this value the magnetic force entirely stops the supply of negative electricity to the plate. The actual phenomena are not so abrupt as this theory indicates. We find in practice that when the plates are near together the magnetic force produces only an exceedingly small effect, and this an increase in the rate of charging of the plate. On increasing the distance between the plates, we come to a stage where the magnetic force produces a very great diminution in the rate of charging; it does not, however, stop it abruptly, as there is a considerable range in which the magnetic field diminishes but does not entirely stop the supply of negative electricity to the plate. At still greater distances the current to the plate under the magnetic force is quite insignificant compared with the current when there is no magnetic field. We should get this gradual instead of abrupt decay of the current, if the ions, instead of all starting from the plane x = 0, started from a layer of finite thickness t; in this case the first ions which failed to reach the plate would be those which started from x = 0, this would occur when  $a = 2mX/eH^2$ , some ions would however continue to reach the plate until  $a = t + 2mX/eH^2$ . Thus if we measure the distance between the plates when the magnetic force first begins to retard the current, we can, if we know the values of X and H, determine the value of e/m. The finite thickness of the layer from which the ions start may be explained by the use of a principle which we shall find of great importance in many other phenomena connected with the discharge of electricity through gases: it is that when ions move through a gas with a velocity exceeding a certain limit, the ions by their collisions with the molecules of the gas through which they move produce fresh ions. Thus when the negative ions which start from the metal surface acquire under the electric field a certain velocity they will produce new ions, and thus the ionisation will not be confined to the metal plate but will extend through a layer of finite thickness.

In using this method of determining e/m it is necessary to have the gas between the plates at a very low pressure, so low that the mean free path of the ion is at least comparable with the distance between the plates; if this is not the case the resistance offered to the motions of the ions by the viscosity of the gas prevents the preceding investigation from being applicable.

The mean value of e/m found in these experiments was  $7.3 \times 10^6$ . It thus agrees very well with the value  $7.6 \times 10^6$  found for the same quantity for the carriers of the negative electricity in the cathode rays: and proves that the carriers of electricity in the two cases are the same, or, as we may express it, that a metal plate emits cathode rays when illuminated by ultra-violet light.

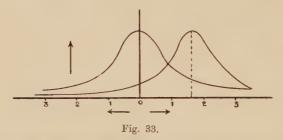
58. Lenard\* in 1900 also measured the value of e/m in the case of the discharge of negative electricity through gas at a very low pressure from a cathode illuminated by ultra-violet light. The arrangement he used is represented in Fig. 32. A is



an aluminium plate on which the ultra-violet light shines: this light comes from a spark between zinc electrodes and enters the tube through the quartz window B. E is another metal

<sup>\*</sup> Lenard, Drudes Annalen, ii. p. 359, 1900.

electrode perforated in the middle and connected with the earth, it shields the right-hand part of the apparatus from the electrostatic action of the charged electrode A. D and C are electrodes which can be connected with an electrometer. When A is charged up a stream of negative electricity goes through the opening in E, and striking against the plate D, charges up the electrometer with negative electricity. If the electrometer be connected with C instead of with D, it will not however receive any charge. We can however give C a charge by deflecting the stream of negative ions by a magnet until they strike against C. As we still further increase the magnetic field the ions will be deflected by the field past C, and the charge communicated to C will fall off rapidly. The amount of negative electricity received by the electrodes D and C respectively, as the magnetic force is increased, was in Lenard's experiments represented by the curves in Fig. 33. The ordinates are the charges received by the electrodes and the abscissae the values of the magnetic force. The curve to the left is for the



electrode D, that to the right for C. Since the negative ions are not exposed to any electric field in the part of the tube to the right of E their paths in this region under a constant magnetic field will be circles whose radii are equal to mv/eH. Now C will receive the maximum charge when the circle with this radius passing through the middle of the hole in E, and having its tangent at this point horizontal, passes also through the middle of the electrode C. The radius E0 of this circle is fixed by the relative positions of E1 and E2. Hence, if we measure E3 when E4 receives its maximum charge, we have

$$R = \frac{mv}{eH} \dots (1).$$

The velocity is determined by the assumption that the work

done by the electric field, when the ion passes from A to E, is spent in increasing the kinetic energy of the ion (we have already considered on page 100 the objections which may be raised against this assumption): this leads to the equation

$$\frac{1}{2}mv^2 = Ve \dots (2),$$

where V is the potential difference between A and E. From equations (1) and (2) the values of e/m and v can be determined. In this way Lenard found that e/m for the negative ions produced by the action of ultra-violet light in a gas at a very low pressure is equal to  $1.15 \times 10^7$ .

**59**. Value of e/m for the negative ions produced by an incandescent wire.

A metal wire when raised to a white heat in a gas at a very low pressure gives out negative ions; the writer\* has determined the value of e/m for the negative ions given out by an incandescent carbon filament in hydrogen at a very low pressure. The method used was the same as that used by him to determine the value of e/m for the ions produced by the action of ultra-violet light, and which has already been described on page 107. The value of e/m found in this way was  $8.7 \times 10^6$ , which agrees within the errors of experiment with the values found for e/m for the ions in the cathode rays, and for those produced by the action of ultra-violet light.

**60.** Value of e/m for the negative ions emitted by radio-active substances.

It has been shown by M. and Madame Curie<sup>†</sup> that the radioactive substance radium emits negative ions. The velocity of these ions and the value of e/m have been determined by Becquerel<sup>‡</sup>. The method he employed was to measure the deflections of the rays produced by an electrostatic and also by a magnetic field. The experiments were made at atmospheric pressure, and the resistance offered to the motion of the ions by the gas through which they pass was neglected: this would not be justifiable in

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 48, p. 547, 1899.

<sup>†</sup> M. et Mme. Curie, Comptes Rendus, t. 130, p. 647. ‡ Becquerel, Rapports présentés au Congrès International de Physique à Paris, t. iii. p. 47, 1900.

the case of the ions we have hitherto been considering, but as the ions emitted by radium are very much more penetrating than those we have hitherto considered, and are able to travel as far through a gas at atmospheric pressure as other kinds of ion travel through a gas at a very low pressure, we shall probably get approximately the right values for e/m and v for the radium ions even if we neglect the resistance of the gas. The radium was placed below two parallel vertical metal plates, about 3.5 cm. wide and 1 cm. apart; above these metal plates was a horizontal photographic plate protected by a covering of black paper from the action of light; a thin slip of mica, symmetrically situated with respect to the metal plates, was placed over the radium, this cast a shadow on the photographic plate which when the metal plates were at the same potential was at the middle of the field; when a great difference of potential, 10,200 volts, was maintained between the plates the position of this shadow was displaced towards the positive plate. Consider an ion passing between the plates, then if l is the length of its path between the plates, F the electric force acting upon it, the displacement of the ion parallel to the lines of electric force when it leaves the region between the plates

is  $\frac{1}{2} \frac{Fe}{m} \frac{l^2}{v^2}$ , and its direction of motion is displaced through an angle  $\tan^{-1} \frac{Fe}{m} \frac{l}{v^2}$ , hence if h is the vertical distance of the photo-

graphic plate above the upper edge of the parallel metal plate, the point where the ion strikes the plate will be deflected through a space  $\delta$  parallel to the line of electric force, where  $\delta$  is given by the equation

$$\begin{split} \delta &= \frac{1}{2} \; \frac{Fe}{m} \; \frac{l^2}{v^2} + h \, \frac{Fe}{m} \; \frac{l}{v^2} \\ &= \frac{Fe}{m} \; \frac{l}{v^2} \left\{ \frac{l}{2} + h \right\} \, . \end{split}$$

The magnetic deflection was found in the following way: a small quantity of radium was placed in a little lead saucer on a photographic plate; as none of the rays from the radium reach the plate the latter is not affected; if however a strong magnetic field, with the lines of force parallel to the plate, acts on the negative ions coming from the radium, these will be bent round and will strike the plate, producing a photograph.

To find the boundary of this photograph, let us take the plane of the photographic plate as the plane of xy, the magnetic force H being parallel to x; the equations of motion of an ion are

$$m \; rac{d^2 x}{dt^2} = 0, \qquad m \; rac{d^2 y}{dt^2} = He \, rac{dz}{dt} \,, \qquad m \; rac{d^2 z}{dt^2} = - \, He \, rac{dy}{dt} \,;$$

the solutions of these equations are, if  $\omega = He/m$ , and u, A, B are constants,

$$x = ut,$$
  

$$y = A (1 - \cos \omega t) + B \sin \omega t,$$
  

$$z = A \sin \omega t + B (\cos \omega t - 1).$$

If v and w are the values of dy/dt, dz/dt when t=0, we have

$$y = \frac{w}{\omega} (1 - \cos \omega t) + \frac{v}{\omega} \sin \omega t,$$
  
$$z = \frac{w}{\omega} \sin \omega t + \frac{v}{\omega} (\cos \omega t - 1);$$

when the ion strikes the plane we have z = 0, hence

$$\tan \tfrac{1}{2} \omega t = \frac{w}{v} \,.$$

Now if the ion is projected so as to make an angle  $\theta$  with the direction of the magnetic force, and if the plane through the direction of projection and the axis of x makes an angle  $\phi$  with the plane of xz, we have, if V is the velocity of projection,

 $u = V \cos \theta$ ,  $v = V \sin \theta \sin \phi$ ,  $w = V \sin \theta \cos \phi$ ,

hence.

 $\tan \frac{1}{2}\omega t = \cot \phi$ 

$$=\tan\left(\frac{\pi}{2}-\phi\right)$$
,

thus

$$\omega t = \pi - 2\phi$$
.

Substituting this value for t, we find, if  $\xi$  and  $\eta$  are the coordinates of the point where the ion strikes the photographic plate

$$\xi = \frac{V \cos \theta}{\omega} (\pi - 2\phi),$$
$$\eta = \frac{2V \sin \theta \cos \phi}{\omega}.$$

Thus, for the particles projected in a plane through the axis of x, the locus of the points where they strike the plate will be

an ellipse whose semi-axes are  $\frac{2V\cos\phi}{\omega}$  and  $\frac{V(\pi-2\phi)}{\omega}$ . For the particle projected in the plane of xz, the semi-axes of the ellipse are  $2V/\omega$  and  $\pi V/\omega$ . An example of such an ellipse is shown in Fig. 34 which is copied from a photograph by Becquerel.



Fig. 34.

By the measurement of the axes of the ellipse we can determine  $V/\omega$ , i.e. Vm/eH. As the radium emits ions having velocities extending over a considerable range, the impression on the plate is not the arc of a single ellipse, but a band bounded by the ellipses corresponding to the smallest and greatest velocities of the ions. Becquerel took photographs when the ions from the radium went (1) through the air at atmospheric pressure, and (2) through air at very low pressure; the photographs were found to be identical, in fact one-half of the photograph represented in Fig. 34 is produced by ions going through air at atmospheric pressure, and the other half by ions going through air at a very low pressure. The identity of the results in the two cases justifies us in our neglect of the resistance of the air.

A simpler method than the electrostatic method used by Becquerel to get a second relation between v and e/m, would be to place the radium on a photographic plate in a little tube so that all the ions start at right angles to the plate. A uniform magnetic field acts parallel to the plate, and above the photographic plate and parallel to it is a metal plate which is connected with an electric machine; when this plate is charged with electricity there will be a strong electric field acting on the ion parallel to its direction of projection and at right angles to the magnetic force. If photographs are taken (1) with the plate uncharged, (2) with the plate charged, the two photographs will give us a simple method of finding v and e/m. For let us suppose that all the ions have the same velocity V, the distance 2R of

the image from the radium in the first photograph is given by the equation

 $R = \frac{m}{e} \ \frac{V}{H} \,.$ 

To find the distance of the image in the second photograph, let us take the same axes as before, and let Z be the electric force at right angles to the plate, then the equations of motion of an ion are

$$\begin{split} m \; \frac{d^2z}{dt^2} &= Ze - He \; \frac{dy}{dt} \; , \\ m \; \frac{d^2y}{dt^2} &= He \; \frac{dz}{dt} \; . \end{split}$$

The solution of these equations, when z, y, dy/dt vanish when t = 0, is

$$y = \frac{Z}{H} \left( t - \frac{\sin \omega t}{\omega} \right) + \frac{V}{\omega} (1 - \cos \omega t),$$
$$z = \frac{Z}{H\omega} (1 - \cos \omega t) + \frac{V}{\omega} \sin \omega t,$$

where V is the velocity of projection of the ion.

When the ion strikes the photographic plate z = 0, hence

$$\tan \frac{1}{2} \omega t = -\frac{V}{Z/H}.$$

Substituting this value of t in the expression for y we find, if  $R_1$  is the distance from the radium of the point at which the ion strikes the plate,

 $R_{1} = \frac{Z}{H}t + \frac{2V}{\omega};$ 

but  $2V/\omega = R$ , where R is the distance from the radium of the point of return of the ion when the upper metal plate is not charged, hence we have

$$R_{1}-R=\frac{Z}{H}t,$$
 
$$\frac{1}{2}\omega t=\frac{R_{1}-R}{R}\frac{V}{Z/H};$$

or

 $\tan \frac{1}{2}\omega t = -\frac{V}{Z/H}$ 

hence since

$$\tan \frac{R_1 - R}{R} \frac{V}{Z/H} = -\frac{V}{Z/H} \dots (1),$$

an equation by which we can determine the value of V/(Z/H) When V is known, e/m can be determined from the value of R.

When  $\mathbb{Z}/H$  is small compared with V an approximate solution of equation (1) is

$$V = (Z/H) \frac{\pi}{2} \frac{R}{R_1 - R}.$$

Becquerel did not use this method of determining V, but the electrostatic method previously described; the latter method is not however in many respects so convenient as the one just given.

As the result of his experiments Becquerel found for one set of rays given out by the radium

$$v = 1.6 \times 10^{10}, \qquad e/m = 10^{7},$$

thus the value of e/m is the same for these negatively charged ions from radium as for the ions in the cathode and Lenard rays, as well as for those produced by ultra-violet light or by incandescent metals. The velocity of the ions is much greater than any we have met with in the case of ions arising in other ways, amounting as it does to more than half the velocity of light; the ions chosen by Becquerel for this experiment were by no means the fastest given out by the radium. Becquerel detected the existence of others whose velocity was at least half as much again as the velocity of those he measured.

It may be convenient to summarise in a table the results of the measurements of e/m made by different observers, and with ions produced in different ways.

It will be seen from the table that taking the same method the values of e/m are practically the same whatever the source of the ions. We have seen too that they do not depend upon the gas or upon the nature of the electrodes; thus in every case in which negative electrification has been observed in gases at low pressures, the value of e/m is a constant quantity and is very large, approximately 1000 times larger than the largest value of the corresponding quantity in the electrolysis of liquid solutions. It is to be noted that these large values of e/m for gases only occur when the pressure of the gas is very low, when in fact there

is very little gas for the ion to get entangled with; when the pressure of the gas is high, the ion seems to act as a nucleus

Table of Values of e/m.

Source of Ions	Observer	Date	Method of Determination	Value of e/m
Cathode rays	J. J. Thomson	1897	Magnetic and electrostatic deflection	7·7×10 <sup>6</sup>
22	J. J. Thomson	1897	Magnetic deflection and heating effect	$1.17 \times 10^7$
2.2	Kaufmann	1897-8	Magnetic deflection and potential difference	$1.86 \times 10^7$
27	Simon	1899	Magnetic deflection and potential difference	$1.865\times10^{7}$
, ,,	Wiechert	1899	Magnetic deflection and velocity of ions	$1.01 \times 10^{7} - 1.55 \times 10^{7}$
Lenard rays	Lenard	1898	Magnetic and electrostatic deflection	$6.39 \times 10^6$
,,	Lenard	1898	Magnetic deflection and retardation in electric field	$6.8 \times 10^6$
Ultra-violet light	J. J. Thomson	1899	Retardation of discharge by magnetic field	$7.6 \times 10^6$
,,	Lenard	1900	Magnetic deflection and potential difference	1·15 × 10 <sup>7</sup>
Incandescent	J. J. Thomson	1899	Retardation of discharge by magnetic field	$8.7 \times 10^6$
Radium	Becquerel	1900	Magnetic and electrostatic deflection	10 <sup>7</sup> approximately

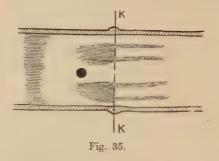
round which the molecules of the gas collect; the ion thus gets loaded up, and the ratio of e/m is very small compared with its value at lower pressures.

## 61. Value of e/m for the positive ions.

The number of determinations of the value of e/m for the ions which carry the positive charge is small compared with those made for the corresponding quantity for the negative ions. The first determination of the value of e/m for the positive ions was made by W. Wien\*. The positive ions he used were those which occur in what are known as 'Canal-strahlen.' If an electric discharge passes between an anode and a cathode perforated with

<sup>\*</sup> W. Wien, Wied. Ann. lxv. p. 440, 1898.

a number of holes, then behind the cathode, i.e. on the side of the cathode opposite to the anode, pencils of light are seen to



penetrate through the holes as in Fig. 35\*, producing phosphorescence when they strike the glass. These rays have been shown by Wien to consist of positively charged ions. He exposed a long pencil of these rays coming through a perforated iron cathode to both an electrostatic and a magnetic field, and measured the corresponding deflections; from these he deduced by the method described on page 93, the values of e/m and v, and found

$$v = 3.6 \times 10^7$$
 cm./sec., while  $e/m = 300$ .

The 'canal-strahlen' or positive rays are only deflected with great difficulty by the magnetic field, and it is necessary to use very strong fields; this increases the difficulty of the investigation; in Wien's experiments the strength of the field was 3250. It will be seen from this result that the velocity of the positive ions is very much smaller than that of any of the cathode rays hitherto measured, while the value of e/m is of an entirely different order, being only about 1/30000 of the value for the negative ion; moreover the value of e/m for the positive ions in the gas is of the same order of magnitude as the value of e/m in the ordinary electrolysis of solutions. Thus if m were the mass of the atom of iron, e the charge carried by an atom of hydrogen, e/m is about 200, or since iron is divalent the value of e/m for the iron in the electrolysis of solutions is about 400. We have not however sufficient data to enable us to determine whether the carriers of the positive electricity in the 'canal-strahlen' are the atoms or molecules of the metal of the cathode or of the gas in the tube.

<sup>\*</sup> Wehnelt, Wied. Ann. lxvii. p. 421, 1899.

The energy in the particles forming the positive rays or canalstrahlen is that which they would acquire by a fall through a potential difference of about 16000 volts. As we know the charge and the mass of the particles forming the positive rays, we can compare the energy in the particles due to this difference of potential with the mean energy possessed at any temperature by the molecules of a gas, the mass of the molecules being the same as that of the particles in the positive rays; doing so we find that even at the highest attainable temperature the energy of a molecule in the gas would be quite insignificant in comparison with that of a particle in the positive rays.

**62**. The writer has determined the value of e/m for the positive ions by the method described on page 106 for the determination of the value of e/m for the negative ions produced by the action of ultra-violet light. The positive ions were produced by raising, by means of an electric current, an iron wire to a red heat in an atmosphere of oxygen, the pressure being very low. The wire was parallel to a metal plate connected with an electrometer, the distance of the wire from the plate was 4 mm. If the wire was charged positively the plate and the electrometer received a positive charge, the current passing between the plate and the hot wire being easily measured by the electrometer; if now the space between the hot wire and the plate was placed in a very powerful magnetic field, the lines of force being parallel to the plate, the rate of leak from the wire to the plate was found to diminish if the potential difference between the wire and the plate did not exceed a certain value—just as in the corresponding case of the negative ions produced by ultra-violet light—but while in the latter case a comparatively feeble magnetic force is sufficient to diminish the current, it requires a very powerful magnetic force to produce the effect with the hot wire; thus for example in my experiments on the positive ions I used a magnetic field of strength 12400 c.g.s. units, while in the experiments on the negative ones a field of 100 was amply sufficient to produce very appreciable effects. In the case of the hot wire I found that using a magnetic field of strength 12400 the rate of leak was less when the magnetic field was on than when it was off, when the potential difference between the plates was less than 50 volts; when it exceeded this value the rate of leak was the same

whether the magnet was on or off. Thus when H = 12400 and  $X = 50 \times 10^{8}/4$  the critical distance is 4 cm. Hence by the results given on p. 106 we have

$$4 = \frac{2 \times 50 \times 10^8}{4 \times (12400)^2} \frac{m}{e},$$
$$\frac{e}{m} = 400.$$

or

This is about the value for e/m for the ion of iron in electrolysis: it does not however prove that the carriers of the positive electricity are the atoms of iron, for if m were the mass of a molecule of oxygen and e the charge on a hydrogen ion in the electrolysis of solutions e/m would be about 310, and the difficulties of the experiment are so great that we cannot say that this result differs from that actually found by more than the possible errors of the experiment.

We see however that for the positive ions e/m is of the same order as in ordinary electrolysis of solutions, while for negative ions it is of an entirely different order.

The effect of the strongest magnetic fields I have been able to use on the current when this is carried by positive ions is very much less marked than the effect of comparatively weak fields on the current when it is carried by negative ions. In the case of the positive ions the magnetic force, even in the most favourable circumstances, only diminishes the current, it does not entirely stop it: this points to the conclusion that the carriers of the positive charge are not all of one kind, but that some are much heavier than others; thus in the case of the leak of positive electricity from a hot platinum wire the study of the effect of the magnetic field on the current leads us to the conclusion that a part of the current is carried by molecules of oxygen and the rest by molecules of platinum, or perhaps by aggregates of several molecules. The proportion between the numbers of the different kinds of carriers seems to vary very largely with the temperature and state of the surface of the platinum.

## CHAPTER VI.

DETERMINATION OF THE CHARGE CARRIED BY THE NEGATIVE ION.

63. We have seen that the value of e/m for the negative ions in gases at a low pressure is about a thousand times the greatest value of the ratio of the same quantities for ordinary electrolytes. The question at once arises, is this due to a difference in the masses of the ions, or to a difference in their electrical charges, or to both these causes: to decide these points we must determine the value of m or e. The writer made in 1898\* and 1899+ determinations of the value of e for the ions produced in one case by Röntgen rays and in the other by ultra-violet light. The method was based on the discovery made by C. T. R. Wilson, (see Chap. VII.) that gaseous ions, whether positive or negative, act as nuclei for the condensation of clouds even in the absence of dust; and that if we have a mass of dust-free gas containing ions in a closed vessel, and cool the gas by a sudden expansion, then a cloud will be produced if the ratio of the volume of the gas after expansion to the volume before is greater than 1.25. An expansion of this amount is quite incapable of producing more than very slight condensation in the gas if it does not contain ions. The water condenses round the ions, and if these are not too numerous each ion becomes the nucleus of a drop of water. Thus by producing a sudden expansion in a gas containing ions we can get a little drop of water round each ion; these drops are visible, and we can measure the rate at which they fall. Sir George Stokes has shown that if v is the velocity with which a drop of water falls through a gas, a the radius of the

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 46, p. 528, 1898.

<sup>+</sup> J. J. Thomson, Phil. Mag. v. 48, p. 547, 1899.

<sup>‡</sup> C. T. R. Wilson, Phil. Trans., A, 1897, p. 265.

drop,  $\mu$  the coefficient of viscosity of the gas, and g the acceleration due to gravity, then

 $v = \frac{2}{9} \frac{ga^2}{\mu};$ 

thus if we measure v we can determine a, and hence the volume of each drop. If q is the mass of water deposited from each cubic centimetre of the gas, n the number of the drops, we have

$$q = n \frac{4}{3} \pi a^3.$$

To find q we may proceed as follows: the gas after being cooled by the very rapid expansion is supersaturated and moisture is deposited on the ions, during the condensation of the water heat is given out which warms the gas so that the temperature of the gas rises above the lowest temperature reached during the expansion before condensation has taken place. Let  $t_2$  be the lowest temperature reached during the expansion, t the temperature when the drops are fully formed, then if L is the latent heat of evaporation of water, C the specific heat of the gas at constant volume, M the mass of unit volume of the gas after expansion, we have

$$Lq = CM (t - t_2)....(1);$$

we neglect the heat required to raise the temperature of the water in the gas in comparison with that required to raise the temperature of the gas itself. We have further

$$q = \rho_1 - \rho,$$

where  $\rho_1$  is the density of the water vapour before condensation begins, and  $\rho$  the density at the temperature t. Substituting this value for q in equation (1), we get

$$\rho = \rho_1 - \frac{CM}{L} (t - t_2) \dots (2).$$

Since  $\rho$  is a known function of t this equation enables us to find t when  $t_2$  is known.

If x is the ratio of the final to the initial volume of the gas and T the temperature in degrees centigrade of the gas before expansion, then since the mass of 1 cubic centimetre of air at the temperature  $0^{\circ}$  C. and under a pressure of 760 millimetres of mercury is '00129 grm., we have

$$M = \frac{.00129}{x} \times \frac{273}{273 + T} \frac{P}{760} \,,$$

where P is the initial pressure of the gas expressed in millimetres of mercury.

Again, 
$$\rho_1 = \frac{\rho'}{x}$$
,

where  $\rho'$  is the density of water vapour at the temperature T before expansion; as the air was saturated with water vapour at this temperature  $\rho'$  can be obtained directly from the Tables of the vapour pressure of water vapour.

The cooling caused by the adiabatic expansion is determined by the equation

$$\log \frac{273 + T}{273 + t_2} = 41 \log x...(3).$$

For in such an expansion  $pv^{\gamma}$  is constant, where p is the pressure and v the volume and  $\gamma$  the ratio of the specific heat at constant pressure to that at constant volume: but  $pv = R\theta$ , where  $\theta$  is the absolute temperature and R a constant, hence we have during an adiabatic expansion

$$v^{\gamma-1}\theta = a \text{ constant};$$

hence if  $v_1\theta_1$ ,  $v_2\theta_2$  are the initial and final values of v and  $\theta$ , we have

$$v_1^{\gamma-1}\theta_1 = v_2^{\gamma-1}\theta_2,$$

$$\theta$$

or

$$\log \frac{\theta_{\scriptscriptstyle 1}}{\theta_{\scriptscriptstyle 2}} = (\gamma - 1) \log \frac{v_{\scriptscriptstyle 2}}{v_{\scriptscriptstyle 1}}.$$

Since  $\gamma = 1.41$  this is equivalent to equation (3). From (3) we determine  $t_2$ , and then since

$$C = .167, L = 606,$$

equation (2) becomes

$$\rho = \frac{\rho'}{x} - \frac{167}{606} \times \frac{00129}{x} \frac{273}{273 + T} \frac{P}{760} (t - t_2) \dots (4).$$

As an example of how this equation is applied let us take a case which occurred in one of the experiments. Here

$$T = 16^{\circ}$$
,  $P = 760$ ,  $x = 1.36$ .

To get  $t_2$  we have

$$\log \frac{273 + 16}{273 + t_2} = 41 \log 1.36 = \log 1.134,$$

hence

$$273 + t_2 = 254.8$$
, or  $t_2 = -18^{\circ}.2$ .

We find from the Tables that at 16°

$$\rho' = .0000135$$
,

hence equation (4) becomes

$$\rho = 99.3 \times 10^{-7} - 2.48 \times 10^{-7} (t + 18.2) \dots (5).$$

To solve this equation we keep substituting various values for t until we find one for which the corresponding value of  $\rho$  given by (5) is the same as the value of the vapour pressure of water at the temperature t. We find by this process of trial and error that the solution of equation (5) is t=1.2, and the corresponding value of  $\rho$  is  $51.5 \times 10^{-7}$ . Substituting this value for  $\rho$  we find  $q=47.7 \times 10^{-7}$  grms.

When we know q and a, n the number of drops is at once determined by the equation

$$n = q/\frac{4}{3}\pi a^3.$$

In this way we can determine the number of ions per cubic centimetre of gas. When we know the number of ions and also the velocity of the ions under unit electric force, we can very easily deduce the charge carried by an ion by measuring the current carried by these ions across each unit of area under an electric force E. For if n is the whole number of ions per c.c., positive as well as negative, U the mean of the velocities of the positive and negative ions under unit electric force, the current through unit area is equal to

## ne E U.

where e is the charge on the ion; the electric force E ought to be so small that the current is proportional to the electric force. When this is not the case the number of ions is diminished by the action of the electric field, and depends upon the magnitude of the electric force.

We can easily measure the current through the ionised gas and thus determine neEU, and as n, E, U are known we can deduce the value of e.

64. This method was first applied by the author to determine the charge on the ions produced by Röntgen rays. The method used for making the cloud and measuring the expansions is the same as that used by C. T. R. Wilson\*: the apparatus for this and the

<sup>\*</sup> C. T. R. Wilson, Proc. Camb. Phil. Soc. ix. p. 333, 1897.

electrical part of the experiment is represented in Fig. 36. The gas which is exposed to the rays is contained in the vessel A;

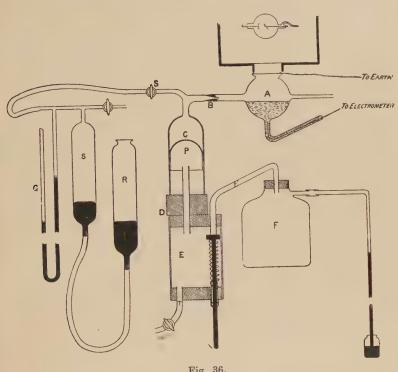


Fig. 36.

this vessel is connected by the tube B with the vertical tube C, the lower end of this tube is carefully ground so as to be in a plane perpendicular to the axis of the tube, it is fastened down to the india-rubber stopper D. Inside this tube there is an inverted thin-walled test tube P with the lip removed and the open end ground so as to be in a plane perpendicular to the axis of the tube. The test tube slides freely up and down the larger tube and acts as a piston. Its lower end is always below the surface of the water which fills the lower part of the outer tube; a tube passing through the india-rubber stopper puts the inside of the test tube in communication with the space E. This space is in connection by the tube H with a large vessel F in which the pressure is kept low by a water-pump. The end of the tube H is ground flat and is closed by an india-rubber stopper which presses

against it, the stopper is fixed to a rod, and by pulling this rod down smartly the pressure inside the test tube is lowered and the test tube falls rapidly until it strikes against the india-rubber stopper. The tube T, which can be closed by a stop-cock, admits air into E and allows us to force the test tube back into its place for another expansion. The tubes R and S are for the purposes of regulating the amount of expansion. To do this the mercury vessel R is raised or lowered when the test tube is in its lowest position until the gauge G indicates that the pressure in A is the desired amount below the atmospheric pressure. The stop-cock S is then closed and air is admitted into the interior of the piston by opening the stop-cock T. The piston then rises until the pressure in A differs from atmospheric pressure only by the amount required to support the weight of the piston; this pressure is only that due to a fraction of a millimetre of mercury.

If  $\Pi$  is the barometric pressure, then  $P_1$ , the pressure of the air before expansion, is given by the equation

$$P_1 = \Pi - \pi,$$

where  $\pi$  is the maximum vapour pressure of water at the temperature of the experiment. The pressure of the air  $P_2$  after the expansion is given by

$$P_2 = P_1 - p,$$

where p is the pressure due to the difference of level of the mercury in the two arms of the gauge G.

Thus if  $v_2$  is the final and  $v_1$  the initial volume of the gas

$$\frac{v_2}{v_1} = \frac{P_1}{P_2} = \frac{\Pi - \pi}{\Pi - \pi - p}.$$

The vessel in which the rate of fall of the fog and the conductivity of the gas are tested is at A. It is a glass tube 36 millimetres in diameter covered with an aluminium plate; to avoid the abnormal ionisation which occurs when Röntgen rays strike against a metal surface, the lower part of the aluminium plate is coated with wet blotting-paper, and the electric current passes from the blotting-paper to the horizontal surface of the water beneath. The induction coil and the focus bulb for the production of the Röntgen rays are placed in a large iron tank, in the bottom of which a hole is cut and closed by an aluminium

window. The vessel A is placed underneath this window and the bulb giving out the rays some distance above it, so that the beam of rays escaping from the tank is not very divergent. The intensity of the rays can be reduced to any required degree by inserting leaves of tinfoil or sheets of aluminium between the bulb and the vessel.

In these experiments it is necessary to work with very weak rays, so that the number of ions is comparatively small; when the number of ions is large some of them seem to escape being caught by the cloud produced by the expansion, for if a second expansion be produced (the ionising agent being cut off) a considerable cloud will be formed, and it may require several expansions before the gas is restored to the state in which it existed previous to the exposure to the ionising agent. The cause of these secondary clouds has not yet been definitely settled, but it is possible that they may be due, partly at any rate, to ions which have not been caught by the first cloud, and if this were so the number of ions deduced from the time of fall of the cloud would be too small; it is therefore advisable to work with such weak ionisation of the gas that the first cloud clears away all the ions.

To find the current passing through the gas, the tank and the aluminium plate on the top of the vessel A are connected with one pair of quadrants of the electrometer, the other pair of quadrants is connected with the water surface in the vessel A; this surface is charged up to a known potential by connecting it with one of the terminals of a battery, the other terminal of which is connected with the earth. After the surface has been charged it is disconnected from the battery and the insulation of the system tested by observing whether there is any leak when the Röntgen rays are shut off; the insulation having been found satisfactory, the rays are turned on and the charge begins to leak from the electrometer; by measuring the rate of leak the quantity of electricity which in one second passes through the gas exposed to the rays can be determined. For suppose that in a second the electrometer reading is altered by p scale divisions, and that one scale division of the electrometer corresponds to a potential difference V between the quadrants, and that C is the capacity of the system consisting of the electrometer, the water surface and the connecting wires, then the quantity of electricity which passes in one second through the gas exposed to the rays is pVC. If n is the total number of ions positive as well as negative per cubic centimetre of the gas,  $u_0$  the mean of the velocities of the positive and negative ions under a potential gradient of a volt per centimetre, E the potential gradient in volts per centimetre acting on the ionised gas, A the area of the water surface, the current through the gas is equal to  $Aneu_0E$ ; but as this current is equal to pVC, we have

$$pVC = Aneu_0E$$
,

an equation by means of which we can determine ne, and as from the experiments on clouds we know the value of n we can at once deduce the value of e. Proceeding in this way the author found in 1898 that for the ions produced by Röntgen rays passing through air, using electrostatic units,

$$e = 6.5 \times 10^{-10} \,\mathrm{gr}^{\frac{1}{2}} \,\mathrm{(cm.)^{\frac{3}{2}} \,(sec.)^{-1}}$$

A similar series of experiments on the ions produced by Röntgen rays passing through hydrogen gave for e the charge on the hydrogen ion the value

$$6.7 \times 10^{-10} \, (\mathrm{gr.})^{\frac{1}{3}} \, (\mathrm{cm.})^{\frac{3}{2}} \, (\mathrm{sec.})^{-1}$$

The difference between this and the value of the charge on the ion in air is much less than the error of experiment, so that the charges on the ions are the same in these gases. This was shortly afterwards confirmed by the experiments made by Townsend on the rates of diffusion of the ions; an account of these experiments has already been given on p. 26.

65. The author in 1901–2 repeated these experiments on the charges carried by the ions, making some modifications in the method. In the first place the ionisation was produced by the radiation from radium instead of by the Röntgen rays; this was done to get a more uniform rate of ionisation than is possible with Röntgen tubes, the irregularity of which gave a great deal of trouble in the earlier investigation. Secondly, the electrometer used in the new experiments was much more sensitive than the old one, the new electrometer was of the Dolezalek type and gave a deflection of 20000 scale divisions for a potential difference of one volt.

The measurements made by C. T. R. Wilson\* (see Chap. VII.)

<sup>\*</sup> C. T. R. Wilson, Phil. Trans. exciii. p. 289.

show that with expansions between 1.25 and 1.3 negative, and only negative, ions act as nuclei for cloudy condensation, while with expansions greater than 1.3 both negative and positive ions are brought down by the cloud. It was feared that when the expansions were sufficiently large to bring both sets of ions into play the more active negative ions might have a tendency to monopolise the aqueous vapour, and that therefore the whole of the positive ions might not be brought down with the cloud. This fear was found to be justified, for with the expansion apparatus used in the earlier experiments it was found that with expansions greater than 1.3 the number of particles in the cloud formed in the ionised gas was not, as it should have been if all the ions had been caught by the cloud, twice as great as when the expansion was less than this value. The apparatus was modified so as to make the rate of expansion very much more rapid than in the earlier experiments; with the new apparatus the number of particles in the cloud when the expansion was greater than 1:3 was twice as great as when the expansion was less than this value; this confirms the view that with this apparatus all the ions are caught by the cloud. The result of a number of determinations of e with the new apparatus, using different samples of radium and different intensities of radiation, was that

$$e = 3.4 \times 10^{-10} \, (\text{gr.})^{\frac{1}{3}} \, (\text{cm.})^{\frac{9}{3}} \, (\text{sec.})^{-1}$$

66. Having found the value of e, let us compare it with E the charge carried by the hydrogen ion in the electrolysis of solutions. If N is the number of molecules in a cubic centimetre of a gas at a pressure of 760 mm. of mercury and at 0° C., then we know as the result of experiments on the liberation of hydrogen in electrolysis (see p. 57) that

## $NE = 1.22 \times 10^{10}$ .

In treatises on the Kinetic Theory of Gases (for example, O. E. Meyer, Die kinetische Theorie der Gase) it is shown how by the aid of certain assumptions as to the nature and shape of the molecules it is possible to find N. The values got in this way vary considerably, the best determinations of N lying between  $2\cdot1\times10^{10}$  and  $10^{20}$ ; this would make E lie between  $6\cdot1\times10^{-10}$  and  $1\cdot29\times10^{-10}$ ; the value of e is well between these limits. Hence we conclude that the charge carried by any gaseous ion is equal

to the charge carried by the hydrogen ion in the electrolysis of solutions.

This conclusion is also confirmed by the experiments of Townsend already referred to. In these experiments the charges on the ions in air, hydrogen and carbonic acid gas were directly compared with E, and proved to be equal to it (see p. 58). Starting with this result we can by direct experiment on gases determine the value of E, and then by the aid of the equation

$$NE = 1.22 \times 10^{10}$$
.

the number of molecules in a cubic centimetre of the gas, and hence the mass of a molecule of the gas; proceeding in this way we avoid all those assumptions as to the shape and size of the molecules of the gas, and the nature of the action which occurs when two molecules come into collision, which have to be made when the same quantities are determined by means of the Kinetic Theory of Gases. The value we have found for E makes

$$N = 3.9 \times 10^{19}$$
.

The determinations of e described above have been made on ions produced by Röntgen or radium rays. The properties of the ions in gases are the same, however, whether the ions are produced by Röntgen, radium, Lenard, or cathode rays, or by the agency of ultra-violet light. Evidence in support of this is afforded by the fact that as we have seen the velocity of the ions in the electric field is the same in whichever of the above-mentioned ways they are produced. We shall see too (Chap. VII.) that they behave in exactly the same way with respect to their power of producing condensation of clouds. We have thus strong reasons for thinking that the charge on the ion does not depend upon the kind of radiation used to liberate the ion. I have made some direct experiments on this point, and have made measurements of the charge on the negative ions produced by the incidence of ultra-violet light on metals; the method used was the same as in the case of the ions produced by Röntgen rays, and the result was that within the limits of experimental error the charge on the negative ion produced by the action of ultra-violet light was the same as that on the ion produced by Röntgen rays\*.

The case of the ions produced by ultra-violet light is interesting, as it is the one in which both the values of e and of e/m

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 48, p. 547, 1899.

(when the pressure is low) have been measured when the ions are produced by the same kind of radiation in the two experiments.

- **68.** As e is the same as E the charge on the hydrogen ion, while e/m is about a thousand times E/M, where M is the mass of the atom of hydrogen, it follows that m is only about 1/1000 of M, so that the mass of the carrier of the negative charge is only 1/1000 of that of the atom of hydrogen.
- 69. Let us now sum up the results of the determinations of e and of e/m which have been made for the ions produced in gases by radiations of different kinds. We have seen that in all the cases in which e has been determined it has been found equal to E, the charge on a hydrogen ion in liquid electrolysis. The charge on the gaseous ion does not, like that on the ions in liquids, depend on the substance from which the ions are produced; thus in the case of the ions produced by Röntgen or analogous radiation, the charge on an ion produced from oxygen is the same as that on one produced from hydrogen, though in liquids the charge on an oxygen ion is twice that on a hydrogen one.

Again, at very low pressures, when the negative ion can escape getting entangled with the molecules of the gas by which it is surrounded, the mass as well as the charge of the negative ion is invariable and much smaller than the mass of the smallest portion of ordinary matter, i.e. that of an atom of hydrogen, recognised in the Kinetic Theory of Gases. We shall call each of these small negative ions a corpuscle, thus negative electrification when the pressure of the gas is low so that there is only a very small quantity of ordinary matter present, consists of an assemblage of corpuscles.

On the other hand the positive ions are as far as we know always associated with masses which are comparable with the masses of the ordinary atoms of the gas in which they occur.

We are at once led by this result to a view of the nature of electricity which in many respects closely resembles that of the old 'One Fluid Theory of Electricity.' The 'electric fluid' corresponds to an assemblage of corpuscles, negative electrification consisting of a collection of these corpuscles: the transference of electrification from place to place being a movement of corpuscles

from the place where there is a gain of positive electrification to the place where there is a gain of negative. Thus a positively electrified body is one which has been deprived of some corpuscles. These corpuscles may either remain free or get attached to molecules of matter with which they come in contact; thus positive electrification is always associated with ordinary matter, while negative electrification may or may not be, according as the corpuscles are or are not attached to molecules of ordinary matter. Thus in gas at very low pressures the corpuscles are free, but in gases at higher pressures they get attached to the molecules of the gas so that there is not much difference between the effective masses of the positive and negative ions; that this is the case is indicated by the results of the experiments we have described on the velocities of the positive and negative ions in the electric field, for though the negative ion moves faster than the positive, the difference is not great. We shall return to the development of this corpuscular theory of electricity in a later chapter.

## CHAPTER VII.

ON SOME PHYSICAL PROPERTIES OF GASEOUS IONS.

70. ONE of the most striking effects produced by ions is the influence they exert on the condensation of clouds. One instance of this is the discovery by R. von Helmholtz\* of the effect of an electric discharge on a high pressure steam jet. steam rushes out from a jet placed near a pointed electrode connected with an electric machine or an induction coil, a remarkable change in the appearance of the jet takes place when electricity is escaping from the electrode. This can conveniently be shown by throwing the shadow of the jet on a screen; when there is no escape of electricity the jet is nearly transparent and the shadow is very slight; as soon however as electricity begins to escape, the opacity of the jet increases to a remarkable extent, the shadow becomes quite dark and distinct, and colours arising from the diffraction of the light by the small drops of water make their appearance, the jet sometimes presenting a very beautiful appearance. For an account of the ways of arranging the experiments so as to observe these colours to the best advantage and of a method by which the size of the drops of water can be deduced from the colour phenomena, we must refer to a paper by Barus<sup>†</sup>. This effect evidently shows that the electrification makes the steam condense into water drops.

In a later paper by R. von Helmholtz and Richarz<sup>+</sup>, published after the death of the former, the authors show that a steam jet is affected by making or breaking the current through the primary

<sup>\*</sup> R. v. Helmholtz, Wied. Ann. xxxii. p. 1, 1887; see also Bidwell, Phil. Mag. v. 29, p. 158, 1890.

<sup>+</sup> Barus, American Journal of Meteorology, ix. p. 488, 1893.

<sup>‡</sup> R. v. Helmholtz and Richarz, Wied. Ann. xl. p. 161, 1890.

of an induction coil, even when the terminals of the secondary placed in the neighbourhood of the jet are separated by much more than the sparking distance, and that the effects persist even when the terminals are wrapped in moist filter-paper so as to catch any metallic particles that might be given off from them.

R. von Helmholtz and Richarz (loc. cit.) showed that the steam jet was affected by gases from the neighbourhood of flames whether these were luminous or not; the very cool flames of burning ether and alcohol are exceptions to this statement.

A platinum wire raised to a dull red heat affected the jet when electrified, and if raised to a bright yellow heat affected the jet even when unelectrified, except when the wire was surrounded by hydrogen, in which case the unelectrified wire had no effect. Coal gas passed through platinum gauze raised to a dull red heat also influenced the jet.

The jet is also affected by the presence in its neighbourhood of certain substances such as sulphuric acid, also by gases which are dissociating or undergoing chemical changes in the air such as N<sub>2</sub>O<sub>4</sub> or NO<sub>2</sub>, it is not affected by ozone or hydrogen peroxide. If however ozone is destroyed by bubbling through such substances as solutions of potassium iodide or potassium permanganate, the gas which emerges has the power of affecting the jet; this gas has also the power of forming clouds when it comes into contact with moist air, as was first shown by Meissner\*; experiments on this point have also been made by R. von Helmholtz and Richarz and by J. S. Townsend +. The action in this case and in other cases of the effect of chemicals is, as we shall see, probably due to the formation of some substance which dissolves in the drops of water and lowers their vapour pressure; thus the drops in this case are not formed of pure water, but of more or less dilute solutions.

Moist air drawn over phosphorus, sodium or potassium also affects the jet.

Lenard and Wolff also showed that the incidence of ultra-

<sup>\*</sup> Meissner, Jahresber. f. Chemie, 1863, p. 126.

<sup>†</sup> J. S. Townsend, Proc. Camb. Phil. Soc. x. p. 52, 1898. ‡ Lenard and Wolff, Wied. Ann. xxxvii. p. 443, 1899.

violet light on a zinc plate or on some fluorescent solutions in the neighbourhood of a steam jet produced condensation in the jet; a similar effect was produced by ultra-violet light passing through quartz. Richarz\* showed that the incidence of Röntgen rays produced condensation in the jet. There was for some time considerable difference of opinion as to the cause of this behaviour of the steam jet; the earliest researches on this subject came at a time when the experiments of Aitken<sup>†</sup>, of Coulier<sup>‡</sup> and of Kiessling had drawn attention to the great effect produced by dust on cloudy condensation. These physicists had shown that the clouds produced by the lowering of temperature resulting from a small adiabatic expansion of the damp dusty air of an ordinary room entirely disappeared if the dust were filtered out of the air: the drops in the cloud were shown to collect round the particles of dust, the water drops were thus able to start with a finite radius-that of the dust particle-and so had not to pass through the stage when their radius was of molecular dimensions, when, as Lord Kelvin has shown, the effect of surface tension would lead to such intense evaporation as soon to cause the disappearance of the drops.

The discovery of the effect of dust on the condensation of water vapour produced a tendency to ascribe the formation of clouds in all cases to dust and to dust alone; in fact, to use the indication of the steam jet as a measure of the dustiness of the air; thus, for example, Lenard and Wolff ascribed the effect which they found was produced by the incidence of ultra-violet light on metals to metallic dust given off by the metal under the influence of the light. On the other hand, R. von Helmholtz, and later Richarz, strongly maintained the view that many of the effects they observed were not due to dust, but to ions, and they gave strong arguments and made some striking experiments in support of this view; as however this evidence is somewhat indirect, and as the truth of their view has been indisputably proved by the direct experiments recently made by

<sup>\*</sup> Richarz, Wied. Ann. lix. p. 592, 1896.

<sup>†</sup> Aitken, Nature, xxiii. pp. 195, 384, 1880. Trans. Roy. Soc. Edin. xxxiii. p. 337, 1881.

<sup>&</sup>lt;sup>+</sup> Coulier, Journal de Pharm. et de Chemie, xxii, p. 165, 1875.

<sup>§</sup> Kiessling, Naturw. Verein Hamburg-Altona, viii. 1, 1884.

- C. T. R. Wilson\*, we shall proceed at once to a description of his researches.
- 71. The method used by Wilson was to suddenly cool the moist gas by an adiabatic expansion, so that the gas which was saturated with water vapour before cooling became supersaturated afterwards. One of the arrangements used by Wilson to produce

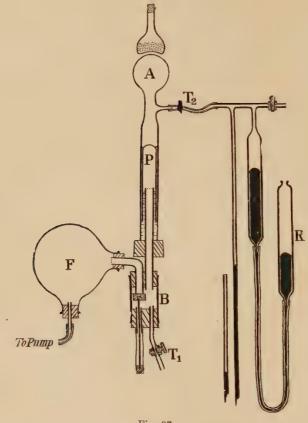


Fig. 37.

the expansion is shown in Fig. 37: the way in which the apparatus works has already been explained (see p. 125). It is very important in these experiments that the expansions which produce the cloud should be as rapid as possible, for with slow expansions

<sup>\*</sup> C. T. R. Wilson, Phil. Trans. 189, p. 265, 1897.

as soon as the supersaturation is sufficient for the first drops to be formed, if these have time to grow before the expansion is completed, they will rob the air of its moisture, and the supersaturation will not rise much above the value required for the formation of the first drops. To ensure this rapid expansion, the piston P, Fig. 37, should be light and able to move freely up and down, and the arrangement by which the difference of pressure between the inside and outside of the cylinder is produced should work very rapidly.

72. Using an arrangement of this nature, Wilson found that when dusty air filled the expansion chamber a very slight expansion was sufficient to produce a dense fog; if this was allowed to settle and the process repeated, the air by degrees got deprived of the dust which was carried down by the fog; when the air became dust-free no fogs were produced by small expansions. If we take as the measure of the expansion the ratio of the final to the initial volume of the gas, no cloud was produced in the dustfree air until the expansion was equal to 1.25. When the expansion was between 1.25 and 1.38, a few drops made their appearance; these drops were very much fewer in hydrogen than in air. On increasing the expansion beyond 1:38 a much denser cloud was produced in the dust-free gas, and the density of the cloud now increased very rapidly with the expansion. Thus we see that even when there is no dust, cloudy condensation can be produced by sudden expansions if these exceed a certain limit. This limit appears to be independent of the nature of the gas, as is shown by the following table, which gives the ratio of the

	Rain-like condensation		Cloud-like condensation	
Gas	Final/initial volume	Super- saturation	Final/initial volume	Super- saturation
Air	1.252	4.2	1.375	7.9
Oxygen	1.257	4.3	1.375	7.9
Nitrogen	1.262	4.4	1.375	7.9
Hydrogen			1.375	7.9
Carbonic acid	1.365	4.2	1.53	7.3
Chlorine	1.30	3.4	1.44	5.9

volumes required to produce the first or rain-like stage of condensation and the supersaturation, i.e. the ratio of the pressure of the aqueous vapour actually present when the condensation begins to the saturation vapour pressure at that temperature: the third and fourth columns give the corresponding quantities for the second stage of the condensation, *i.e.* when the expansion produces a dense cloud.

The rain-like condensation is absent in hydrogen.

- 73. The description given above relates to the behaviour of gas in the normal state; on exposing the gas to Röntgen rays, Wilson found that as in the normal gas, there were no drops until the expansion was equal to 1.25; on passing this limit however the density of the cloud was very greatly increased by the rays, and if these were strong the few drops which were all that were formed when the rays were absent were replaced by a dense and almost opaque cloud. The strength of the rays does not affect the expansion required to produce the cloud; no matter how strong the rays may be there is no cloud produced unless the expansion exceeds 1.25: the strength of the rays increases the number of drops in the cloud, but does not affect the stage at which the cloud begins. The effect of the rays in producing a cloud lasts some few seconds after the rays have been cut off. Wilson\* has shown that the radiation from uranium and other radio-active substances produces the same effect as Röntgen rays, as does also ultra-violet light when incident upon such a metal as zine: the effects produced by ultra-violet light are however somewhat complicated and we shall have to return to them again.
- 74. That the effect produced by Röntgen and uranium rays is due to the production of charged ions produced in the gas can be shown directly by the following experiment. If the ions produced by the Röntgen rays act as nuclei for the water drops, then since these ions can be withdrawn from the gas by applying to it a strong electric field, it follows that a cloud ought not to be formed by the rays when the air which is expanded is exposed to a strong electric field while the rays are passing through it. This was found to be the case, and the experiment is a very striking one. Two parallel plates were placed in the vessel containing the dust-free air: these plates were about 5 cm. apart, and were large enough to include the greater part of the air between them †. The

<sup>\*</sup> C. T. R. Wilson, Phil. Trans. 192, p. 403, 1899.

<sup>+</sup> J. J. Thomson, Phil. Mag. v. 46, p. 528, 1898.

plates could be connected with the terminals of a battery of small storage cells giving a potential difference of about 400 volts. Röntgen rays passed through the gas between the plates; the gas had previously been freed from dust. When the plates were disconnected from the battery a suitable expansion produced a dense cloud; when however the plates were connected with the battery only a very light cloud was produced by the expansion, and this cloud was almost as dense when the Röntgen rays did not pass through the air as when they did.

- 75. When a dense cloud has been produced by Röntgen rays by an expansion between 1.25 and 1.38, or by an expansion without Röntgen rays greater than 1.38, then for some little time after drops can be produced by expansions less than 1.25, and these are not eliminated by the action of an electric field. A dense fog apparently leaves behind it little drops of water, which, though too minute to be visible, act in the same way as particles of dust, producing cloudy condensation with very slight expansions. Wilson\* has also shown that when electricity is discharged from a pointed electrode in the expansion chamber, cloudy condensation is, as in the case of exposure to Röntgen rays, much increased for expansions between 1.25 and 1.38. When the discharge was stopped before the expansion took place, it was found that fogs could be produced for 1 or 2 minutes after the cessation of the discharge; the expansion required to produce the fog diminished as the interval after the cessation of the discharge increased, showing that some of the nuclei produced had grown during this interval. This effect is probably due to the formation of some chemical compound during the discharge, perhaps nitric acid, which by dissolving in the drops lowers their vapour pressure.
- 76. Wilson (loc. cit.) showed that the passage of ultra-violet light through a gas (as distinct from the effects produced when it is incident on a metallic surface) produces very interesting effects on the condensation of clouds. If the intensity of the light is small, then no clouds are produced unless the expansion equals that (1.25) required to produce clouds in gases exposed to Röntgen rays. If however the ultra-violet light is very intense, clouds are produced in air or in pure oxygen, but not in hydrogen, by very

<sup>\*</sup> C. T. R. Wilson, Phil. Trans. 192, p. 403, 1899.

much smaller expansions, and the expansion required decreases as the time of exposure to the light increases; thus the nuclei producing the clouds grow under the influence of the light. If the light is exceedingly strong, clouds are produced in air or oxygen without any expansion at all; these clouds are exceedingly fine and may last for hours after the light is cut off. Wilson was even able to produce these clouds in air standing over a 17% solution of caustic potash, and which therefore was not saturated with water vapour; in this case the drops lasted for three hours after the light was cut off, so that there could be very little evaporation from the drops; this, as Wilson points out, shows that the drops cannot be pure water. These clouds are probably analogous to those observed many years ago by Tyndall\*, when ultra-violet light passes through air containing the vapours of certain substances of which amyl-nitrite was the one which gave the most striking effects. The effects can be explained by the formation under the influence of the ultra-violet light of some substance— Wilson suggests that in his experiments it was H<sub>2</sub>O<sub>2</sub>—which by dissolving in the drops as they form lowers the equilibrium vapour pressure, and thus enables the drops to grow under circumstances which would make drops of pure water evaporate. This explanation is supported by the fact that ultra-violet light does not produce these clouds in water vapour by itself or in hydrogen: and also by the fact that, unlike the clouds due to Röntgen rays, these clouds formed by ultra-violet light do not diminish in density when a strong electric field is applied to the gas, showing that the nuclei are either not charged or that if they are charged they are so loaded with foreign molecules that they do not move perceptibly in the electric field.

77. Buisson†, who examined this question with great care, could not detect any conductivity in the air through which the ultra-violet light passed. Lenard‡ has however shown recently that a certain kind of ultra-violet light which is absorbed so quickly by the air as to be extinguished within a space of a few centimetres when the air is at atmospheric pressure, does produce electrical conductivity

<sup>\*</sup> J. Tyndall, Phil. Trans. 160, p. 333, 1870.

<sup>†</sup> Buisson quoted by Perrin, Thèses présentées à la Faculté des Sciences de Paris. 1897, p. 31.

<sup>‡</sup> Lenard, Drude's Annalen, i. p. 486; iii. p. 298, 1900.

in the gas through which it passes, and that a charged conductor placed in the neighbourhood of air traversed by these rays loses its charge, and does so much more rapidly when the charge is positive than when it is negative. Lenard determined the velocity of the negative ions by a method analogous to that described on page 38 and found for this velocity through air at atmospheric pressure 3.13 cm./sec. under a potential gradient of a volt per cm.: this is about twice the velocity of the ions produced by Röntgen rays; on the other hand the velocity of the positive ions under the same potential gradient was not more than '0015 cm./sec., which is only about one thousandth part of the velocity of the positive ion produced by Röntgen rays. The greater mobility of the negative ions explains why the leak from a positively charged body in the neighbourhood of the ionised gas is so much more rapid than that from a negatively charged one. We shall return to this point in the chapter on the effect of ultra-violet light on gases.

78. The results obtained by Wilson and Lenard seem to point to the conclusion that when gas is exposed to the action of ordinary ultra-violet light, we have some chemical action taking place which results in the formation of a product which by dissolving in water lowers the vapour pressure over the drops and thus facilitates their formation. When these drops are exposed to the influence of ultra-violet light of the kind investigated by Lenard, they lose, as so many other bodies do when illuminated by light of this kind, negative electricity, and it is the negative ions liberated in this way which produce the electrical conductivity investigated by Lenard. The difference between the action of ultra-violet light and Röntgen rays is that the former when very intense can produce clouds with little or no expansion, while the latter cannot; this on the theory given above is due to ultraviolet light being more efficient than Röntgen rays in promoting chemical action; there are many examples of this, e.g. the combination of hydrogen and chlorine.

The influence of minute traces of soluble substances in promoting the formation of clouds has been shown in a very straightforward way in some experiments made by H. A. Wilson\*. The writer† has shown how drops, even if their existence is very

<sup>\*</sup> H. A. Wilson, Phil. Mag. v. 45, p. 454, 1898.

<sup>†</sup> J. J. Thomson, Phil. Mag. v. 36, p. 313, 1893; B. A. Report, 1894.

transient, would facilitate the progress of chemical combination between the gases surrounding them, and how this action would afford an explanation of the remarkable fact investigated by Baker\* and Pringsheim+, that the occurrence of some of the best known cases of chemical combination between gases depends upon the presence of moisture and does not take place in gases dried with extreme care.

79. Nuclei from metals. C. T. R. Wilson; has shown that certain metals produce nuclei which cause cloudy condensation when the expansion exceeds 1.25, although the effects are much more marked when the expansion is increased to 1.30. The amount of this effect depends greatly upon the kind of metal used: amalgamated zinc gives comparatively dense clouds, polished zinc and lead also show the effect well; on the other hand polished copper and tin produce no appreciable effect. The order of the metals in respect to their power of producing nuclei for cloudy condensation is the same as their order in respect to their power of affecting a photographic plate placed at a small distance from their surface, a subject which has been studied by Russell§ and Colson. The effect produced by the presence of a metal on clouds in hydrogen is very slight.

Although the expansion required to produce cloudy condensation when metals are present is the same as when charged ions are produced by Röntgen rays, the metal effect differs from the Röntgen ray effect inasmuch as it is not diminished by the application of an intense electric field. It is possible however that in still air the ionised gas is confined to a layer close to the surface of the metal, and that the rush of gas caused by the sudden expansion detaches the layer and scatters the ions throughout the volume of the gas. If this be the case, then, since the ions are only free during the short time the expansion is taking place, they will not be appreciably affected by the electric field, which cannot in the short time at its disposal sweep the ions from the gas. The existence of such a layer of ionised gas next the metal is

<sup>\*</sup> Baker, Phil. Trans. 179, p. 571, 1888.

<sup>†</sup> Pringsheim, Wied. Ann. xxxii. p. 384, 1887.

<sup>‡</sup> C. T. R. Wilson, Phil. Trans. 192, p. 403, 1899.

<sup>§</sup> Russell, Proc. Roy. Soc. lxi. p. 424, 1897; lxiii. p. 102, 1898.

<sup>||</sup> Colson, Comptes Rendus, 123, p. 49, 1896.

rendered very probable by the effects which are known to accompany the splashing of drops of water, mercury and many other liquids. Thus Lenard\* showed that when drops of water splashed against a metal plate, the drops of water became positively electrified while there was negative electrification in the surrounding air. Air shaken up in a bottle containing mercury becomes negatively electrified. Lord Kelvin + has shown that when air is bubbled through water it comes off charged with negative electricity. I have recently found that if the air is made to bubble with great vigour through water, then when it leaves the water it contains positive as well as negative ions, though the latter are the more numerous; air treated in this way was found to discharge a body with a negative charge, though not so rapidly as one with a positive one. As another illustration of electrification produced by an agitation at the surface of water we may mention that Holmgren; has shown that when two wet cloths are brought together and then pulled suddenly apart electrification is produced, the positive electrification being on the cloth, the negative in the air. He also found that when the area of a water surface was changing rapidly, as for example when ripples were travelling over the surface, electrification was produced, the positive electricity being on the water and the negative in the air. The writer found \$\ that when the liquids were surrounded by pure hydrogen instead of air, the electrification produced by splashing was exceedingly small: Wilson, as has already been stated, found that the effect produced by metals on cloudy condensation was exceedingly small in hydrogen. These facts are sufficient to show that a disturbance at the surface of a large number of substances is accompanied by the spread of ions through the adjoining gas: the most natural explanation of this fact is that there is on the surface of these bodies a thin layer of ionised gas which can be detached by mechanical agitation. It is important to notice that if this layer of ionised gas were very close to the surface of the metal, the ions in it would not be dispersed into the surrounding gas even though the metal were charged up so as to produce an

<sup>\*</sup> Lenard, Wied. Ann. xlvi. p. 584, 1892.

<sup>+</sup> Lord Kelvin, Proc. Roy. Soc. lvii. p. 335, 1894.

<sup>‡</sup> Holmgren, Sur le Développement de l'électricité au contact de l'air et de l'eau. Société physiographique de Lond, 1894.

<sup>§</sup> J. J. Thomson, Phil. Mag. v. 37, p. 341, 1894.

electric field of very considerable strength. For suppose we have a charge e at a point P at a distance r from a plane conducting surface, then there will, in consequence of the electricity of opposite sign induced on the plane, be a pull on the charge at P towards the plane equal to  $e^2/4r^2$ ; if there is an external field of strength F tending to make the charged body move away from the plane, this will not be able to overcome the attraction towards the plane unless Fe is greater than  $e^2/4r^2$ , or F greater than  $e/4r^2$ . Let us suppose e is equal to the charge on an ion,  $3.4 \times 10^{-10}$  in electrostatic units, and that the strength of the electric field is 100 volts per centimetre which on the electrostatic system is equal to \(\frac{1}{3}\), then we see that the force on the ion in this strong field will be towards the plate, i.e. the ion will not be driven into the surrounding gas if r is less than  $1.6 \times 10^{-5}$ ; we see from this example that it must be exceedingly difficult to detach very thin layers of ionised gases by electrical means.

The few nuclei that produce rain-like condensation with expansions between 1.25 and 1.38 in gases not exposed to any external ionising agent may possibly I think come from a layer of gas torn off the water in the vessel by the disturbance caused by the expansion. These nuclei, as Wilson has shown, are not removed by an electric field, and yet they produce clouds with exactly the same expansions as is required for the charged ions produced by Röntgen rays. We have seen (see Chap. I.) that even in gases in the normal state there is a small amount of conductivity, indicating the presence of a few free ions, and these alone would cause the formation of a few drops, but if these were the nuclei mainly responsible for the rain-like condensation they ought to be removed by the electric field; indeed it seems not impossible that some of the nuclei which produce the electrical conductivity in normal air may have diffused from the layers of ionised gas at the surface of liquids or solids in contact with the gas. If, as Elster and Geitel hold, the gradual increase in the rate of escape of the electricity which occurs after fresh gas is brought into a closed vessel is not due to the settling down of dust from the gas, then this phenomenon is an additional argument in favour of the view that layers of ionised gas next the surface of solids or liquids exert a considerable influence on the condensation of clouds by expansion. The effect could be easily explained as due to the slow

diffusion of ionised gas from the walls of the vessel in which the gas is contained.

Comparative efficiency of positive and negative ions in producing condensation of clouds.

The writer\* in 1893 made an experiment with a steam jet which showed that negative electrification had a decidedly greater effect in promoting condensation than positive. The following arrangement was used. A vertical glass tube dipped into the steam chamber, and to the top of this tube was fused a horizontal cross piece, the steam issued from nozzles at the ends of the cross piece; into these nozzles pointed platinum wires were fused, and these wires were connected with the terminals of a small induction coil. When the coil was in action there was great condensation in the two jets, but the jet at the nozzle connected with the negative terminal of the coil was always denser than that connected with the positive; this was not due to any want of symmetry in the tubes or differences in the nozzles, for on reversing the coil the denser cloud passed from one nozzle to the other. No sparks passed between the platinum electrodes, the strength of the coil being only sufficient to give a non-luminous discharge from their points.

Later in 1898+ I observed indications of a similar effect when clouds were produced by expansion, but the subject was first systematically investigated by C. T. R. Wilson; in 1899. Wilson investigated the amount of expansion required to make positive and negative ions act as nuclei for the condensation of water drops; he used several methods, the arrangement of the apparatus in one of these is shown in Fig. 38. The vessel in which the clouds were observed was nearly spherical and about 5.8 cm. in diameter. It was divided into two equal chambers by a brass partition (about 1 mm. thick) in the equatorial plane; the vessel was cut in two and the edges of the two halves ground smooth, to allow them to be easily cemented against the face of the partition. The latter was circular and had a narrow strip of brass soldered to each face extending all round the circumference except for a

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 36, p. 313, 1893.

<sup>†</sup> J. J. Thomson, Phil. Mag. v. 46, p. 528, 1898.

<sup>‡</sup> C. T. R. Wilson, Phil. Trans. 193, p. 289, 1899.

gap at the top. When the halves of the glass vessel were cemented against these strips, a slit was left at the gap about 4.5 cms. long

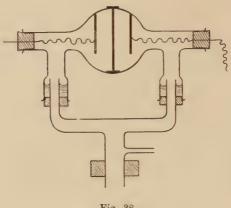


Fig. 38

and 2.5 mm, wide on each side of the partition. This slit was covered with a thin piece of aluminium cemented to the outer surface of the glass and to the edge of the brass partition. A thin layer of air in contact with each surface of the partition could thus be exposed to Röntgen rays from a source vertically over the dividing plate. Each half of the apparatus contained a second brass plate parallel to the central plate and 1.8 cm. from There was room between the sides of these plates and the walls of the vessel for the air to escape when the expansion was made. To keep the beam of Röntgen rays parallel to the surface of the partition a lead screen with a slit 4 mm. wide was placed about 2 cm. above the aluminium window of the glass vessel: this screen was moved until when both plates were kept at the same potential exactly equal fogs were obtained on the two sides. The metal plates were covered with wet filter-paper to get rid of any ions due to the metal. Suppose now that the middle plate is earthed while the left-hand plate is at a lower and the right-hand plate at a higher potential. Then it is evident since the ionisation is confined to a layer close to the middle plate that under these circumstances the left half of the vessel will contain positive ions and the right half negative ones. Wilson found that with an expansion of 1.28 there was a dense fog in the half containing the negative ions, and only a few drops in the half containing the positive ones, and that this excess of condensation in the negative half continued until the expansion was equal to 1.31, when little or no difference was to be seen in the clouds in the two halves. Care was taken that the potential of the positive plate should exceed that of the middle one by the same amount as this exceeded the potential of the negative plate.

The difference between the effects produced by positive and negative ions is shown in the following table, where the time of fall of the drops is used to measure the number of nuclei which produce condensation; if this number is small, then the water drops formed round them will be large and will therefore fall rapidly, while if the number of nuclei be large, since there is only the same quantity of water to be distributed among them,

TIME TAKEN BY FOGS TO FALL, IN SECONDS.

Expansion	Left side	Right side	Ratio of times negative/positive
1.28	positive 5 negative 15	negative 16 positive 3	$\frac{3 \cdot 2}{5 \cdot 0}$ 4·1
1:30	negative 15 positive 5 negative 10 positive 2	positive 2 negative 15 positive 2 negative 10	7·5 3·0 5·0 5·0 5·0
1:31	positive 7 negative 14	negative 12 positive 7	$\frac{1.7}{2.0}$ 1.8
1.32	negative 8 positive 8 negative 14 positive 12	positive 5 negative 10 positive 8 negative 17	$ \begin{vmatrix} 1.6 \\ 1.2 \\ 1.7 \\ 1.4 \end{vmatrix} 1.5 $
1.33	negative 12 positive 12	positive 10 negative 13	$\begin{bmatrix} 1 \cdot 2 \\ 1 \cdot 1 \end{bmatrix} 1 \cdot 15$
1.35	negative 10 positive 10	positive 10 negative 10	1·0 1·0} 1·0

the drops will be small and will fall slowly. In the experiments referred to in the table there was a potential difference equal

to that due to two Leclanché cells between the middle plate and either of the outer ones. The words positive and negative in the table indicate that the positive or negative ions respectively were in excess in the region referred to.

The difference in the rates of fall of the drops with the same expansions is due to irregularities in the action of the bulb used to produce the Röntgen rays. The negative ions begin to act as nuclei for foggy condensation when the expansion is about 1.25, corresponding to about a fourfold supersaturation, while we see from the table that the positive ions do not begin to act as nuclei until the expansion is equal to 1.31, corresponding to about a sixfold supersaturation. Wilson has shown that all the negative ions are caught when the expansion is equal to 1.28, but that it is not until the expansion reaches 1.35 that all the positive ions are caught. This is not due to the negative ions having a larger electrical charge than the positive; to show this, take an expansion vessel such as that shown in Fig. 36 and ionise the gas in it by Röntgen rays; first produce a fog with an expansion of 1:28 (which only brings down the negative ions), and determine the number of ions from the time of fall in the way explained on page 124; then with the same intensity of radiation produce a cloud by an expansion of 1:35, which brings down both the positive and negative ions, and again calculate the number of ions; we shall find it twice as great as in the first case, thus showing that the numbers of positive and negative ions are equal. As the gas as a whole has no charge, the total charge on the positive ions must be equal to that on the negative, hence as there are as many positive ions as negative, the charge on a positive ion must be the same as that on a negative one. We shall return to the origin of the greater efficiency of the negative than of the positive ions when we discuss the theory of the action of ions in promoting condensation. In the meantime we may point out that this difference between the ions may have very important bearings on the question of atmospheric electricity, for if the ions were to differ in their power of condensing water around them, then we might get a cloud formed round one set of ions and not round the other. The ions in the cloud would fall under gravity, and thus we might have separation of the positive and the negative ions and the production of an electric field, the work

required for the production of the field being done by gravity\*. An action of this kind would tend to make the charge in the air positive, as more negative ions than positive would be carried down by water drops: for a further consideration of this effect we may refer the reader to the papers by Elster and Geitel† on the ionic theory of atmospheric electricity.

Theory of the effect of ions on Condensation. The effect of electrification on the evaporation of drops of water was investigated by the writer in Applications of Dynamics to Physics and Chemistry, p. 165. The general tendency of this effect can easily be seen from elementary principles: for if we have a drop of water of radius a, carrying a charge e of electricity, its potential energy is equal to  $\frac{1}{2}e^2/Ka$ , where K is the specific inductive capacity of the dielectric surrounding the drop. Now as the drop evaporates the electricity remains behind, so that e does not change while a diminishes, hence the potential energy due to the electrification of the drop increases as the drop evaporates; thus to make the drop evaporate when charged more work has to be available than when it is uncharged, so that electrification will diminish the tendency of the drop to evaporate, and the drop will be in equilibrium when the vapour pressure of the water vapour around it would not be sufficient to prevent the evaporation of an uncharged drop. The surface tension of the water will, as was shown by Lord Kelvin, produce the opposite effect; for the potential energy due to the surface tension is equal to  $4\pi a^2 T$ , where T is the surface tension; thus as the drop evaporates the energy due to surface tension diminishes, so that the work required to vaporise a given quantity of water is less than if surface tension were absent, or, what is the same thing, as if the surface were flat. Thus a curved drop will evaporate when a flat one would be in equilibrium.

It is shown in Applications of Dynamics to Physics and Chemistry, p. 165, that when  $\delta p$ , the change in the vapour pressure due to the electrification and surface tension, is only a small fraction of the original vapour pressure p,

$$\frac{\delta p}{p} = \frac{1}{R\theta} \left\{ \frac{2T}{a} - \frac{e^2}{8\pi K a^4} \right\} \frac{1}{\sigma - \rho};$$

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 46, p. 528, 1898.

<sup>+</sup> Elster and Geitel, Physikalische Zeitschrift, i. p. 245, 1900.

 $\sigma$  is the density of water,  $\rho$  that of the vapour,  $\theta$  the absolute temperature, R the constant which occurs in the equation for a 'perfect' gas,  $p=R\theta\rho$ ; in the investigation this equation is assumed to hold for the water vapour. When the change in the pressure is not a small fraction of the equilibrium vapour pressure for an infinitely large drop, then the investigation already alluded to shows that the preceding equation has to be replaced by

$$R\theta\,\log_e\frac{p}{P} + \frac{R\theta\left(\rho'-\rho\right)}{\sigma} = \left(\frac{2T}{a} - \frac{e^2}{8\pi Ka^4}\right)\frac{1}{\sigma}\,,$$

where p and  $\rho$  are the equilibrium vapour pressure and density for a drop of radius a, P and  $\rho'$  the corresponding quantities for a drop of infinite radius. Since  $\rho' - \rho$  is small compared with  $\sigma$ , this equation becomes approximately

$$R\theta \log_e \frac{p}{P} = \left(\frac{2T}{a} - \frac{e^2}{8\pi K a^4}\right) \frac{1}{\sigma} \dots (1).$$

We see from this equation that if e is zero the equilibrium vapour pressure p for a drop of finite size is always greater than P, so that such a drop would evaporate unless the vapour around it were supersaturated; when however the drop is electrified this is no longer the case, for we see from equation (1) that in this case if the vapour is saturated, *i.e.* if the vapour pressure is P, the drop will grow until its radius a is given by the equation

$$\frac{2T}{a} - \frac{e^2}{8\pi K a^4} = 0.$$

Thus if the drop were charged with the quantity of electricity carried by a gaseous ion, i.e.  $3.4 \times 10^{-10}$  electrostatic units, and if the surface tension of the small drop had the value 76, which is the value for thick water films, then a would be equal to  $1/3.2 \times 10^7$ , and thus each gaseous ion would be surrounded by a drop of water of this radius; if we call this radius c, then equation (1) may be written

$$R\theta c \log_e \frac{p}{P} = 2Tx (1 - x^s) \dots (2),$$

where x = c/a. This equation enables us to find the size of a drop corresponding to any vapour pressure.

For water vapour at  $10^{\circ}$  C.,  $R\theta$  is equal to  $1.3 \times 10^{\circ}$ . Putting

for c the value previously found and T = 76, equation (2) becomes approximately

 $27 \log_e \frac{p}{P} = x (1 - x^s)$ ....(3).

From this equation we see that even in a space far from saturated with water vapour, i.e. when p is only a fraction of P, drops will be formed, and that the size of these drops diminishes only very slowly as the quantity of water vapour in the surrounding air diminishes; thus, if we diminish the quantity of water vapour in the air to 1/e, i.e. 1/2.7 of that required to saturate it, we see from equation (3) that the radius of the drops formed round the ions would only be a little less than 10/11 of the radius of the drop formed in saturated air: and that to reduce the drop to half the radius corresponding to saturation, we should have to dry the air so completely that p/P was only about  $1/3 \times 10^{16}$ . We have seen that there are always ions present in the air, hence there will always be small drops of water present if there is any water vapour in the air; if, as has been suggested, these drops play a part in certain cases of chemical combination, the preceding numerical example will show the difficulty of getting the gas dry enough to produce a substantial reduction in the volume of these charged drops.

83. Supersaturation required to make one of the charged drops grow to a large size. As the radius of the drop increases from c to an infinite size, x diminishes from unity to zero. Now the righthand side of equation (2) vanishes at each of these limits, but between them it reaches a maximum value which occurs when  $4x^3 = 1$  or  $x = \frac{1}{1.58}$ , when  $x(1-x^3)$  reaches the value '471; hence we see from equation (3) that for the drops to increase to a large size  $\log_e p/P$  must reach the value 1.7 approximately. Hence for the drops to grow p/P must be about 5.3: this, on the theory we have given, is the amount of supersaturation required to make large drops grow round the ions. We have seen from Wilson's experiment that it actually requires a four-fold supersaturation, but as in the theory the saturated water vapour was assumed to obey Boyle's law, and the surface tension was assumed to have the value it has for thick films, neither of which assumptions is likely to be true, the agreement between the theory and the experiments is as close as could be expected.

- 84. Wilson showed that even when there is no external ionisation a dense cloud, the nuclei of which are not charged, is produced by an eight-fold supersaturation: we can by the aid of equation (1) determine the radii of these nuclei, supposed spherical; putting in that equation e = 0, T = 76,  $R\theta = 1.3 \times 10^{\circ}$ , and p/P = 8, we find that a, the radius of the nucleus which produces this kind of condensation, is equal to  $1/1.9 \times 10^7$ . This nucleus is thus slightly larger than the drop which collects round an ion, as we found that the radius of this drop is  $1/3.1 \times 10^7$ . With regard to the nature of the nuclei which produce the cloud corresponding to the eight-fold supersaturation, Wilson has proved that the amount of supersaturation required to produce the cloud is the same in air, oxygen, hydrogen, and carbonic acid; the size of the nuclei is therefore the same in all these gases; it is thus very improbable that they consist of aggregations of the molecules of the gas, it would seem most likely that they are minute drops of water which are continually being formed from the saturated vapour and then evaporating, but lasting sufficiently long to enable them to be caught during the sudden expansion, and to act as the nuclei round which the drops in the cloud condense. These minute drops of water are not however all of the same size, for after passing the expansion 1:38 the density of the cloud increases very rapidly as the expansion increases, showing that many more nuclei become efficient when the expansion increases. This behaviour of the cloud indicates that there are little drops of water of different sizes, the small ones being more numerous than the larger ones, and that there is a fairly definite limit to the size of the drop, the number of drops whose size exceeds this limit being too small to produce an appreciable cloud. This collection of drops of different sizes is what we might expect if we regard the little drops as arising from coalescence of molecules of water vapour, and the larger drops from the coalescence of the smaller ones.
- 85. The fact that the drops are of different sizes indicates that they are not in a state of equilibrium with regard to evaporation and condensation, and the drops have probably a very ephemeral existence. It may however be pointed out that on the view of the relation between surface tension and the thickness of water films, to which Reinold and Rücker were led by their experi-

librium.

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ments on very thin films, drops of pure water of a definite radius might be in equilibrium with saturated water vapour even if they were not charged. For according to these physicists the relation between the surface tension and the thickness of the film is represented by a curve of the type shown in Fig. 39, the ordinates



Fig. 39.

representing the surface tension and the abscissæ the thickness of the film: this curve shows maxima and minima values for the surface tension.

Now consider the case of a drop whose diameter is a little greater than OM; in this case as the radius of the drop increases the surface tension diminishes; the potential energy due to surface tension is proportional to the product of the surface tension T and the area of the surface  $4\pi a^2$ ; hence if we can find a point between Q and T where  $\delta(T, 4\pi a^2) = 0$  or  $\frac{dT}{da} = -\frac{2T}{a}$ , any small change in the size of the drop would not be accompanied by a change in the potential energy due to surface tension. Thus surface tension would not affect the conditions of equilibrium between the liquid and the water vapour, so that if the volume were saturated with equilibrium the drop would be in equi-

86. We have seen that water vapour condenses more easily on a negative than on a positive ion, while the velocity of the negative ion under a given electric field is greater than that of the positive ion: the second result seems to indicate that the size of the system, consisting of the negative ion and whatever may be attached to it, is smaller than the system for the positive ion,

while the first indicates that it is larger. We must remember, however, that the velocity of an ion under an electric field is the average velocity estimated for the life of an ion. Now we have seen that the negative ion when first liberated is what we have called a corpuscle, and its mass is exceedingly small compared with that of the positive ion; thus at first the velocity of the negative ion will be greater than that of the positive, but in consequence of its greater mobility the negative ion is more likely than the positive to attach itself to foreign bodies in its neighbourhood, say to those minute drops of water which an expansion greater than 1:38 brings into evidence; thus though the negative ion starts by being smaller than the positive, it may before it recombines with a positive ion to form a neutral system have become the centre of an aggregation greater than that surrounding the positive ion. The efficiency of an ion as a nucleus for condensation depends upon the maximum size of the aggregation, while the velocity under the electric field depends upon the average size; the average size of a negative ion may easily be less than that of a positive ion, since the negative is so much smaller to begin with, while the greater mobility of the negative is likely to make it in the end the centre of a larger system than the positive.

## CHAPTER VIII.

## IONISATION BY INCANDESCENT SOLIDS.

87. WE shall now proceed to the study of some special cases of ionisation, beginning with that due to incandescent metals. the air in the neighbourhood of red-hot metals is a conductor of electricity has been known for nearly two centuries; the earliest observations seem to have been made by Du Fay\* in 1725, by Du Tour+ in 1745, by Watson; in 1746, by Priestley§ in 1767, and by Cavallo | in 1785. Becquerel f in 1853 showed that air at a white heat would allow electricity to pass through it even when the potential difference was only a few volts. Blondlot \*\* confirmed and extended this result, and proved that air at a bright red heat was unable to insulate under a difference of potential as low as 1/1000 of a volt; he showed, too, that the conduction through the hot gas was not in accordance with Ohm's law. Recent researches have thrown so much light on the causes at work in the ionisation of gases in contact with glowing solids, that it is unnecessary to enter into these earlier investigations in greater detail. Guthrie++ seems to have been the first to call attention to one very characteristic feature of ionisation by incandescent metals, i.e. the want of symmetry between the effects of positive and nega-He showed that a red-hot iron ball in air tive electrification. could retain a charge of negative but not of positive electrification, while a white-hot ball could not retain a charge of either positive or negative electrification.

\* Du Fay, Mém. de l'Acad. 1733.

|| Cavallo, Treatise on Electricity, vol. i. p. 324.

¶ Becquerel, Annales de Chimie et de Physique, iii. 39, p. 355, 1853.

<sup>†</sup> Du Tour, Mém. de Mathématique et de Physique, xi. p. 246, 1755.

<sup>‡</sup> Watson, Phil. Trans. abridged, vol. x. p. 296.

<sup>§</sup> Priestley, History of Electricity, p. 579.

<sup>\*\*</sup> Blondlot, Comptes Rendus, xcii. p. 870, 1881; civ. p. 283, 1887.

<sup>††</sup> Guthrie, Phil. Mag. iv. 46, p. 257, 1873.

88. The ionisation produced by incandescent metals was investigated systematically in great detail by Elster and Geitel\*, who used for this purpose the apparatus represented in Fig. 40.

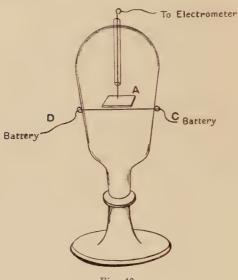


Fig. 40.

This is a glass vessel containing an insulated metal plate A, which is connected with one pair of quadrants of an electrometer. Underneath this plate there is a fine metallic wire, which can be raised to incandescence by an electric current passing through the leads C, D; to prevent any disturbing effects arising from the change produced by the current in the electric potential of the wire, the middle point of the wire was connected with the earth. Let us first take the case when the gas in the vessel is air or oxygen at atmospheric pressure, then, as soon as the glow of the hot wire begins to be visible, the metal plate receives a positive charge; this charge increases until the potential of the plate reaches a value which varies very much with the dimensions of the apparatus used: in Elster and Geitel's experiments it was of the order of a few volts. This potential increases as the temperature of the wire increases, until the wire is at a yellow heat; at

<sup>\*</sup> Elster and Geitel, Wied. Ann. xvi. p. 193, 1882; xix. p. 588, 1883; xxii. p. 123, 1884; xxvi. p. 1, 1885; xxxi. p. 109, 1887; xxxvii. p. 315, 1889. Wien. Berich. xcvii. p. 1175, 1889.

this stage the potential of the plate is a maximum. After passing this stage the potential diminishes as the wire gets hotter and hotter, until at a bright white heat the charge received by the plate is very small.

The electrification on the plate is very much influenced by the pressure of the gas. Starting at atmospheric pressure and gradually exhausting the vessel, we find that at first the change of pressure does not produce any great effect upon the potential of the plate A, but when we approach very high exhaustions, such as those in Crookes' tubes, the potential of the plate begins to diminish, until at very low pressures it changes sign and may as the exhaustion proceeds reach a very large negative value. The pressure at which the change in sign of the electrification of the plate takes place depends upon the temperature of the wire, the higher the temperature the higher the pressure at which the reversal of the electrification occurs. Again, long-continued incandescence of the wire favours the negative electrification of the plate; the physical condition of the platinum wire is changed by long-continued heating, and the wire becomes brittle. The following experiment, due to Elster and Geitel\*, seems to indicate that the gases absorbed in the platinum wire and which are gradually, but only very gradually, expelled by long-continued heating, play a considerable part in the electrical phenomena connected with the incandescence of metals. They found that if the platinum wire was kept glowing in a fairly good vacuum long enough for the metal plate to receive a negative charge, the introduction of a very small quantity of fresh gas reversed the sign of electrification on the metal plate, and the pressure had to be reduced far below the original value for the negative electrification to be recovered.

89. The effects are also complicated by the dust and vapour given off by the glowing platinum, and which form a deposit on the walls of the vessel. The production of this dust can very easily be shown by the study of clouds formed by the method described in Chapter VII. If a fine platinum wire is fused into the expansion apparatus, and the air rendered dust-free in the usual way, so that no clouds are produced by an expansion less than 1.25, dense clouds will be formed by comparatively small expansions after a current has been sent through the wire strong enough to raise it

<sup>\*</sup> Elster and Geitel, Wien. Berich. xcvii. p. 1175, 1889.

to incandescence\*; indeed it is not necessary to make the wire so hot as to be luminous, an increase in the temperature of the wire to 200 or 300° C. is sufficient to produce the cloud.

The sign of the electrification produced by glowing substances is influenced by the nature of the substances and of the gas surrounding them; thus in hydrogen Elster and Geitel† showed that the plate above the incandescent wire became negatively electrified even when the hydrogen was at atmospheric pressure. This electrification continually increased with the temperature. To get the negative electrification, however, the wire must be at least at a bright yellow heat; at lower temperatures the electrification is positive; a clean copper wire, on the other hand, gives a positive electrification in hydrogen, unless the pressure is very low.

Elster and Geitel showed that the sign of the electrification in water vapour and the vapours of sulphur and phosphorus was the same as in air; they could detect no electrification in mercury vapour.

- 90. The influence of the nature of the incandescent substance is shown by the fact that with incandescent carbon filaments the electrification on the metal plate is always negative. It is also shown clearly by some experiments made by Branly<sup>+</sup>. Branly's method was as follows: he hung up a charged insulated conductor in the neighbourhood of the incandescent body; he found that when the latter was a piece of platinum at a dull red heat the insulated conductor lost a negative but not a positive charge; when the platinum was white hot the conductor was discharged whether electrified positively or negatively. If the incandescent body was an oxide and not a pure metal, at any rate if it was an oxide of one of the metals tried by Branly, viz. lead, aluminium or bismuth, then it would discharge a positively electrified body but not a negatively electrified one, which is exactly opposite to the effect produced by a pure metal at a dull red heat.
- 91. McClelland sucked the gases from the neighbourhood of the incandescent wire and then investigated their properties. He

<sup>\*</sup> R. v. Helmholtz, Wied. Ann. xxxii. p. 1, 1887. Lodge, Nature, xxxi. p. 267, 1884.

<sup>†</sup> Elster and Geitel, Wied. Ann. xxxi. p. 109, 1887.

<sup>‡</sup> Branly, Comptes Rendus, exiv. p. 1531, 1892.

<sup>§</sup> McClelland, Proc. Camb. Phil. Soc. x. p. 241, 1900.

found that as soon as the wire began to glow the gas would discharge a negatively but not a positively electrified body; when the temperature of the electrified body was increased by about 400° C., the gas began to discharge a positively electrified body, though not so freely as it did a negatively electrified one; when the wire got to a bright yellow heat the gas discharged both positive and negative electricity with equal facility. McClelland investigated the laws of conduction of electricity through the gas which had been in contact with the glowing wire; he found that it showed all the characteristics of conduction through a gas containing ions; thus the relation between the current and the electromotive force is represented by a curve like Fig. 5, the current soon reaching saturation. McClelland also determined the velocity in an electric field of the ions, produced by the incandescent metal. He found that their velocity was small compared with that of the ions produced by Röntgen rays, and that the hotter the wire the smaller was the velocity of the ions.

- **92**. The account we have already given of the effects observed in the neighbourhood of an incandescent wire shows that the electrification produced in this way is a very complicated phenomenon, and depends:
  - (1) On the temperature of the wire.
  - (2) On the pressure of the gas around the wire.
  - (3) On the nature of the gas.
  - (4) On the nature of the incandescent wire.

We shall simplify the investigation of the cause of this electrification if we study a case in which as many as possible of these effects are eliminated. Now (2) and (3) are eliminated if we work with the highest attainable vacuum; in this case the phenomena are greatly simplified and exhibit points of remarkable interest. To investigate them we may use a piece of apparatus like that shown in Fig. 41. It consists of a straight piece of fine wire AB, which can be heated to any desired temperature by an electric current led in through the leads CA, DB. Around this wire and insulated from it is a metallic cylinder, shown in section in EF and GH; this cylinder should be longer than, and coaxial with, the wire. This system is sealed into a glass vessel connected with an air pump and the pressure reduced as low as possible, say to

'001 mm. of mercury. It is desirable to keep the wire red hot for a very considerable time (I have found a week not too long), in

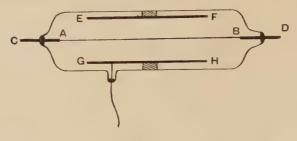


Fig. 41.

order to expel gases absorbed in the wire; until these are got rid of the behaviour of the wire is very irregular. The vessel should be pumped from time to time while the wire is hot, to get rid of the gases coming out of the wire; it will be necessary to exhaust the vessel from time to time, even after these have been expelled, as the heat coming from the wire seems to liberate gas from the walls of the glass vessel and the metal cylinder. Connect the hot wire to one terminal of a battery and the cylinder to the other, and place in the circuit a sensitive galvanometer. If now the wire be made red hot and connected with the negative pole of the battery, an appreciable current will go through the galvanometer; if, however, the terminals are reversed so that the hot wire is connected with the positive pole of the battery, the current which passes is too small to be detected by the galvanometer; thus there can be a current through the exhausted vessel when the negative electricity goes from the hot wire to the cold cylinder, but not an appreciable one when the positive electricity would have to go from the wire to the cylinder; the system can thus transmit a current in only one direction. The current does not obey Ohm's law: at first it increases with the electromotive force, but it soon reaches a saturation value beyond which it does not increase, even though the electromotive force is increased. provided the increase is not sufficient to enable the field itself to ionise the gas. In some experiments made by the author, about 10 volts was sufficient to produce the saturation current.

93. The saturation current increases very rapidly with the temperature. This is well shown by the curve in Fig. 42, which

represents the results of the experiments made by O. W. Richardson\*, in the Cavendish Laboratory, on the saturation current between a hot platinum wire and a metal cylinder surrounding it

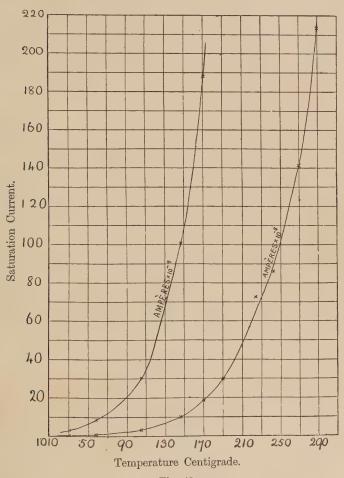


Fig. 42.

in a high vacuum. The temperatures were obtained by measuring the resistance of the wire. Richardson found that the relation between the saturation current I and the absolute temperature  $\theta$  could be expressed by an equation of the form

$$I = a\theta^{\frac{1}{2}} \epsilon^{-\frac{b}{\theta}} \,,$$

\* O. W. Richardson, Proc. Camb. Phil. Soc. xi. p. 286, 1902.

for the curve in Fig. 42,

$$a = 1.51 \times 10^{26}, \quad b = 4.93 \times 10^{4}.$$

In the case of this wire the current amounted to about  $4\times 10^{-4}$  ampères at the temperature  $1500^{\circ}$  C., which represents a rate of emission of negative electricity from the hot wire of above one milliampère per square centimetre of surface. If the same formula held up to the melting point of platinum, which we shall take to be  $2000^{\circ}$  C., the rate of emission of negative electricity from the glowing wire would be about 1/10 of an ampère per square centimetre.

The rate of escape of negative electricity from glowing carbon in some cases greatly exceeds that from glowing platinum. This is no doubt chiefly owing to the fact that the carbon can be raised to a much higher temperature than the platinum. Richardson has obtained from carbon filaments in a good vacuum currents of the order of an ampère per square centimetre of surface.

94. This escape of negative electricity from glowing carbon in high vacua is the cause of an effect observed in incandescent electric lamps, known as the Edison effect, and which has been studied by Preece\* and in great detail by Fleming†. The 'Edison effect'

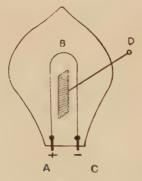


Fig. 43.

is as follows: Suppose that ABC represents the carbon filament of an incandescent lamp, and that an insulated metal plate is

<sup>\*</sup> Preece, Proc. Roy. Soc. xxxviii. p. 219, 1885.

<sup>+</sup> Fleming, Proc. Roy. Soc. xlvii. p. 118, 1890; Phil. Mag. xlii. p. 52, 1896.

inserted between the filaments; then if the positive end A of the filament is connected with a wire D leading from the metallic plate and a galvanometer inserted between A and D, a considerable current, amounting in some of Fleming's experiments to three or four milliampères, passes through the galvanometer, the direction of the current being from A to D through the galvanometer. If, however, the metal plate is connected with the negative electrode of the lamp and a galvanometer inserted in this circuit, the current through the galvanometer is exceedingly small compared with that observed in the preceding case. We see that this is what would occur if there was a vigorous discharge of negative electricity from the negative leg of the carbon filament, and no discharge or a much smaller one from the positive leg; this would tend to make the potential of the metal plate differ but little from that of the negative leg of the carbon loop, while the difference of potential between the positive leg and the plate would be nearly that between the electrodes of the lamp, and consequently the current through a circuit connecting the positive electrode to the metallic plate would be much greater than through one connecting the negative electrode to the plate.

Fleming showed that when the negative leg of the carbon loop was surrounded by a cylinder made either of metal or of an insulating substance, the Edison effect disappeared almost entirely. Fleming too found, as Elster and Geitel had previously shown by a somewhat different method, that a current of electricity could pass between an incandescent carbon filament and a cold electrode, if the direction of the current was such as to cause the negative electricity to pass from the hot filament to the cold plate, and that a current would not pass in the opposite direction. Elster and Geitel showed, too, that a plate placed near an incandescent filament received even in very high vacua a charge of negative electricity. The behaviour of the hot filament shows that it, like the incandescent platinum wire, emits negative electrification. That the emission from the carbon filament is much greater than that from the platinum wire—great as we have seen the latter to be—is shown by the fact that although, as Fleming (loc. cit.) has shown, the 'Edison effect' can be observed with an incandescent platinum wire in place of the carbon filament, the effect with platinum is exceedingly small compared with that with carbon, and

is only appreciable when the platinum is so hot that it is on the point of melting.

95. There can thus be no doubt that from incandescent metals and carbon there is a very rapid escape of negative electricity. The question arises, What are the carriers of this electrification? The answer to this question seems at first sight obvious, for both the carbon filament and the platinum wire volatilise, or at any rate give off dust if not vapour at high temperatures. This is shown by the familiar deposit of carbon on the glass of incandescent lamps, and of platinum or platinum oxide on the walls of an exhausted vessel in which a platinum wire has been glowing for a long period. It seems natural, therefore, to regard the carriers of the negative electricity as the molecules or atoms of carbon or platinum vapour. We might, however, be led to suspect the accuracy of this view when we observe the enormous quantities of negative electricity which can be discharged by a small piece of very thin wire; quantities which are inconsistent with that law of electrolysis which states that to carry a quantity of electricity E we require a mass of a substance  $E_{\epsilon}$ , where  $\epsilon$  is the electrochemical equivalent of the substance.

We can, however, determine by the method of Art. 51 the ratio of the charge e to the mass m of the carriers of the negative electricity from an incandescent wire. The results of this determination, which are given in Art. 51, are conclusive, for they show that the value of e/m for these carriers is the same as its value for the carriers of the negative electricity in the cathode rays, and in the discharge of negative electricity from metals placed in a good vacuum and illuminated by ultra-violet light. Thus the negative electricity from the hot wire is carried by the same carriers as the cathode rays, i.e. by 'corpuscles,' those small negatively electrified bodies of constant mass which in all the cases yet investigated act as the carriers of negative electricity in high vacua.

We thus are led to the conclusion that from an incandescent metal or glowing piece of carbon 'corpuscles' are projected, and though we have as yet no exact measurements for carbon, the rate of emission must, by comparison with the known much smaller rate for platinum, amount in the case of a carbon filament at its highest point of incandescence to a current equal to several ampères per square centimetre of surface. This fact may have an important application to some cosmical phenomena, since, according to the generally received opinion, the photosphere of the sun contains large quantities of glowing carbon; this carbon will emit corpuscles unless the sun by the loss of its corpuscles at an earlier stage has acquired such a large charge of positive electricity that the attraction of this is sufficient to prevent the negatively electrified particles from getting right away from the sun; yet even in this case, if the temperature were from any cause to rise above its average value, corpuscles would stream away from the sun into the surrounding space. We may thus regard the sun, and probably any luminous star, as a source of negatively electrified particles which stream through the solar and stellar systems. Now when corpuscles moving at a high speed pass through a gas they make it luminous; thus when the corpuscles from the sun meet the upper regions of the earth's atmosphere they will produce luminous effects. Arrhenius\* has shown that we can explain in a satisfactory manner many of the periodic variations in the Aurora Borealis if we assume that it is caused by corpuscles from the sun passing through the upper regions of the earth's atmosphere.

The emission of corpuscles from incandescent metals and carbon is readily explained by the view—for which we find confirmation in many other phenomena—that corpuscles are disseminated through metals and carbon, not merely when these are incandescent, but at all temperatures; the corpuscles being so small are able to move freely through the metal, and they may thus be supposed to behave like a perfect gas contained in a volume equal to that of the metal. The corpuscles are attracted by the metal, so that to enable them to escape into the space surrounding it they must have sufficient kinetic energy to carry them through the layer at its surface, where its attraction of the corpuscles is appreciable. If the average kinetic energy of a corpuscle like that of the molecule of a gas is proportional to the absolute temperature, then as the temperature increases, more and more of the corpuscles will be able to escape from the metal into the air outside.

<sup>\*</sup> Arrhenius, Physikalische Zeitschrift, ii. pp. 81, 97, 1901.

Rate at which the corpuscles escape from the metal.

96. We can without much difficulty find an expression for this quantity if we assume that the corpuscles in the metal behave like a perfect gas. Let AB, CD represent two planes parallel to the surface of the metal including between them the region in which the metal exerts an appreciable force upon the corpuscle. Let us take the axis of x at right angles to these planes, the positive direction of x being from the air to the metal; then if p is the pressure due to the corpuscles, n the number of corpuscles in unit volume, X the force acting on a corpuscle, we have when there is equilibrium

$$\frac{dp}{dx} = Xn \dots (1);$$

but if the corpuscles behave like a perfect gas  $p = \beta \theta n$ , where  $\theta$  is the absolute temperature and  $\beta$  a constant which is the same for all gases; substituting this value for p in equation (1), we get

$$\beta\theta \frac{dn}{dx} = X n....(2);$$

integrating this equation from CD to AB, we get

$$\log \frac{n'}{N} = -\frac{w}{\beta \theta},$$

$$n' = N e^{-\frac{w}{\beta \theta}}....(3),$$

or

where n' and N are respectively the numbers of corpuscles in unit volume of the air and metal, and

$$w = \int X \, dx \; ;$$

thus w is the work required to drag a corpuscle out of the metal.

Equation (3) gives the number of corpuscles in the air when things have attained a steady state. To find the number of corpuscles coming from the metal in unit time let us proceed as follows: regard the steady state as the result of a dynamical equilibrium between the corpuscles going from the metal to the air and those going from the air to the metal. If n' is the number of corpuscles in unit volume of the air, the number which

in one second strike against unit area of the metal is by the Kinetic Theory of Gases equal to

$$\overset{*}{+} \sum_{0}^{\infty} u dn,$$

dn being the number of corpuscles which have velocities between u and u + du, and the summation is to be taken for all positive values of u. Now if n' is the total number of corpuscles in unit volume

$$dn = n' \sqrt{\frac{hm}{\pi}} \, \epsilon^{-hmu^2} \, du,$$

where m is the mass of a corpuscle: hence

$$\sum_{0}^{\infty} u \, dn = n' \, \sqrt{\frac{hm}{\pi}} \int_{0}^{\infty} e^{-hmu^{2}} u \, du$$

$$= \frac{1}{2} \frac{n'}{\sqrt{\pi hm}}$$

$$= \frac{n'c}{\sqrt{6\pi}},$$

where c is the velocity of mean square and is equal to  $\alpha(\theta/m)^{\frac{1}{2}}$ ,  $\alpha$  being a constant which is the same for all gases: substituting the value of n' from equation (3) we find that the number of corpuscles coming from the air and striking against unit area of the metal in unit time is equal to

$$rac{lpha}{\sqrt{6\pi}} \Big(rac{ heta}{m}\Big)^{\! rac{1}{2}} N \epsilon^{-rac{w}{eta heta}} \, ;$$

if we suppose that all the corpuscles which strike against the metal enter it, this will be the number of corpuscles entering the metal, and therefore in the steady state the number leaving it; the number may be written in the form

$$a\theta^{\frac{1}{2}}\epsilon^{-\frac{b}{\theta}}$$
:

this number multiplied by e will be the quantity of negative electricity leaving unit area of the metal in unit time, and therefore will be the saturation current from a hot wire at the temperature  $\theta$ . Richardson's measurements of the saturation current at different temperatures agree well, as we have seen, with a formula of this form. From the values of a and b determined by experiments on the escape of electricity from a hot wire

we can deduce the values of N and w. Richardson found that for platinum

 $a = 1.5 \times 10^{26}$  and  $b = 4.93 \times 10^{4}$ ;

this gives

 $N = 1.3 \times 10^{21}$  and  $w = 8 \times 10^{-12}$  ergs.

The pressure due to the corpuscles in the metal would at atmospheric temperature be between 30 and 40 atmospheres.

The emission of the negative corpuscles from heated substances is not, I think, confined to the solid state, but is a property of the atom in whatever state of physical aggregation it may occur, including the gaseous. The emission of the negative corpuscles from the atoms is well shown in the case of sodium vapour; if a little sodium be placed in a tube from which all gas has as far as possible been exhausted there will be in the dark no leak from a charged conductor sealed in the tube, if however the temperature is raised to about 300° C. in the dark a considerable leakage of electricity from the charged conductor will occur, whether the charge be positive or negative; the leak in the former case is however greater than in the latter. It might be thought that the leak is due to the corpuscles given out by the solid sodium in the tube, these however would be negatively charged and could not discharge a negatively charged conductor; nor is it due to sodium condensed on the charged conductor itself, for there is no leak on cooling down to the temperature of the room and exposing the charged conductor when negatively electrified to light; if sodium had condensed on the charged metal the leak would have been very perceptible.

The emission of the negatively electrified corpuscles from sodium atoms is conspicuous as it occurs at an exceptionally low temperature; that this emission occurs in other cases although at very much higher temperatures is, I think, shown by the conductivity of very hot gases (or at any rate by that part of it which is not due to ionisation occurring at the surface of glowing metals), and especially by the very high velocity possessed by the negative ions in the case of these gases; the emission of negatively electrified corpuscles from atoms at a very high temperature is thus a property of a very large number of elements, possibly of all.

The emission of corpuscles from the atom must play a very

important part in the decomposition of the molecules of a compound by heat, if the forces which bind the atoms together in the molecule are mainly electrical in their origin. For imagine a molecule consisting of two atoms, one, A, positively, the other, B, negatively electrified, and suppose that the temperature is raised until the point is reached when the negatively electrified atom begins to discharge the negatively electrified corpuscles: when this stage is reached B loses a corpuscle. Let us suppose that under the electric field this corpuscle finds its way to the positively electrified A neutralising its charge, so that momentarily A and B are without charge, the attraction previously existing between them is annulled and there is no longer anything to prevent their drifting apart. It does not follow however that the molecule is necessarily permanently split up, for A has now no positive charge to prevent the negative corpuscles from escaping, and as it is the electro-positive element in the compound it would under similar conditions lose corpuscles more readily than B; thus A will soon regain its positive charge. B being without charge cannot discharge negative corpuscles as easily as it did previously when it was negatively electrified, thus some time may elapse before B emits a corpuscle, and in the interval it may get struck by a negative corpuscle and thus acquire a negative charge, recombination might then occur between it and the positively charged A, this combination being dissolved again by the process we have already sketched. We should thus get to a state in which there is statistical equilibrium, the number of recombinations in unit time being equal to the number of atoms dissociated in that time: the proportion of the free to the combined atoms will depend upon the properties of each of the atoms; the more easily A loses its corpuscles by heating and the greater the difficulty of getting the corpuscles out of B, the smaller will be the proportion of free atoms. These considerations show that heat may produce dissociation in other ways than the more commonly recognised one of increasing the kinetic energy until the centrifugal force is great enough to overpower the attraction.

98. We thus see that from an incandescent wire corpuscles are projected at a rate sufficient to produce a very large rate of leak when the pressure of the gas surrounding the wire is very low; at such pressures there is very little gas to hamper the motion of

the corpuscles, which consequently can move with very high velocities; as soon as a corpuscle emerges from the incandescent surface it travels away from it towards the cylinder surrounding the wire, and when the current between the wire and the cylinder is saturated none of the corpuscles diffuse back again into the wire.

When however the pressure of the gas surrounding the wire is considerable the corpuscles cannot travel so freely, they tend to accumulate in the neighbourhood of the wire and some of them diffuse back into it again. The density of the corpuscles in the neighbourhood of the wire cannot exceed a definite value, given by equation (3), p. 166: just as in the case of the evaporation of a liquid, the pressure of vapour in contact with the liquid cannot exceed a definite value depending upon the temperature.

99. To drive through a gas at a considerable pressure currents comparable with those easily obtainable in a vacuum would require the application of very large differences of potential. For let us take the case of two parallel plates at right angles to the axis of x, 1 cm. apart; let the plate x = 0 be the hot plate, X the electric force at a point x,  $u_0$  the velocity of a corpuscle under unit electric force; then if the velocity of the corpuscle is proportional to the electric force, the velocity at the point x will be  $u_0X$ , and if n be the number of corpuscles per unit volume, e the charge on a corpuscle, i the current through unit area, then we have

hence 
$$i=u_{0}Xne,$$
 
$$\frac{dX}{dx}=4\pi ne,$$
 
$$X\frac{dX}{dx}=\frac{4\pi i}{u_{0}},$$
 
$$X^{2}=\frac{8\pi i}{u_{0}}x+X_{0}^{2},$$

where  $X_0$  is the value of X at the surface of the plate. From this equation it follows that if V is the potential difference between the plate and a point x away from it, then

$$V > \left(\frac{8\pi i}{u_o}\right)^{\frac{1}{3}} \frac{2}{3} x^{\frac{3}{2}}.$$

From this expression we may calculate a lower limit to the potential difference necessary to send a current of 1 milliampère per square centimetre from a hot to a cold plate 1 cm. distant when the gas is at atmospheric pressure; in a high vacuum and at a white heat such a current could be produced by a potential difference of 100 volts or so. In order to get a lower limit for V we shall give to  $u_0$  the greatest value which has been observed for the negative ions at atmospheric pressure; this is the value obtained by H. A. Wilson in the case of flames at a temperature of about  $2000^{\circ}$  C. and is equal to 1000 cm./sec. for a potential gradient of 1 volt per cm. If we use the electrostatic system of units, the unit electric force is 300 volts per cm.; hence for the case quoted  $u_0 = 3 \times 10^5$  cm./sec.: on the same system of units 1 milliampère =  $3 \times 10^5$ ; substituting these values of i and  $u_0$  and putting x = 1, we find V > 11 electrostatic units or 3300 volts.

From these results we see that if the emission of corpuscles was the only effect occurring at the surface of the wire we should at high pressures get a small leak when the hot wire was charged negatively, no leak when it was charged positively. There would be no positive leak because the corpuscles are negatively electrified, and a positive leak requires a supply of positive ions. The negative corpuscles when moving with sufficient velocity through a gas ionise it, and if the corpuscles coming from the wire moved fast enough they would ionise the gas around the wire, and thus produce a supply of positive as well as negative ions; the velocity however possessed by at any rate an enormous majority of the ions from the metal is far too small to produce this ionisation. When the field is so intense that the corpuscles acquire sufficient velocity to ionise the gas the current will increase rapidly with the pressure.

The phenomena we have already described show that when gas is present there must be other sources of ionisation besides the corpuscles: for we have seen that beginning at a very dull red heat there are positive ions around the wire, and these increase as the temperature increases; negative ions do not however make their appearance until about a bright yellow heat; they increase more rapidly with the temperature than the positive, until at very high temperatures there are as many negative as positive; indeed,

in the opinion of Koch\*, the number of the negative ions at these high temperatures exceeds that of the positive. There is evidently some source of ionisation besides the emission of corpuscles and one which begins at a much lower temperature. We proceed to the consideration of some of the effects arising from it.

100. Incandescent wire surrounded by gas. We have first to notice that the source of the ionisation is at the surface of the incandescent metal, and does not extend to any considerable distance in the gas. One proof of this is that the saturation current between an incandescent metal plate and a parallel plate is independent of the distance between the plates; thus in some experiments I made on this point I found that the saturation current was the same when the plates were 3 mm. apart as when they were 5 mm., the pressure was that due to about 25 mm. of mercury; thus even at this low pressure the source of ionisation did not extend as much as 3 mm. from the hot plate, for if it had done so the saturation current would have been less at the smaller distance.

Another very striking proof of the same thing is afforded by the experiments of H. A. Wilson + on the conductivity of flames containing the vapours of metallic salts. If two pieces of platinum foil are immersed in a flame so as to be heated to a red heat and are connected with the terminals of a galvanic battery, a current will pass through the flame from one of these electrodes to the other. This current is very largely increased when volatile salts are placed in the flame so as to introduce into it large quantities of salt vapour. Wilson found that when this vapour was produced by placing a small bead of the salt in the flame there was little or no increase in the current when the bead was so placed that the vapour did not come into contact with either electrode; when the vapour came into contact with the positive electrode there was a substantial increase and when it touched the negative electrode a very large one. The increase in the current produced by the vapour indicates an increase in the number of ions, and the preceding results show that this increase does not take place unless the metallic vapour comes into contact with the glowing metal.

<sup>\*</sup> Koch, Wied. Ann. xxxiii. p. 454, 1888.

<sup>†</sup> H. A. Wilson, Phil. Trans. A. 192, p. 499, 1899.

Another proof that the ionisation is confined to the surface of the hot metal is that the saturation current between the two electrodes is independent of their distance apart.

We can by the following method\* measure the conductivity of a flame without introducing into it any metallic electrodes and can thus directly determine the change if any produced in the case by the admixture of salt vapours. A and B (Fig. 44) are two

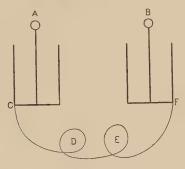


Fig. 44.

Leyden jars the insides of which are connected with the terminals of an induction coil or electric machine. The outside coatings of these jars are connected by the circuit CDEF containing the two loops D and E; in one of these loops, E, a glass bulb containing gas at a very low pressure is placed: when the coil or machine is in action the jars are continually being charged and discharged; each time the jars are discharged alternating currents with, for moderate sized jars, a frequency of some millions per second pass through the wire CDEF; the currents flowing round the loop E induce currents through the rarefied gas in the bulb, these currents through the gas make it luminous, so that the discharge of the jar is accompanied by a bright ring in the bulb in E. If conductors of not too great conductivity are inserted in the loop D it will be found that the brightness of the ring in E is diminished, and the higher the conductivity the greater the diminution; in this way by observing the effects of different conductors when placed in D we can get some idea of their conductivity. Now Wilson found that the effect of the flame of a Bunsen burner passing through D upon the ring discharge in E was quite appreciable, but

<sup>\*</sup> J. J. Thomson, Proc. Camb. Phil. Soc. viii. p. 258, 1895.

that this effect was not perceptibly increased when salt vapours were introduced into the flame though the current between electrodes in the flame was increased several hundred times by the introduction of the salt.

The effect of a conducting metallic plate in facilitating ionisation in its neighbourhood is very easily explained; ionisation involves the separation of a positive from a negative charge of electricity; if these charges are placed close to a metallic plate, other charges will be induced in the plate which will almost annul the attraction between the original charges; these therefore will be much more easily separated than when they are far from conductors and the attraction between them has its normal value. The strong ionisation of salts in solvents having very large specific inductive capacities is another aspect of the same phenomenon, for a dielectric of high inductive capacity produces much the same kind of effect on the attraction between electrical charges in its neighbourhood as a conductor: it thus facilitates the separation of the charges and therefore ionisation. Water, alcohol, and indeed all ionising solvents have large specific inductive capacities.

If the ionisation is confined to the surface of the incandescent metal, then the current between a hot electrode and a cold one will be carried by ions of one sign, even though ions of both signs are found at the surface of the metal. When the temperature is so low that only ions of one sign are produced at the metal (as is the case with platinum below a yellow heat), then all the ions carrying the current must have come from the same electrode. This explains an effect observed by the author many years ago \*: the current between two pieces of platinum foil immersed in a vessel heated to a bright red heat was found to be completely stopped by placing a cold metallic plate between the electrodes and the current did not recommence until the middle plate was raised to incandescence. This is evidently what would occur if there was a production of positive ions at the two electrodes A and B and nowhere else; for suppose A is the positive electrode, then all the ions which reach B have started from A; if we place between A and B a plate whether made of a conductor or insulator we stop all the ions before they reach B and thus stop the current. The current

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 29, p. 441, 1890.

will recommence when the plate gets hot enough to produce ions at its surface. If ions of both signs are produced at each of the hot plates the current will not be stopped by the middle plate but will be greatly diminished.

101. Relation between the current and the potential difference. Let us consider the case of two parallel plates at right angles to the axis of x, then if only one of the plates is incandescent, or if both are incandescent but the temperature is so low that only positive ions are produced at the surface of the plates, then the ions carrying the current between the plates will be all of one sign and we may apply the results of Art. 98. Hence if X is the electric force, R the velocity of the ion under unit electric force, we have, if i is the current,

$$X\frac{dX}{dx} = \frac{4\pi i}{R};$$

hence if R is independent of x we have

$$X^2 = \frac{8\pi i}{R} x + C;$$

if the current is small X vanishes at the hot plate, hence if the equation to this plate is x = 0,

$$X = \left\{ \frac{8\pi i}{R} \right\}^{\frac{1}{2}} x^{\frac{1}{2}} ;$$

if V is the difference of potential between the plates, d the distance apart, we have

$$V = \left(\frac{8\pi i}{R}\right)^{\frac{1}{2}} \frac{2}{3} d^{\frac{2}{3}},$$

$$i = \frac{9RV^{2}}{32\pi d^{3}} \qquad (1).$$

or

This equation has been tested by Rutherford\*; we cannot however expect the theory to be in very close agreement with the facts, for in deducing equation (1) we have made several assumptions which are not satisfied in practice; in the first place we have assumed that R is independent of x, this will only be true when the temperature is uniform between the plates, it will not be true when one plate is hot and the other cold, for the velocity

<sup>\*</sup> Rutherford, Physical Review, xiii. p. 321, 1901.

of the ion depends upon the temperature. Thus H. A. Wilson\* has shown that in a flame at the temperature of about 2000° C. the velocity of the negative ion under a potential gradient of 1 volt per cm. is about 1000 cm./sec., that of the positive ion under the same gradient 62 cm./sec.; in hot air at a temperature of about 1000° C. the velocity of the negative ion is only about 26 cm./sec., that of the positive about 7.2 cm./sec. McClelland+ found that the ions from an incandescent wire when they got into the cold air at some distance from the wire travelled with velocities as small as 04 cm./sec.: and that the velocity diminished as the ions got further from the wire and could be increased again by warming the ions; thus R varies rapidly with the temperature and therefore with x.

The increase of R with the temperature makes the current increase rapidly with the temperature of the hot plate. We see from equation (1) that the current for a constant small difference of potential does not depend upon the amount of ionisation near the plate $^+_+$ , so that the increase of ionisation at the higher temperature would not explain the increase of current when the wire gets hotter; a satisfactory explanation of this increase is however afforded by the increase of R with the temperature.

When the temperature of the hot plate is high enough for negative as well as positive ions to exist near the plate, the leak between the hot plate and a cold one will be greater when the hot plate is the negative electrode than when it is the positive: for in the former case the current is carried by negative ions, in the latter by positive, and equation (1) shows that with the same potential difference the current is proportional to the velocity of the ion by which it is carried. Now the velocity of the negative ion is always greater than that of the positive, and the ratio of the velocity of the negative to that of the positive increases rapidly with the temperature; thus the experiments of H. A. Wilson on the leak through gases mixed with the vapours of salt (l.c.) show that this ratio at 2000° C. is about 17 while at 1000° C. it is only about 3.5. At ordinary temperatures for the case of ions drawn

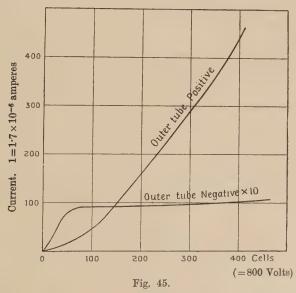
<sup>\*</sup> H. A. Wilson, Phil. Trans. A. 192, p. 499, 1899.

<sup>+</sup> McClelland, Phil. Mag. v. 46, p. 29, 1899.

<sup>‡</sup> It must be remembered that equation (1) only applies when the current is small, so that X=0 when x=0; when the current approaches saturation it increases rapidly with the amount of ionisation at the plate.

from the neighbourhood of the hot wire, M°Clelland's experiments show that this ratio is only about 1.25. The great increase of current produced by changing the sign of a very hot electrode from + to - is a very well marked phenomenon; one striking example of it is furnished by an old experiment of Hittorf's\*. In this experiment a bead of salt was placed in a flame between glowing electrodes: the increase in the current was much greater when the bead was placed close to the negative electrode than when it was placed near to the positive. These results, it must be remembered, are only true when the currents are very small compared with their saturation values; the saturation values do not depend upon the velocities of the ions but only upon the number of ions produced in unit time at the surface of the hot metal.

The velocity of an ion under a constant electric force increases as the pressure of the gas diminishes, hence we see from equation (1) that the current when small will increase when the pressure diminishes.



102. A well-marked feature of the discharge from incandescent metals is the very rapid increase of the current, when this is small,

<sup>\*</sup> Hittorf, Pogg. Ann. Jubelband, p. 430, 1874.

with the electromotive force, an increase much more rapid than that given by Ohm's law. This has frequently been observed; thus, for example, Pringsheim  $\ast$  gives as an empirical formula for the current i in terms of the potential difference V for the discharge between two pointed electrodes in a hot gas

$$i = \frac{V + aV^2}{w},$$

where a and w are constants. The rapid increase in the current is well illustrated by the curve in Fig. 45 given by H. A. Wilson + for the case of the current between a hot platinum wire and a hot platinum tube outside it; in this curve the ordinates represent the current and the abscissæ the potential differences, the curve for the case when the tube is negative illustrates too the 'saturation' of the current under high electromotive forces. This rapid increase of the current is accounted for by equation (1), which shows that the current is proportional to the square of the potential difference.

103. The nature of the carriers of the electricity in the current from a hot wire. The discharge of positive electricity from a wire at a temperature between a red and yellow heat is not determined solely by the nature and pressure of the gas and the temperature of the wire, it is very largely influenced by the treatment to which the wire has been subjected previous to the discharge. Thus if we measure the leak between a hot wire and a cold metal cylinder surrounding it, the gas being at a low pressure, we often find that when the wire is first heated the leak is very large to begin with, but slowly diminishes until after several hours' continuous heating the current may have sunk to 1/20 of its original value: if when it has fallen to this point fresh gas is introduced into the vessel containing the hot wire and then after some time pumped out until the pressure is the same as before the introduction of the gas, the current is very greatly increased for a time; it again diminishes as the heating continues but can be revived by the introduction of fresh gas. As this diminution occurs whether or not the current is kept flowing between the hot wire and the surrounding cylinder, it cannot be due to an effect analogous to the

<sup>\*</sup> Pringsheim, Wied. Ann. lv. p. 507, 1895.

<sup>+</sup> H. A. Wilson, Phil. Trans. A. 197, p. 415, 1901.

ordinary polarisation of electrolytes, although we shall see reasons for thinking that such an effect does exist to some extent in conduction through hot gases.

The facts just mentioned suggest that the gas absorbed by the platinum and slowly given off when heated plays an important part in the carriage of the electricity from the wire, and we can easily understand how this gas, coming straight from the midst of a good conductor, would be ionised and able to carry the current. The emission of absorbed gas from the platinum is however, according to Berliner\*, closely connected with the disintegration of the platinum wire which takes place when the wire is kept glowing and which is made evident by a deposit of platinum or platinum oxide on the walls of the tube and a diminution in the weight of the hot wire: the carriers of the electricity might thus be the dust or vapour of platinum escaping from the wire. This disintegration of the platinum has been studied by Berliner\*, Elster and Geitel †, Nahrwold ‡, and Stewart §: who have shown

- (1) That the amount of disintegration produced in a given time by the incandescence of a platinum wire diminishes after prolonged heating.
- (2) That the amount of this disintegration is very much increased by the presence of oxygen. It is exceedingly small in nitrogen and hydrogen; indeed, some of the experiments suggest that there would be no disintegration of a glowing platinum wire in these gases if every trace of oxygen could be removed from them. We may suppose that where oxygen is present slight oxidation takes place, producing a weathering of the surface which facilitates the disintegration of the metal.

The disintegration of the platinum can be easily shown by the effect of the incandescence of the wire on the condensation of clouds in the air in its neighbourhood. We owe this method to Aitken ||. One simple way of showing this effect is to have a fine platinum wire fused in the expansion chamber in the cloud

<sup>\*</sup> Berliner, Wied. Ann. xxxiii. p. 289, 1888; xxxv. p. 791, 1888.

<sup>†</sup> Elster and Geitel, Wied. Ann. xxxi. p. 109, 1887.

<sup>‡</sup> Nahrwold, Wied. Ann. xxxi. p. 448, 1887; xxxv. p. 107, 1888.

<sup>§</sup> Stewart, Phil. Mag. xlviii. p. 481, 1889.

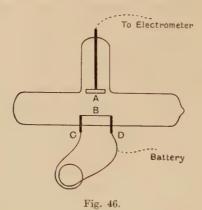
<sup>||</sup> Aitken, Trans. Roy. Soc. Edin. xxx. p. 337.

apparatus (Fig. 37). If the air be made dust-free when the wire is cold, then on sending a current through the wire so as to raise it to a red heat and then letting it cool, a dense cloud is produced by a very small expansion; as this expansion is much smaller than that required to produce a cloud on ions, there must be particles much larger than molecules in the neighbourhood of the wire. Unless the wire is very carefully cleaned an increase of temperature much less than that required to produce luminosity is sufficient to produce a cloud. This depends apparently upon dirt or moisture deposited on the wire, and Aitken's experiments show that this effect disappears when the wire has been cleaned by long-continued incandescence; no amount of incandescence seems however to destroy the cloud when the temperature of the platinum wire is raised to that corresponding to a red heat. Mr Owen, who has recently made experiments in the Cavendish Laboratory on this point, finds that when the platinum wire is in air or oxygen there is, even after long-continued incandescence of the wire, always a cloud when the temperature of the wire is raised to about 300° C. In pure hydrogen however the wire has to be raised nearly to a red heat before this cloud is formed.

104. There is a close similarity between the laws of disintegration of the wire and those of the leak of positive electricity from it. We have already alluded to the effect of long-continued heating on the leak: the presence of oxygen has also a very marked effect. This can be shown in a striking way by observing the pressure at which a plate in the neighbourhood of the hot wire begins to acquire a negative instead of a positive charge. If the wire be not too hot, then at high pressures the plate will be charged positively; on exhausting the vessel a point will be reached where the positive charge begins to decrease, then vanishes and finally is replaced by a negative charge. This change in the sign of the charge on the plate occurs at much higher pressures in hydrogen and nitrogen than in oxygen, where this reversal is difficult to obtain unless the wire be very hot. When the reversal of sign has been obtained in hydrogen or nitrogen the addition of a surprisingly small quantity of oxygen is sufficient to make the charge on the plate positive again. It is possible that part of the diminution in the positive leak produced by long-continued heating at low pressures may be due to the burning up of the oxygen, or when there is any grease present to the replacement of oxygen by the vapours of hydrocarbons liberated by the continuous heating. The increase in the positive electrification produced by oxygen is easily explained if there is any oxidation of the metal at a red heat; for in the oxide thus formed the oxygen carries the negative, the metal the positive charge; thus if the oxygen in the neighbourhood of the platinum wire got ionised by the heat, the platinum by combining with the negative but not with the positive oxygen ions would leave an excess of positive ions in the neighbourhood. That chemical action has a considerable effect on the electrification is confirmed by the observation of Branly that the oxides of metals give off at a dull red heat negative electricity, whereas metals give off positive; in the case of the oxides the chemical action which takes place is the dissociation of the oxide into the metal and oxygen, the oxygen ions carrying the negative charge and thus producing negative electrification round the wire. A similar explanation applies to the following result which I observed with the arc discharge; when the arc passed between terminals of bright copper there was an excess of positive electricity in the gas round the terminals; if however the terminals were thickly coated with oxide and placed in hydrogen the electrification in the gas was negative until the oxide was reduced: when this had been accomplished the electrification became positive.

105. A very small amount of chemical action is sufficient to produce very intense electrification, so that it might be urged that even in the best attainable vacuum there is sufficient gas to produce the electrification; that this positive electrification occurs in very good vacua is certain; in a vacuum so good that it was hardly possible to get any discharge through it with an induction coil giving an 8-inch spark, I have got the positive electrification from a red-hot platinum wire which had been kept glowing at a much higher temperature 8 hours a day for a week. Stronger evidence that the positive electrification is not due entirely to chemical action on the wire is afforded by a determination of the nature of the carriers of this charge; if the charge arose from chemical action we should expect the carriers to be the atoms or molecules of the gas. The following experiments show that although there are a few carriers of this character the majority

of them are much larger and are probably molecules, or even larger masses, of platinum. The method used to determine the mass of the carriers was the same as that used (see p. 106) to determine the mass of the negative carriers at high temperatures, inasmuch however as the mass of the positive carriers turns out to be enormously greater than that of the negative ones, it is necessary in dealing with the positive leak to employ very much greater magnetic forces than those used in the previous experiments, and this involves some modifications in the conditions of the experiment. The arrangement used is shown in Fig. 46.



A is an insulated metal plate placed in the middle of a brass tube about 5 mm. in diameter; this plate is connected with a quadrant electrometer. B is a piece of platinum foil parallel to the plate and about 3 mm. from it; this foil can be raised to incandescence by an alternating electric current passing through the leads C, D. The current was produced by making the circuit connecting the leads loop round a transformer. By this method the hot wire and its leads could be easily insulated; the hot wire and the brass tube were connected with one terminal of a battery of small storage cells, the other terminal of which was connected with the earth. The current to the plate A from the hot wire was measured by the deflection produced in the electrometer in a given time; this deflection was measured for various potentials of the hot wire, with the magnetic field both on and off; the highest potential at which a given magnetic field produces an appreciable diminution gives, as is explained in Art. 48, the means of determining m/e—the ratio of the mass of the carrier to its charge. In the investigation of Art. 48 it was assumed that the electric force was uniform in the region in which the ions were moving; in the case of the hot wire there are so many ions all of one sign carrying the current that they disturb the potential gradient and make the force vary from point to point. We can easily prove however that this inequality in the electric field will not impair the validity of the method. If the field is not uniform the paths of the ions will not be cycloids; the ions however whether the field is uniform or not, after receding a certain distance d from their source, will be turned round by the magnetic force and begin to move back, thus they will never get further than d away from the source. Now if the plate on which the ions are received is at a distance greater than d from the hot metal which is the source of the ions, the magnetic field will produce a diminution in the current flowing into the plate, while if the distance is less than d, the magnetic field will produce no diminution in the leak. This critical distance d can be determined by comparing the currents with the magnetic field on and off: it is evidently the distance from the source at which the velocity of the ion parallel to the electric force vanishes. If x is the distance of an ion from the hot plate, X the electric force acting on the ion, H the magnetic force supposed to be uniform and parallel to the axis of z, then we have

$$m \frac{d^2x}{dt^2} = Xe + He \frac{dy}{dt} \qquad .....(1),$$

$$m \frac{d^2y}{dt^2} = -He \frac{dx}{dt} \qquad .....(2)$$

$$m \frac{dy}{dt} = -Hex,$$

or

since  $\frac{dy}{dt} = 0$ , when x = 0; substituting this value for  $\frac{dy}{dt}$  in

equation (1) we get

$$m\frac{d^2x}{dt^2} + \frac{H^2e^2}{m} x = Xe.$$

Integrating with respect to x from x = 0 to x = d, we have since dx/dt vanishes both when x = 0 and when x = d

$${\textstyle \frac{1}{2}} \frac{H^2 e^2 d^2}{m} = e \int_0^d \ X dx \, ;$$

if V is the difference of potential between the plates  $V = \int_0^d X dx$ ;

hence 
$$\frac{1}{2} \frac{H^2 e}{m} d^2 = V$$
 or 
$$\frac{e}{m} = \frac{2V}{H^2 d^2} \dots (3),$$

and thus even when the field is not uniform e/m is given by the same equation as in Art. 48.

In applying this method to the case of the leaking of positive electricity from a hot wire we find that enormously greater magnetic forces are necessary to produce any diminution upon the leak than were required to produce the same effect on the leak of negative electricity from a hot wire (see p. 164): and even with the greatest magnetic forces obtainable the effects of the magnetic field upon the rate of leak are sometimes scarcely appreciable. The effect of a magnetic field upon the positive leak like the positive leak itself is irregular, even when the temperature of the wire and the pressure of the gas are kept as constant as possible, small changes in conditions which it is very difficult to control or even to specify producing great changes in the leak and in the effect of the magnetic field upon it. It is probable that these changes correspond to a change in the nature of the carriers of the electricity. In some cases the leak is not affected by the magnetic field even of 19000 units. When, however, the discharge is sensitive to the magnetic field the general nature of the effects observed with the apparatus already described and with a field of 19000 units is as follows, the pressure of the gas (air) being about '007 mm.; the numbers given are only approximate as the irregular variations in the leak are so large as to make accurate measurement impossible. When the potential difference between the hot metal and the plate connected with the electrometer was small, say 3 or 4 volts, the leak was very nearly stopped by the magnetic field; with a potential difference of 10 volts the leak was reduced by the magnetic field to about one-quarter of its original value, the effect of the magnetic force upon the leak diminished as the potential difference increased but was appreciable until this reached about 120 volts. Thus in this case we see that while some of the carriers can reach the plate under a difference of potential of 10 volts, there are others which require a potential difference

of 120 volts to do so. If  $e_1/m_1$  be the ratio of the charge to the mass of the first carrier,  $e_2/m_2$  that of the second, then putting in equation (3)

H = 19000, d = 3 and  $V = 10 \times 10^{8}$  and  $120 \times 10^{8}$ , we get

$$\frac{e_1}{m_1} = 60,$$

$$\frac{e_2}{m_2} = 720$$
;

if  $e_1$ ,  $e_2$  were the same as the charge on a hydrogen ion, then  $m_1$  and  $m_2$  would be respectively about 170 and 14 times the mass of the hydrogen atom; these are limiting values of e/m, there are also intermediate values. These results indicate that the electricity is carried both by atoms of the metal (in this case platinum) and of the gas, the former predominating. The fact that in certain cases the rate of leak is not affected by the magnetic force even when the potential difference is reduced to one volt or less shows that in these cases the carriers have much larger mass than the molecule of platinum, they are probably platinum dust.

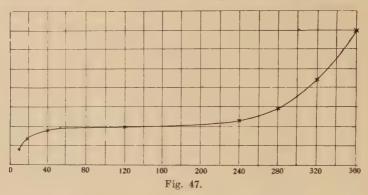
Rutherford\* from experiments on the velocity of the ions through air at atmospheric pressure also came to the conclusion that carriers of very different kinds were at work in carrying the positive electricity from a hot metal.

Though the effect of the magnetic field on the rate of leak diminishes when the potential difference is increased and at one stage disappears, yet on still further increasing the potential a stage is reached where the magnetic force again produces a very considerable diminution in the rate of leak. This stage is closely connected with the way in which the rate of leak varies with potential difference; if we represent the rate of leak by the ordinates, the potential difference by the abscissæ of a point on a curve, then as McClelland† has shown, the curve is of the type represented in Fig. 47 showing three well-marked stages: in the first the current increases rapidly with the potential difference, in the second the current is saturated and is independent of the potential difference, in the third stage the current again increases rapidly. This increase is as we shall see due to the formation of fresh ions by the motion through the gas of ions coming from the hot plate,

<sup>\*</sup> Rutherford, Physical Review, xiii. p. 321, 1901.

<sup>†</sup> McClelland, Proc. Camb. Phil. Soc. xi. p. 296, 1902.

there are in this stage negative as well as positive ions between the electrodes. It is in the third stage that the magnetic field



again produces a diminution in the rate of leak, the explanation of this is I think that the magnet stops the motion of the *negative* ions which are now helping to carry the current and which as we have seen are very much hampered by a magnetic field.

Elster and Geitel\* found that the rate of positive leak was often, indeed in their experiments generally, increased, not diminished, by the magnetic field; with the apparatus described and arranged as on page 182, I only observed an increase in one case, i.e. when the temperature was high and the potential difference small. At a very high temperature negative as well as positive ions are produced at the plate, these negative ions are projected with great velocity so that even if the plate has a small positive charge the negative ions coming from the plate will exceed the positive ones and a conductor in the neighbourhood will receive a negative charge. If the potential of the plate be raised until this conductor gets a positive charge, then the application of a magnetic field will often considerably increase the positive charge on the conductor; this increase is, however, due to the retardation of the stream of negative ions and not to the acceleration of the positive ones. the metal tube in which the hot plate (Fig. 46) is contained is not connected with the hot plate but with the earth, then a magnetic field will often increase the rate at which the plate acquires a positive charge; this, however, is merely the diversion of positive ions from the tube to the cold plate by the magnetic field.

<sup>\*</sup> Elster and Geitel, Wied. Ann. xxxviii. p. 27, 1889.

106. We could determine the value of e/m for the carriers of electricity by the following method, which is applicable when the current is carried by ions of one sign and when the pressure of the gas is so low that we can neglect the resistance of the gas to the motion of the ions. Let us consider the case of a current between two parallel plates, one of which is the hot plate or other source of ions. Take the axis of x at right angles to the plate, let V be the difference of potential between the hot plate and a point whose coordinate is x,  $\rho$  the density of the electricity. Then

$$\frac{d^2V}{dx^2} = -4\pi\rho \dots (1).$$

If v be the velocity of the ion at x,  $v_0$  its velocity when starting from the plate, m its mass and e its charge, then

$$\frac{1}{2} m (v^2 - v_0^2) = Ve$$
 .....(2);

but since all the ions are of one sign, i the current through unit area is equal to  $v\rho$ , hence from (1) and (2)

$$\left(v_0^2 + \frac{2e}{m}V\right)\left(\frac{d^2V}{dx^2}\right)^2 = 16\pi^2i^2...(3);$$

integrating this equation we have, if we write X for dV/dx,

$$X^2 = C + \frac{8\pi i.m}{e} \left\{ v_0^2 + \frac{2e}{m} V \right\}^{\frac{1}{2}};$$

hence if X is the value at the cold plate,  $X_0$  that at the hot, V the potential difference between the plates, and C the constant of integration,

we have

$$X^{2} - X_{0}^{2} = \frac{8\pi i \cdot m}{e} \left[ \left\{ v_{0}^{2} + \frac{2e}{m} V \right\}^{\frac{1}{2}} - v_{0} \right];$$

if X' and  $X_0'$ , i' and V' are corresponding values in a second experiment we have

$$X'^{2} - X_{0}^{'2} = \frac{8\pi i' \cdot m}{e} \left[ \left\{ v_{0}^{2} + \frac{2e}{m} V' \right\}^{\frac{1}{2}} - v_{0} \right];$$
hence if 
$$(X^{2} - X_{0}^{2}) / 8\pi i = \xi, \quad (X'^{2} - X_{0}^{'2}) / 8\pi i' = \xi',$$
we have 
$$\frac{e^{2}}{m^{2}} \xi^{2} + 2v_{0} \frac{e}{m} \xi = \frac{2e}{m} V,$$

$$\frac{e^{2}}{m^{2}} \xi'^{2} + 2v_{0} \frac{e}{m} \xi' = \frac{2e}{m} V',$$

$$\frac{e}{m} \xi \xi' (\xi - \xi') = 2 (V \xi' - V' \xi) \dots (4),$$

an equation by which we can determine e/m when we know  $\xi$ ,  $\xi'$ , V, and V'. To determine  $\xi$  and  $\xi'$  we require to know the value of X at the two plates. This can be done as follows: as the pressure is very low we can produce by independent electrodes cathode rays in the vessel in which the leak is taking place; if we arrange these electrodes so as to allow a small pencil of these rays to pass close to first one plate and then the other and measure the electrostatic deflection of the rays, we can from this deflection deduce the electric force and then by equation (4) the value of e/m.

# Effect of the Gas on the rate of leak.

107. We have seen that in the best vacua we can produce a metal when first it begins to glow gives off positive electricity and then at considerably higher temperatures negative electricity as well, the rate of emission of negative electricity increasing more rapidly with the temperature than that of the positive, so that at very high temperatures the negative is greatly in excess of the positive. Thus to make a metal emit positive electricity we have to communicate a certain amount of energy to its surface, a larger amount being required to make it give out negative electricity. When the incandescent metal is surrounded by gas at an appreciable pressure we find that the nature of the gas has a very distinct effect upon the amount of leak. The author\* has shown that gases such as the vapours of iodine and bromine, chlorine, hydriodic acid gas, hydrobromic acid gas, hydrochloric acid gas, the vapours of potassium iodide, sal-ammoniac, sodium chloride. potassium chloride, which are dissociated by heat conduct electricity on quite a different scale from those which like air, hydrogen or nitrogen do not suffer any dissociation; thus the dissociable gases furnish a much larger supply of ions than the others: even in these easily dissociable gases by far the greater part of the dissociation occurs where the gas is in contact with the glowing electrodes; this is proved by the experiment described on page 172.

The vapours of many metals conduct very well; of the metals I tried, sodium, potassium, thallium, cadmium, bismuth, lead, alumi-

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 29, pp. 358, 441, 1890.

nium, magnesium, tin, zinc, silver and mercury; sodium and potassium had the highest conductivity; while the conductivity of the vapours of mercury, tin, thallium, did not seem any greater than that of air; so that the small conductivity actually observed might have been due to the presence of air and not to the vapour of the metal.

Application of the leak through hot gases to determine the amount of work required to ionise a gas.

108. By measuring the current through a gas we can determine the number of ions in unit volume if we know the velocity of the ions under a given electric field: for if  $R_1$  and  $R_2$  are the velocities under unit electric force of the positive and negative ions respectively, n the number of ions (of either sign) per cubic centimetre,  $\iota$  the current under the electric force X, then

$$\iota = n (R_1 + R_2) eX.$$

If these ions come from the gas we may regard the molecules of the gas as dissociating into positive and negative ions and these recombining to form neutral molecules; the problem of finding the proportion between the number of ions and the number of neutral molecules is the same as that of finding the proportion between the atoms and molecules in a gas which is dissociating. This problem has been solved and an expression found for the way in which the number of free atoms depends upon the temperature (see Willard Gibbs, Equilibrium of Heterogeneous Substances, p. 239; Boltzmann, Wied. Ann. XXII. p. 39; J. J. Thomson, Applications of Dynamics to Physics and Chemistry, p. 193). When the number of free ions is small compared with the number of neutral molecules—as it is in the case of the ionisation of a gas by heat, then if n is the number of ions per unit volume

$$n^{2} = p \phi (\theta) e^{-\frac{w}{R\theta}},$$

where p is the pressure of the neutral molecules,  $\theta$  the absolute temperature, w the work required to ionise one gramme of the molecules of the gas, R is the constant which occurs in the equation  $p = R\rho\theta$  for the neutral gas,  $\rho$  being the density of the gas,  $\phi(\theta)$  is a function of  $\theta$  which does not change rapidly with the temperature, so that when the number of ions changes very rapidly

with the temperature as it does in the case of conduction through hot gases the variation in n is chiefly due to the factor  $e^{-\frac{w}{R\theta}}$ .

Hence if  $n_1$ ,  $n_2$  are the numbers of free ions at the temperatures  $\theta_1$  and  $\theta_2$  respectively, we have approximately, regarding  $\phi(\theta)$  and w as constant,

$$\log \frac{n_2^2}{n_1^2} = \frac{w}{R} \left\{ \frac{1}{\theta_1} - \frac{1}{\theta_2} \right\};$$

hence if we determine  $n_2/n_1$  by measuring the current through the hot gas we can find w. By this method H. A. Wilson\* found that for air it required about 2100 calories to ionise one gramme of air. As the ionisation of a gas consists in the separation of positive and negative charges it is natural to express the work required to effect this process as due to the movement of the charge on the ion through a certain difference of potential. If V is this potential difference, e the charge on an ion, n the number of molecules in a gramme of air, m the mass of a molecule, we have

 $neV = 2100 \text{ calories} = 2100 \times 4.2 \times 10^7 \text{ ergs}; nm = 1;$ 

hence

$$\frac{e}{m} V = 2.1 \times 4.2 \times 10^{10};$$

for hydrogen  $e/M=10^4$  if M is the mass of an atom of hydrogen; hence if the charge on the ion is the same as that on hydrogen we have for air  $e/m=10^4/28$ , hence

$$V = 2.5 \times 10^8 = 2.5 \text{ volts.}$$

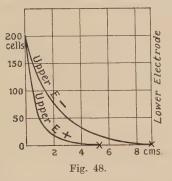
Thus the work done in ionising a molecule of air corresponds to moving the charges through about 2.5 volts.

The distribution of potential near Glowing Electrodes.

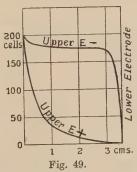
109. We shall confine ourselves to the case when the current is passing between two parallel plane electrodes. If one of these be hot and the other cold—too cold to produce any ionisation at its surface—the current will be carried entirely by ions of one sign, the electric force will therefore increase continuously from the hot plate to the cold one, and (see Art. 101) the distribution of potential will be represented by a curve similar to that in Fig. 48, the lower electrode being the hotter of the two. Similar curves will represent the distribution of potential when

<sup>\*</sup> H. A. Wilson, Phil. Trans. A. 197, p. 415, 1901.

both plates are hot provided the temperature of the negative plate is not high enough for negative as well as positive ions to be produced at the plate, for it is evident that in this case the current has to be carried entirely by positive ions. When however both



plates are hot enough to ionise the gas and the negative so hot that negative as well as positive ions are produced, then when the field is so strong that most of the positive ions are driven from the positive plate and the negative ions from the negative plate, we shall have an excess of positive ions at the negative plate, so that in the region the potential curve will be concave, and of negative ions at the positive, which will make the potential curve convex, and the potential curve will be like the higher curve in Fig. 49,



the straight part in the middle showing that except close to the plates there are approximately equal numbers of positive and negative ions present. Curves similar to these for the distribution of potential have been obtained by H. A. Wilson\* and Marx†.

When the hot plates are made of different materials Pettinelli

<sup>\*</sup> H. A. Wilson, Phil. Trans. A. 192, p. 499, 1899.

<sup>†</sup> Marx, Drude's Ann. ii. p. 768, 1900.

and Marolli\* have shown that the magnitude of the current depends upon which metal is used as the cathode, thus with electrodes of carbon and iron the current when the carbon was cathode was three or four times greater than when the iron was cathode: they state that the current is greatest where the more porous substance is used as the cathode. These effects are much more marked at high than at low temperatures; it is probable that they do not commence until the temperature is high enough to produce negative ions.

The difference in the velocities of the ions produces very marked unipolar effects in the current, i.e. the current with the same electromotive force is very much greater in one direction than the opposite; we can very easily see the reason for this, for take the case where only one electrode is hot enough to ionise the gas, then we see from equation (1), p. 195 that the current is proportional to the velocity under unit force of the ion carrying the current. As the velocity of the negative ion is greater than that of the positive, the current will be greater when it is carried by the negative ions than when it is carried by the positive. It must be remembered that the ratio of the velocities of the ions produced by an incandescent metal depends very largely upon the temperature. Thus McClelland+ who measured it in air at the ordinary temperature (the ions having been blown from the incandescent wire to the place of observation), found that the velocity of the negative ions was only about 25 per cent. greater than that of the positive, while H. A. Wilson, who measured this ratio at high temperatures for the ions produced when salts were volatilised in flames or hot air, found that at 1000° C. the velocity of the negative ion was for the salts of the alkali metals 3.6 and for those of the alkali earths 7 times that of the positive. At 2000°C. the velocity of the negative ions was for the alkali metals seventeen times that of the positive. The absolute values were still more different, thus McClelland found for the velocity under a potential gradient of a volt per cm. velocities ranging from ·006 cm./sec. to ·03 cm./sec., while Wilson at 1000° C. found 26 cm./sec. for the negative, and 7.2 cm./sec. for the positive; at 2000° C. the values were respectively 1030 cm./sec. and 62 cm./sec.

<sup>\*</sup> Pettinelli and Marolli, Atti della Accad. dei Lincei, v. p. 136, 1896.

<sup>†</sup> McClelland, Proc. Camb. Phil. Soc. x. p. 241, 1899.

<sup>‡</sup> H. A. Wilson, Phil. Trans. A. 192, p. 499, 1899.

### CHAPTER IX.

#### IONISATION IN GASES FROM FLAMES.

110. It has been known for more than a century that gases from flames are conductors of electricity: a well-known application of this fact—the discharge of electricity from the surface of a non-conductor by passing a flame over it—was used by Volta in his experiments on Contact Electricity. We shall not attempt to give any historical account of the earlier experiments on this subject, because the conditions in these experiments were generally such that the interpretation of the results obtained is always exceedingly difficult and often ambiguous: the reason of this is very obvious—to investigate the electrical conditions of the flame wires are generally introduced, these become incandescent and so at once add to the electrical phenomena in the flame the very complicated effects we have been discussing in the last chapter.

The gases which come from the flame, even when they have got some distance away from it and have been cooled by the surrounding air, possess for some time considerable conductivity, and will discharge an insulated conductor placed within their reach. The conductivity can be entirely taken out of the gas by making it pass through a strong electric field, this field abstracts the ions from the gas, driving them against the electrodes so that when the gas emerges from the field, although its chemical composition is unaltered its conducting power is gone. This result shows too that no uncharged radio-active substances, such as emanate from thorium and some other substances, are produced in the flame, these would not be taken out by the field so that if they existed the conductivity of the gas would not be destroyed by the field. If not driven out of the gas by an electric field the ions are fairly long lived. Thus in some experiments Giese

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noticed that the gas retained appreciable conductivity 6 or 7 minutes after it had left the flame. The ions stick to any dust there may be in the air and then move very slowly so that their rate of recombination becomes exceedingly slow. McClelland\* has shown that the velocity of the ions under a given electric force decreases very much as they recede from the flame; thus close to the flame the velocity under the force of a volt per centimetre was '23 cm./sec., while some distance away from it the velocity was only '04 cm./sec.

In order that a conductor should be discharged by a flame it is not necessary that it should be placed where the gases from the flame would naturally strike it—thus for example it will be discharged if placed underneath a Bunsen flame. The explanation of this is that the electric field due to the charged conductor drags out of the flame and up to the conductor ions of opposite sign to the charge.

This ionised gas is produced by flames of coal gas whether luminous or not, by the oxy-hydrogen flame, by the alcohol flame of a spirit lamp, by a flame of carbonic oxide; it is not however produced in very low temperature flames such as the pale lambent flame of ether. Thus to produce the ionised gas high temperature as well as chemical combination is required. That chemical combination alone is insufficient to produce ionisation is shown by the case of hydrogen and chlorine which do not conduct even when combining under ultra-violet light. Braun; has shown that in the explosive wave produced in the combination of certain gases there is ionisation, but in this case there is also very high temperature.

In the coal gas flame the part where the gas comes in contact with the air and where there is most combustion is positively electrified, while the interior of the flame is negatively electrified, this accounts for the effect produced by holding a negatively electrified body near the flame, the luminous part turns to the negative body, and if this is near stretches out until it comes into contact with it; if the flame be placed between two

<sup>\*</sup> McClelland, Phil. Mag. v. 46, p. 29, 1898.

<sup>+</sup> J. J. Thomson, Proc. Camb. Phil. Soc. xi. p. 90, 1901.

<sup>‡</sup> Braun, Zeitschrift für Physikalische Chemie, xiii. p. 155, 1894.

oppositely charged plates the bright outer portion of the flame is attracted towards the negative plate while the inner portion moves, but less markedly, towards the positive plate. This effect is illustrated by Fig. 50 taken from a paper by Neureneuf\*; in

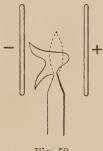


Fig. 50.

some experiments made by Holtz<sup>†</sup>, one of which is figured in Fig. 51, the flame was divided by the electric field between the

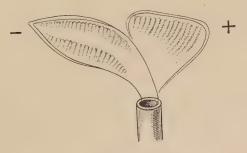


Fig. 51.

plates into two sheets; the reader will find many other interesting experiments on the effect of an electric field on the shape of flames in the papers by Neureneuf and Holtz. It appears from these results that in the bright portion of the flame where combustion is taking place there is an excess of positive electricity, while in the unburnt coal gas there is an excess of negative, a fact discovered a long time ago by Pouillet‡. If the hydrogen and oxygen were ionised by the heat, then since negative ions of oxygen combine with positive ions of hydrogen to form water, the

<sup>\*</sup> Neureneuf, Annales de Chim. et de Phys. v. 2, p. 473, 1874.

<sup>†</sup> Holtz, Carl Répert. xvii. p. 269, 1881.

<sup>‡</sup> Pouillet, Ann. de Chim. et de Phys. xxxv. p. 410, 1827.

negative oxygen ions and the positive hydrogen ones would get used up, and there would be an excess of positive electricity in the oxygen and of negative in the hydrogen. It is possible too that at a temperature corresponding to that of vivid incandescence in a solid the molecules of a gas may like those of a solid give out the negative corpuscles, on this account there would be a tendency for the hotter parts of the flame to be positively the colder negatively electrified. When as in luminous flames we have small particles of solid carbon raised to the temperature of vivid incandescence the electrical effects are complicated by those due to incandescent solids which as we have seen in the last chapter are very considerable.

When two wires connected together through a sensitive galvanometer are placed in different parts of the flame currents flow through the galvanometer; suppose one of the wires is placed in the cool inner portion of the flame where there is an excess of negative electricity, while the other wire is placed at the outside of the flame where there is an excess of positive electricity there will, neglecting any ionisation due to the wire, be a current from the hot outer portion of the flame to the cool inner portion through the galvanometer: the wire in the outer portion will however certainly be raised to incandescence if its temperature keeps so low that only positive ions are produced at its surface, then there will on this account be a current of electricity from the hot to the cool part of the flame through the flame and thus in the opposite direction to the previous current. If however the wire got so hot that it emitted more negative than positive ions the effect of the incandescence of the wires would be to increase instead of diminishing the current due to the flame itself. Thus we see that these currents will vary in a complex way with the temperature. For an account of the currents which can thus be tapped from a flame and for other electrical properties of flames we must refer the reader to the papers of Erman\*, Hankel†, Hittorf‡, Braun§, Herwig|, and

<sup>\*</sup> Erman, Gilbert. Ann. xi. p. 150, 1802; xxii. p. 14, 1806.

<sup>†</sup> Hankel, *Pogg. Ann.* lxxxi. p. 213, 1850; cviii. p. 146, 1859.

<sup>†</sup> Hittorf, Pogg. Ann. exxxvi. p. 197, 1869; Jubelbd. p. 430, 1874.

<sup>§</sup> Braun, Pogg. Ann. cliv. p. 481, 1875.

<sup>||</sup> Herwig, Wied. Ann. i. p. 516, 1877.

especially of Giese\*, who was the first to suggest that the conduction of electricity through flames and hot gases was due to the motion of charged ions distributed through the gases: there is a very complete account of these researches in Wiedemann's *Elektricität*, bd. IV. B, chap. 4.

### Conductivity of Gases containing Salt Vapours.

111. When the vapours of salts are introduced into a flame the conductivity between metallic terminals is very greatly increased, and the electrical properties are simpler and more regular than in pure flames; the laws of the flow of electricity through these salt-laden flames have been investigated by Arrhenius† and H. A. Wilson<sup>†</sup>. The method—devised by Arrhenius and adopted by Wilson-of introducing the salt into the flame was as follows: a dilute solution of the salt was sprayed into exceedingly fine drops by a Gouy sprayer, the spray got well mixed with the coal gas on its way to the burner, and in the flame the water evaporated and the salt vaporised. The amount of salt supplied to the flame in unit time was estimated by determining the rate at which a bead of salt introduced into an equal and similar flame so as to produce the same coloration as that produced by the spray in the original flame burnt away. The salts used were chiefly the haloid and oxy-salts of the alkali metals and earths. The conductivity due to the salt was determined by subtracting from the current observed when the salt was in the flame the current with the same electromotive force in the pure flame. It was found that when the concentration of the solutions is small, equivalent solutions § of all salts of the same metal impart the same conductivity to the flame. With large concentration this is no longer the case, the oxy-salts giving greater conductivity than the haloid salts. According to Arrhenius all the salts in the flame are converted into hydroxides, so that whatever salts are used, the metal in the flame always occurs in the same salts. The relation between the current and the electro-

<sup>\*</sup> Giese, Wied. Ann. xvii. pp. 1, 236, 519, 1882; xxxviii. p. 403, 1889.

<sup>+</sup> Arrhenius, Wied. Ann. xlii. p. 18, 1891.

<sup>‡</sup> H. A. Wilson, Phil. Trans. A. 192, p. 499, 1899.

<sup>§</sup> Equivalent solutions are those in which the weight of salt per litre is proportional to the molecular weight of the salt.

motive force is represented by Fig. 52 taken from Wilson's paper: we see that the curves resemble in many respects those given in

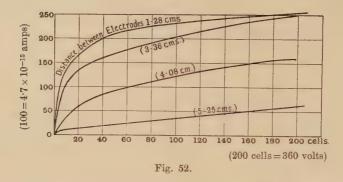


Fig. 4, which represent this relation for the typical ionised gas. There is one well marked difference, however, in the typical curve. the straight part is horizontal, i.e. the current does not increase at all with the electromotive force; in the case of the salt vapour the straight part is inclined at a finite angle to the horizontal, indicating a slow but steady increase of the current with the electromotive force. The cause of this difference between the normal curves and the curve for the flame is I think that in the latter case the ionisation takes place mainly at the surface of the electrodes (for the proof of this see p. 172). We have thus two sources of supply for the ions, so that to 'saturate' the current we must use up all the ions from both sources, i.e. all the negative ions produced at the negative electrode, and all the positive ions at the positive electrode must be sent into the gas and used to carry the current. Now as we shall see the velocity of the negative ions in flames containing salt vapours is very much greater than that of the positive, so that the negative ions will be much more easily detached from the negative electrode than the slowly moving positive ions from the positive electrode: thus we shall exhaust the supply of the negative ions long before we do that of the positive. If all the current were carried by the negative ions it would be saturated as soon as the supply of these was exhausted; in practice a small but appreciable fraction of the current is carried by the positive ions, so that after the supply of negative ions is exhausted the current will go on slowly increasing for a long range of potential difference until finally the supply of positive ions is exhausted, and then and not till then the current will become independent of the potential difference between the electrodes. The difference between the field required to drive all the ions from the negative and positive electrodes is well illustrated by an experiment of Wilson's, in which only one of the electrodes was hot, the other was too cold to give rise to any ionisation; in this case when the hot electrode was negative the current was saturated with a comparatively small potential difference, while it required an exceedingly large potential difference to saturate the current when the hot electrode was positive.

Another proof in addition to those given on p. 172 that the ionisation at the electrodes is greater than in the body of the gas is afforded by experiments made with the electrodes at different distances apart. If the greater part of the ionisation took place in the body of the gas the saturation current would be proportional to the distance between the electrodes. In the case of conduction through flames containing vapours of salts Wilson has shown that the saturation current is very approximately independent of the distance between the electrodes.

112. The conductivity given to the flame by the salts of the different alkali metals under the same condition as to temperature, potential difference and concentration. The Caesium salts conduct the best, and then follow in order the salts of Rubidium, Potassium, Sodium, Lithium, and Hydrogen. The order of the conductivities is thus the same as that of the atomic weights of the metals, and the difference between the metals is very large, as is shown by the following table given by H. A. Wilson:

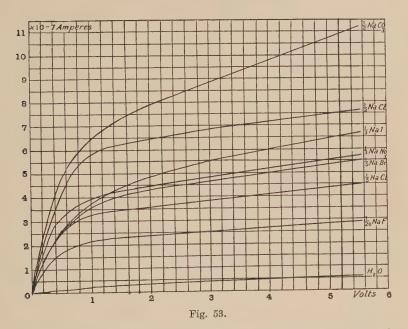
	Chlorides.			Nitrates.		
Potential Difference	5.60	•795	•237	5.60	•795	·237
	Current			Current		
Caesium	123	60.5	22.2	303	115	36.6
Rubidium	41.4	26.4	11.3	213	82.4	25.9
Potassium	21.0	13.4	5.75	68.4	29.3	9.35
Sodium	3.49	2.45	1.15	3.88	2.67	1.32
Lithium	1.29	-87	-41	1.47	•99	•53
Hydrogen	.75		.27			

On the Variation of Conductivity with the strength of the Solution.

113. Arrhenius came to the conclusion that, using the same salt, the conductivity was proportional to the square root of the concentration, while H. A. Wilson considered that the application of this simple law was restricted in the case of the oxy-salts to extremely dilute solutions, and that although the range of its application was more extended in the case of the haloid salts, the agreement was only approximate. If we refer to the general theory of conduction through an ionised gas (see page 68) we find that the conductivity when the current is far from saturation is proportional to  $q^{\frac{1}{2}}$ , where q is the number of ions produced per second in a cubic centimetre of the gas. In the case of the salt vapour q will be proportional to the number of molecules of salt in a cubic centimetre of the gas, and will thus be proportional to the strength of the solution. This result is derived from the study of the case when ionisation takes place throughout the volume of the gas; it will however be applicable in its main features to the case when the ionisation only takes place near the surface of the electrodes, provided the thickness of the layers in which the ionisation occurs is large compared with the average distance between the molecules of the salt, and that the distribution of potential between the electrodes is not affected by the concentration of the salt; this second supposition is probably not true. The above reasoning only applies to the case when the current is far from the saturation value; when it approaches this value the current is proportional to q and not to  $q^{\frac{1}{2}}$ ; thus we should expect that in the case of currents through flames under large electromotive forces Arrhenius' law would cease to be true. and the current would be proportional to the concentration. Inspection of the curves given in Fig. 53 taken from a paper by Smithells, Dawson and Wilson\* will show that the variations of the current with the strength of the solution, even when the current is well past the knee of the curve representing the relation between current and potential difference, are much less than they would be if they varied directly as the concentration; in fact, even in this stage they are much more nearly proportional to the square root than to the first power of the concentration. This

<sup>\*</sup> Smithells, Dawson and Wilson, Phil. Trans. A. 193, p. 89, 1900.

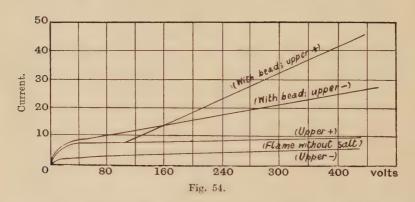
effect is rather difficult to account for. May it be due to the thickness of the layer through which the ionisation extends depending to some extent on the concentration? This would be



the case if the ionisation were produced by radiation or corpuscles proceeding from the electrodes, the absorption of the radiation being due in whole or in part to the work done in ionising the salt; for consider the extreme case where the absorption is wholly due to the ionisation of the salt, then if the absorption were great enough to stop the radiation from one electrode before it reached the other, the amount of ionisation, and therefore the saturation current, would be independent of the concentration; with large concentrations the ionisation would be confined to a thin layer near the electrodes, with small concentrations this layer would be thicker, but the total amount of ionisation would be the same in the two cases. If the radiation was not completely absorbed in the space between the electrodes the amount of ionisation would increase with the concentration, but its rate of increase would be slower than that of the concentration. Wilson has shown (see p. 210) that at very high temperatures the saturation current is proportional to the concentration.

## Velocity of the Ions.

114. The velocity of the ions in flames containing salt vapours has been determined by H. A. Wilson\*, who used a method of which the principle is as follows. Suppose that in a flame we have two electrodes one vertically over the other, and that we introduce a bead of salt just underneath the upper electrode, the vapour from this bead will be carried along by the upward rush of gases in the flame, and unless the ions in the salt vapour are driven downwards by the electric field between the electrodes, none of them will reach the lower electrode. If however the ions from the salt do not reach the electrode the current between the electrodes will be unaffected by the presence of the salt. when the potential difference between the electrodes is small the current will not be increased by the introduction of the salt, but as soon as the electric force between the electrodes is sufficient to drive one of the ions against the blast in the flame, the current will be increased by the bead of salt. This is illustrated by the curve in Fig. 54 taken from Wilson's paper; we see that when



the upper electrode was positive the current was not increased by the bead until the potential difference between the electrodes was about 100 volts, while for greater differences of potential the bead produced a substantial increase in the current. Thus when there was a difference of 100 volts between the electrodes, the smallest electric force in the space traversed by the ion must be just

<sup>\*</sup> H. A. Wilson, Phil. Trans. A. 192, p. 499, 1899.

sufficient to give to the positive ion a downward velocity equal to the upward velocity of the gas in the flame. Since the electric field is not uniform between the electrodes (see p. 191), it is necessary to measure the distribution of potential between the electrodes in order to determine the minimum electric force; when this and the upward velocity of the gas in the flame are known we can determine the velocity of the ions in a flame under a given electric force. By this and similar methods Wilson deduced the following values for the velocities of the ions under an electric force of a volt per centimetre.

In a flame whose temperature was estimated to be about 2000° C., the velocity of the negative ion, whatever salts were put in the flame, was about 1000 cm./sec.

The velocities of the positive ions of salts of Caesium, Rubidium, Potassium, Sodium, and Lithium were all equal, and were about 62 cm./sec.

In a stream of hot air whose temperature was estimated at 1000° C. the following results were obtained for the velocities under a potential gradient of 1 volt per cm.

Negative ions ... ... ... ... ... 26 cm./sec. Positive ions of salts of Li, Na, K, Rb, and Cs 7·2 cm./sec. Positive ions of salts of Ba, Sr, and Ca ... 3·8 cm./sec.

The absolute numbers must be regarded as only approximately true, the relative values are probably much more accurate.

The velocities are very much less at 1000° C. than they are at 2000° C., but we notice that while the negative ion at the lower temperature moves at only 1/40 of its pace at the higher, the velocity of the positive ion is by the same fall in temperature only reduced to about 1/8.5 of its value.

These determinations of the velocity throw some light on the character of the ions; for suppose e is the charge of electricity on the ion, X the electric force acting upon it, the mechanical force acting on the ion is equal to Xe; if  $\lambda$  is the mean free path of the ion, v its velocity of translation, then the time between two collisions is  $\lambda/v$ , and in this time the force acting upon it will give it a velocity in the direction of the force equal to  $Xe\lambda/vm$ , where m is the mass of the ion; the average velocity

parallel to X due to the electric force will therefore be  $Xe\lambda/2vm$ : and this will be the velocity with which the ion will, under the electric force, move through the gas. The equal velocity of all negative ions from whatever source they may be derived might at first sight seem to indicate that as Arrhenius supposed all the salts were converted to hydroxides in the flame, and that the negative ion was in every case the radicle OH: let us calculate what on this supposition would be the velocity of the negative ion at a temperature of 2000° C. We do not know the free path of OH through a mixture of coal-gas and air, but as the free path of the molecule H<sub>2</sub> through hydrogen at 0° C. and at atmospheric pressure is  $1.8 \times 10^{-6}$  cm., and the free path of O<sub>o</sub> through oxygen under the same circumstances is  $1.06 \times 10^{-5}$  cm., we may as a rough approximation take for the mean free path of OH through the mixture the value  $1.4 \times 10^{-6}$  cm. at  $0^{\circ}$  C.; at  $2000^{\circ}$  C.  $\lambda$  the mean free path would be this value multiplied by 2273/273, i.e.  $1.2 \times 10^{-4}$ . To get the value of v we remember that  $mv^2$  is the same for all gases at the same temperature, while at different temperatures it is proportional to the absolute temperature. For  $O_2$  at  $0^{\circ}$  C.  $v = 4.25 \times 10^4$  cm./sec., hence for OH at  $0^{\circ}$  C.  $v = 5.6 \times 10^4$  cm./sec., and for OH at 2000° C.  $v = 1.6 \times 10^5$ : e/mfor OH is equal to  $1.1 \times 10^3$ , hence substituting these values in the expression  $Xe\lambda/2vm$  and putting  $X=10^{8}$  we find for the velocity under the potential gradient of one volt per cm. 37 cm./sec.: the actual velocity is as we have seen 1000 cm./sec.: hence we conclude that the radicle OH cannot be the carrier of the negative charges. The great velocity of the negative ions at these high temperatures points to the conclusion that the negative ions start as corpuscles and gradually get loaded by molecules condensing round them; at temperatures as high as 2000° the time they exist as free corpuscles is an appreciable fraction of their life; while they are free corpuscles they have an exceedingly large velocity, so that though this is enormously reduced when they become the nucleus of a cluster, their average velocity is very considerable. At low temperatures condensation takes place much sooner, so that the average velocity is lower.

The fact that under an electric field the velocities of the positive ions of all the salts of the univalent metals are the same, shows that these too become the nucleus of a group whose size only

depends upon the charge on the positive ion; since the velocities of the positive ions for the divalent metals while equal among themselves are less than those of the monovalent metals, we conclude that these divalent ions become the centres of clusters more complex than those which collect round the monovalent ions.

Determinations of the velocities of the ions in flames have also been made by Marx\*, he finds for the velocity of the negative ion the same value as Wilson, i.e. 1000 cm./sec. under a potential gradient of a volt per centimetre, he gets however for the positive ions under the same gradient considerably larger values than Wilson, i.e. 200 cm./sec. instead of 62 cm./sec. A calculation similar to that just given for the velocity of the radicle OH shows that a velocity of 200 cm./sec. is of the same order as the velocity at 2000° C. of an atom of hydrogen in an electric field.

Transverse Electromotive Force produced by a magnetic field acting on a flame carrying a current.

115. If an electric current is flowing through a flame parallel to the direction x, and a magnetic force at right angles to this direction, say parallel to the direction y, is applied to the flame, a transverse electromotive force is produced which is at right angles to both x and y. This electromotive force has been detected and measured by Marx $\dagger$ . The general explanation of this effect, which is analogous to the 'Hall' effect in metals, is easy; the calculation of its magnitude except in a few special cases is however beset by difficulties.

As there is a current parallel to x flowing through the flame, the average direction of the positive ions will be along, say, the positive direction of x, that of the negative ions in the opposite direction. Let V be the average velocity of the positive ions, V' that of the negative, if these are moving in a magnetic field where the magnetic force H is parallel to y, they will be subject to mechanical forces tending to move them in the same direction, this direction being parallel to z, at right angles to both x and y. The magnitudes of the mechanical forces acting on the positive and negative ions are respectively HeV and HeV', where e is the

<sup>\*</sup> Marx, Drude's Ann. ii. p. 768, 1900.

<sup>+</sup> Ibid. p. 798, 1900.

charge on an ion. The displacement of the ions under these forces will (if V is not equal to V') produce a current of electricity through the flame parallel to z; if however the ions cannot escape in this direction the current will soon stop, as the accumulation of ions will produce a back pressure and an electrostatic field which will balance the effect of the mechanical forces arising from the magnetic field.

We shall now proceed to deduce the equations which give the disturbance produced by the magnetic field; these equations are not limited to the case of flames, but apply to all cases of the conduction of electricity through a gas containing ions.

Let the direction of the primary current, *i.e.* the current before the magnetic field is applied, be taken as the axis of x, let the magnetic force act downwards at right angles to the plane of the paper: then the force on the ions will be in the plane of the paper and at right angles to the axis of x; we shall take the axis of z in this direction.

Let H be the intensity of the magnetic force,

- X, Z the components of the electric force parallel to the axes of x and z respectively,
- u, v the velocities of the positive and negative ions under unit electric force,
- $p_1$ ,  $p_2$  the pressures at any point due to the positive and negative ions respectively,
- m, n the number of positive and negative ions per cubic centimetre at any point.

We shall assume that these ions behave like a perfect gas, so that  $p_1 = Rm$ ,  $p_2 = Rn$ , where R is a constant proportional to the absolute temperature.

Let us consider first the positive ions, their velocity parallel to the axis of x is Xu, hence the mechanical force on an ion parallel to z due to the magnetic field is euXH, the force on the ion due to the electric field is Ze, and the force on the ions in unit volume due to the variation in the pressure at different points in the field is  $-dp_1/dz$ , hence the total force parallel to z on the positive ions in unit volume is equal to

$$-\frac{dp_1}{dz} + me (uXH + Z),$$

and the number crossing in unit time one square centimetre of surface at right angles to z is equal to

$$\frac{u}{e}\left\{-\frac{dp_1}{dz}+me\left(uXH+Z\right)\right\},$$

similarly the flux parallel to x is equal to

$$\frac{u}{e}\left\{-\frac{dp_1}{dx} + me\left(-uZH + X\right)\right\},\,$$

or, if we neglect terms depending upon  $H^2$  the term uZH may be omitted and the flux parallel to x is then

$$\frac{u}{e}\left\{-\frac{dp_1}{dx} + meX\right\}.$$

Similarly the flux of the negative ions parallel to z is equal to

$$\frac{v}{e} \left\{ -\frac{dp_2}{dz} + ne\left(vXH - Z\right) \right\},\,$$

and the flux parallel to x to

$$\frac{v}{e}\left(-\frac{dp_2}{dx}-neX\right).$$

Let q be the number of ions produced in one cubic centimetre of the gas in one second,  $\alpha nm$  the number of ions which recombine in one second in unit volume; then by the equation of continuity we have when things are in a steady state,

$$\frac{u}{e}\frac{d}{dz}\left\{-\frac{dp_1}{dz} + me\left(uXH + Z\right)\right\} + \frac{u}{e}\frac{d}{dx}\left(-\frac{dp_1}{dx} + meX\right) = q - \alpha mn,$$

$$\frac{v}{e}\frac{d}{dz}\left\{-\frac{dp_2}{dz} + ne\left(vXH - Z\right)\right\} + \frac{v}{e}\frac{d}{dx}\left(-\frac{dp_2}{dx} - neX\right) = q - \alpha mn;$$

we have also, using electrostatic units,

$$\frac{dX}{dx} + \frac{dZ}{dz} = 4\pi e (m-n),$$

and  $\frac{dX}{dz} - \frac{dZ}{dx} = 0.$ 

Since  $p_1 = Rm$ ,  $p_2 = Rn$ , we have as many equations as there are variables,  $p_1$ ,  $p_2$ , m, n, X, Z. The solution will however depend very greatly upon the boundary conditions; thus one solution is Z = 0,  $p_1$  and  $p_2$  constant, and X independent of z and the

same as when the magnetic force is zero: this, however, involves a transverse flux of positive ions equal to  $mu^2XH$  and of negative ions equal to  $nv^2XH$ , and is not consistent with a steady state unless there is some means for this transverse stream to escape. If there is no way of escape for the transverse streams of ions the flux of the ions parallel to z must vanish at the boundaries of the gas. Let us suppose that it vanishes throughout the gas, then we have

$$-\frac{dp_1}{dz} + me(uXH + Z) = 0....(1);$$
  
$$-\frac{dp_2}{dz} + ne(vXH - Z) = 0...(2).$$

Putting  $p_1 = Rm$ ,  $p_2 = Rn$  and  $(m-n)e = \rho$  we get from (1) and (2)

$$\frac{R}{e}\frac{d\rho}{dz} = eXH(mu - nv) + Ze(m + n) \quad ......(3);$$

and since, changing to electromagnetic units,

$$4\pi \frac{d\rho}{dz} = \frac{1}{V^2} \left( \frac{d^2Z}{dx^2} + \frac{d^2Z}{dz^2} \right),$$

where V is the velocity of light; (3) becomes

$$\frac{R}{4\pi e\,V^2}\left(\frac{d^2Z}{dx^2} + \frac{d^2Z}{dz^2}\right) = eXH\left(mu - nv\right) + Ze\left(m + n\right) \quad .....(4),$$

an equation to find Z. In the terms on the right-hand side, we may put for X, m, n the values when H = 0, if we are content to neglect terms in  $H^2$ .

Since  $V^2 = 9 \times 10^{20}$ ,  $e = 1.1 \times 10^{-20}$  (in electromagnetic units),  $R = 5 \times 10^{-14}$ , for a gas at 0° C., we see that (4) may be written

$$4\times10^{-16}\left(\frac{d^{2}Z}{dx^{2}}+\frac{d^{2}Z}{dz^{2}}\right)=eXH\left(mu-nv\right)+Ze\left(m+n\right).$$

If the sum of the partial pressures due to the positive and negative ions were 1 atmosphere e(m+n) would be about 5, hence we see that if the pressure of the ions is large compared with  $10^{-15}$  atmospheres and if Z does not vary exceedingly rapidly with x, a very approximate solution of (4) will be

$$Z = \frac{XH(nv - mu)}{m+n} \qquad \dots (5).$$

This may be written

$$Z = \frac{H\left(i_{n}-i_{p}\right)}{e\left(m+n\right)},$$

where  $i_n$  and  $i_p$  are respectively the currents carried by the negative and positive ions.

At a place where there is no free electricity m = n; in this case (5) becomes

 $Z = \frac{1}{2}XH \ (v - u).$ 

This is the formula usually employed, but we see from the preceding work it is only applicable in a very special case.

When solutions of KCl of various strengths were sprayed into a flame Marx\* found values of Z/XH varying from  $10\cdot18\times10^{-6}$  for the pure flame to  $3\cdot7\times10^{-6}$  when a saturated solution of KCl was sprayed into it, the sign of the result showing that the velocity of the negative ion is greater than that of the positive. If we apply the preceding formula we find, on the supposition that the measurements were made in a part of the flame where there was no free electricity, that the difference between the velocities of the negative and positive ions under an electric force of one volt per centimetre, i.e.  $10^{8}$  units, would vary from 2036 cm./sec. for the pure flame to 740 cm./sec. for the flame containing the concentrated solution; the value 940 found by H. A. Wilson by direct experiment is between these limits.

If the electric and magnetic forces are considerable there will, when there is no escape for the transverse flow of ions, be very considerable variations in the number of ions in the gas: for putting  $p_1 = Rm$ ,  $p_2 = Rn$ , we get from equations (1) and (2),

$$R\frac{d}{dz}\log mn = eXH(u+v),$$

$$Ce^{X(u+v)z/R}$$

or  $mn = Ce^{eX(u+v)z/R},$ 

where C is a constant. To see what concentration this implies let us take the case of air ionised by Röntgen rays, the pressure being 1/1000 of an atmosphere, then since u+v at atmospheric pressure is  $3\times 10^{-8}$  cm./sec., at the assumed pressure it will be  $3\times 10^{-5}$ , and if X is 10 volts a centimetre, i.e.  $10^9$ , and  $H=10^2$ , then since  $e/R=4\times 10^{-7}$ , we see

$$mn = C\epsilon^{1\cdot 2z}$$
;

\* Marx, Drude's Ann. ii. p. 798, 1900.

thus in the space of a centimetre parallel to z, mn will about triple in value: this variation in the number of ions will affect the distribution of the current parallel to x, the current will be greatest where there are most ions and will therefore no longer be independent of z: this variation in the current may affect the distribution of potential between the electrodes and thus introduce fresh sources of disturbance into the problem.

In the case when there are only ions of one sign present, say the negative, there is a very simple solution of the preceding equations, for we see that Z = eHXv,  $p_2$  constant and X the same as when there is no magnetic force satisfies these equations.

Maximum current that can be carried by the vapour of a salt.

116. H. A. Wilson\* has made an exceedingly important set of experiments on the maximum current that can be carried by a given amount of salt vapour; in these experiments the solution containing the salt vapour was not sprayed into flame, but into air heated by passing through a long platinum tube raised to bright yellow heat by a furnace; a smaller central tube was placed along the axis of the outer tube and the current between the inner and outer tubes measured. When solutions of the strength 1/10th normal were sprayed and the temperature of the tubes raised and the potential difference increased, a stage was reached when neither an increase in the temperature nor in the potential difference produced any increase in the current. Wilson measured this limiting current and found that it was equal to the current which when passing through an aqueous solution of the salt would electrolyse in one second the same quantity of salt as was sprayed in that time into the hot air; thus if the salt had been supplied to water at the same rate as it was supplied to the hot air the maximum current that could be sent through the aqueous solution would be the same as that which could be sent through the air; this was proved for the following salts of the alkali metals: CsCl, CsCO<sub>3</sub>, RbI, RbCl, Rb<sub>2</sub>CO<sub>3</sub>, KI, KBr, KF, K2CO3, NaI, NaBr, NaCl, Na2CO3, LiI, LiBr, LiCl, Li2CO3.

<sup>\*</sup> H. A. Wilson, Phil. Mag. vi. 4, p. 207, 1902.

### CHAPTER X.

#### IONISATION BY LIGHT. PHOTO-ELECTRIC EFFECTS.

THE discovery by Hertz\* in 1887 that the incidence of ultraviolet light on a spark gap facilitated the passage of the spark, led immediately to a series of investigations by Hallwachs+, Hoort, Righis and Stoletow on the effect of light, and especially of ultra-violet light, on charged bodies. It was proved by these investigations that a newly cleaned surface of zinc, if charged with negative electricity, rapidly loses this charge however small it may be when ultra-violet light falls upon the surface; while if the surface is uncharged to begin with, it acquires a positive charge when exposed to the light, the negative electrification going out into the gas by which the metal is surrounded; this positive electrification can be much increased by directing a strong airblast against the surface. If however the zinc surface is positively electrified it suffers no loss of charge when exposed to the light: this result has been questioned, but a very careful examination of the phenomenon by Elster and Geitel I has shown that the loss observed under certain circumstances is due to the discharge by the light reflected from the zinc surface of negative electrification on neighbouring conductors induced by the positive charge, the negative electricity under the influence of the electric field moving up to the positively electrified surface.

\* Hertz, Wied. Ann. xxxi. p. 983, 1887.

<sup>†</sup> Hallwachs, Wied. Ann. xxxiii. p. 301, 1888.

<sup>‡</sup> Hoor, Repertorium des Physik, xxv. p. 91, 1889.

<sup>§</sup> Righi, C. R. evi. p. 1349; evii. p. 559, 1888.

<sup>||</sup> Stoletow, C. R. cvi. pp. 1149, 1593; cvii. p. 91; cviii. p. 1241; Physikalische Revue, bd. i., 1892.

<sup>¶</sup> Elster and Geitel, Wied. Ann. xxxviii. pp. 40, 497, 1889; xli. p. 161, 1890; xlii. p. 564, 1891; xliii. p. 225, 1892; lii. p. 433, 1894; lv. p. 684, 1895.

The ultra-violet light to produce these effects may be obtained from an arc lamp, or by burning magnesium, or by sparking with an induction coil between zinc or cadmium terminals, the light from which is very rich in ultra-violet rays. Sunlight is not rich in ultra-violet rays, as these have been absorbed by the atmosphere, and it does not produce nearly so large an effect as the arc-light. Elster and Geitel who have investigated with great success the effects produced by light on electrified bodies have shown that the more electropositive metals lose negative charges even when exposed to ordinary daylight. They found that amalgams of sodium or potassium enclosed in a glass vessel lose a negative charge in the daylight, though the glass would stop any small quantity of ultra-violet light that might be left in the light after its passage through the atmosphere. When sodium or potassium by themselves instead of their amalgams were used, or, what is more convenient for many purposes, the liquid alloy formed by mixing these metals in the proportion of their combining weights, they found that the negative electricity was discharged by the light from a petroleum lamp: while with the still more electropositive metal rubidium the negative electricity could be discharged by the light from a glass rod just heated to redness. They found, however, that the eye was more sensitive to the radiation than the rubidium, for no discharge could be detected until after the radiation from the glass rod was visible.

Elster and Geitel arrange the metals in the following order with respect to their power of discharging negative electricity:

Rubidium.
Potassium.
Alloy of Potassium and Sodium.
Sodium.
Lithium.
Magnesium.
Thallium.
Zinc

For copper, platinum, lead, iron, cadmium, carbon, and mercury the effects with ordinary light are too small to be measurable. The order of the metals for this effect is the same as in Volta's series for contact-electricity, the most electropositive metals

giving the largest photo-electric effect. Many substances besides metals discharge negative electricity under the action of ultraviolet light: lists of these substances will be found in papers by G. C. Schmidt\* and O. Knoblauch†. Among the more active photo-electric solids are, fluor-spar, the various coloured varieties of which vary greatly in the degree to which they possess this property; the sulphides of antimony, lead, arsenic, manganese, silver, and tin (the sulphates do not possess this property); hydroxide of tin, iodide of lead, many aniline dyes in the solid state.

Pure water is not photo-electric, and a thin film of water over the surface of a metal destroys the effect due to the metal. The solutions of many substances are however very photo-electric, especially solutions of fluorescent substances such as eosine, fuchsine, cyanine, hydrochinone, congo-red; potassium nitrate and formic acid also show this effect. Among well-known substances which do not show this effect we may mention solutions of sulphate of quinine, potassium permanganate and phenol.

# Photo-electric properties of gases.

117. With gases the action of light may be expected to manifest itself in a different way from that occurring in the case of solids and liquids, we cannot expect to get a separation of electricity of such a kind that one region of the gas becomes positively, another negatively, electrified. If a molecule of a gas loses, like a piece of metal, negative electricity when exposed to ultraviolet light, then this molecule will behave like a positive ion, and the negative corpuscle it has lost will attach itself to some other molecule of the gas which will act like the negative ion; thus if ultra-violet light produced on the molecules and atoms of a gas the same effect as it does on a mass of metal we should expect this effect to show itself as ionisation of the gas. In the case of sodium vapour, light produces a decided increase in the conductivity; it is not necessary that the light should be ultra-violet, the light from a petroleum lamp is sufficient to produce well-marked effects; we have seen that sodium when in the solid state is

<sup>\*</sup> G. C. Schmidt, Wied. Ann. lxiv. p. 708, 1898.

<sup>†</sup> O. Knoblauch, Zeit. f. Physikalische Chemie, xxix. p. 527, 1899.

peculiarly sensitive to the action of light. Experiments have been made on other gases; thus Henry\* who tried the effect of ultraviolet light on iodine vapour, which absorbs a good deal of light, could not detect any increase in conductivity when the gas was illuminated: Buisson† was unable to detect any conductivity in air through which ultra-violet light was passing: recently, however, Lenard has described an effect due to a very easily absorbed kind of ultra-violet light produced when sparks from an induction coil pass between aluminium terminals; this light is so easily absorbed by air that its effect becomes inappreciable after it has passed through a few centimetres of air at atmospheric pressure. Quartz is more transparent than air to this light; coal-gas is very much less transparent than air, while hydrogen is more so. the aluminium terminals were placed behind a quartz window in a metal plate, then a charged conductor placed on the far side of the plate near to the gas illuminated by these rays was found to lose its charge rapidly if positively electrified, very much more slowly if negatively electrified. In order to avoid spurious effects due to the light falling on metal surfaces in the neighbourhood Lenard covered these with soap and water, which he found prevented any discharge of electricity due to light falling on a metal plate. The much greater loss experienced by the plate when the charge was positive than when it was negative indicates that the velocity of the negative ions is much greater than that of the positive. Lenard measured by a method used by Zeleny and described on p. 38, the velocities of the ions; he found that under a potential gradient of a volt per centimetre the velocity of the negative ions through air at atmospheric pressure is 3.13 cm./sec.: this is considerably greater than (almost double) the velocity found by Rutherford for the negative ions produced by ordinary ultra-violet light incident on a metal plate: the velocity of the positive ions was found by Lenard for a gradient of a volt per centimetre to be only 0015 cm./sec., that is only about 1/2000 of the velocity of the negative ions. The exceedingly small velocity of these positive ions raises the question as to whether they are not particles of dust or minute drops of impure water, rather than

<sup>\*</sup> Henry, Proc. Camb. Phil. Soc. ix. p. 319, 1897.

<sup>†</sup> Buisson, quoted by Perrin, Ann. de Chimic et de Physique, vii. 11, p. 526, 1897.

<sup>‡</sup> Lenard, Drude's Ann. i. p. 486; iii. p. 298, 1900.

gaseous ions. It is essential to show that they are not of this nature if these experiments are to demonstrate the ionisation of the air by the ultra-violet light, for the enormous discrepancy between the velocities of the positive and negative ions is exactly what we should expect if dust possessing photo-electric properties were exposed to the influence of ultra-violet light; such particles would emit negative electricity, while the positive electricity would remain behind on the dust; the comparatively large dust particles would move very slowly in an electric field, while the negative ions being free from dust might be expected to move with much greater velocity. Lenard discusses this interpretation of his results and rejects it for reasons which do not appear to us absolutely convincing. He considers that the negative ions produced by the action of ultra-violet light on air are essentially different from those produced when the light falls on a metal, and that while the latter are able to produce condensation in a steam jet, the former are unable to do so. The evidence for this is as follows; though the gas under direct illumination by the ultra-violet light produces vigorous condensation in a steam jet, yet if the negative ions are pulled out of the illuminated gas by a positively charged plate placed at some distance away no condensation of the jet takes place in the region between the plate and the gas exposed to the light, though the leak of positive electricity from the plate shows that this region is being traversed by negative ions. To make the experiment conclusive, however, we require to know the sensitiveness of the steam jet, i.e., the minimum number of ions per cubic centimetre it is capable of detecting, and also to be sure that the number of negative ions in the neighbourhood of the jet exceeds this minimum: now the second point is one that requires very careful attention, for if the electric field in the neighbourhood of the plate is intense the negative ions will be moving at a very high speed and a very small number of ions in each cubic centimetre would be sufficient to produce a very appreciable leak; in fact if this leak is 'saturated' we see that the density of the ions will be inversely proportional to the strength of the field, so that by increasing this strength sufficiently we could certainly stop the condensation of the steam-jet. Thus this experiment does not prove that the negative ions are incapable of acting as centres of condensation: to make the proof valid we should require to know that the number of ions in each unit volume was so large that condensation would take place if these ions had the property of the normal negative ion.

118. C. T. R. Wilson\* has studied the action of ultra-violet light on gases from the point of view of the effect produced by the light on the formation of clouds. His results with intense light have already been described in Chapter VII., we shall only consider here the effects he got with very feeble light, as the effects have a direct bearing on the question of the ionisation of air by ultraviolet light, though they do not touch the question as to the effects produced by the extremely absorbable light studied by Lenard. Wilson found that with very feeble ultra-violet light clouds were produced by expansion when this exceeded a definite amount, just as in the case of a gas ionised by Röntgen rays, and that the amount of expansion required was just the same for the ultraviolet light as for these rays: this at first sight looks as if the ultra-violet light ionised the gas. Wilson, however, found that the clouds produced by ultra-violet light differed from those produced by Röntgen rays, inasmuch as the former were not affected by strong electric fields, whereas the formation of the latter was almost entirely prevented by such fields. If the clouds due to ultra-violet light had been due to the ionisation of the gas the ions would have been removed by the field and the clouds stopped. At the same time the coincidence between the expansions required for the formation of clouds under ultra-violet light and when ions are present is so remarkable that it makes us very reluctant to believe that the nuclei are different in the two cases; it seems to me that an explanation which is in harmony with the facts is that charged ions do form the nuclei of the drops formed by weak ultra-violet light, but that these ions are produced during the expansion of the gas and are not present when the gas is at rest; these ions might arise in the following way: we have seen in Chapter VII. that under the action of strong ultra-violet light visible clouds are formed without expansion, these clouds being probably due to the formation of hydrogen peroxide, which mixing with the water lowers the vapour pressure; now when the light is very feeble it seems probable that there may still be a formation of drops of water which, however, in consequence of the very small amount of hydrogen peroxide produced by the feeble light, never

<sup>\*</sup> C. T. R. Wilson, Phil. Trans. 192 A, p. 403, 1899.

grow large enough to be visible. Thus we may regard the air exposed to the ultra-violet light as full of exceedingly minute drops of water; when the expansions take place the air will rush violently past the drops and we get a state of things which in many respects is analogous to the bubbling of gas through water; when, however, air bubbles through water there is as Lord Kelvin\* has shown negative electricity in the air and positive in the water; thus when the air rushes past the water drops we should expect the air to contain negative ions, the positive ions being on the drops; the ions once formed would act as nuclei for clouds if the expansion exceeded the value 1.25. If this view is correct, then we should expect the number of ions produced by an expansion greater than 1.25 to increase with the expansion, for in this case the expansion has to produce the nuclei as well as deposit the clouds, and the more vigorous the expansion the greater would be the number of nuclei produced.

It is an important meteorological question as to whether direct sunlight can produce a cloud in the atmosphere without expansion. Wilson was not able to get a cloud in a closed vessel in sunlight with less than the normal expansion 1.25. He points out, however, that the conditions in the open air are more favourable to the production of clouds than those in a closed vessel, for in a closed vessel the drops might diffuse to the sides before they had time to grow to a visible size, while in the atmosphere this way of escape would not be open to them.

## Photo-electric effects involve an absorption of Light.

119. Stoletow† at an early stage in the history of this subject called attention to the connection between the photo-electric effects and the absorption of the ultra-violet light; he pointed out that water which does not give photo-electric effects does not absorb many of the visible or ultra-violet rays, while solutions such as those of methyl-green or violet, which are photo-electric, show strong absorption. Hallwachs‡, who investigated the subject in greater detail, showed that all the photo-electric liquids which he tried showed strong absorption for the ultra-violet light, but

<sup>\*</sup> Lord Kelvin, Proc. Roy. Soc. lvii. p. 335, 1894.

<sup>†</sup> Stoletow, Physikalische Revue, bd. i. 1892. ‡ Hallwachs, Wied. Ann. xxxvii. p. 666, 1889.

that strong absorption was not always accompanied by photoelectric effects; thus for example the aqueous solution of fuchsine is photo-electric, while the alcoholic solution is not, and yet the alcoholic solution absorbs more ultra-violet light than the aqueous one.

The effects of increased absorption are shown in a very beautiful way by the experiments of Elster and Geitel\* on the leak of negative electricity from surfaces of sodium, potassium, and rubidium under different coloured lights. The experiments, the results of which are shown in the following table, were made as follows; the rate of escape from the three metals when exposed to the white light from a petroleum lamp was measured, these measurements are given in the table under the heading 'white light.' The light from this lamp was then sent through an ammoniacal solution of copper oxide and the metals exposed to the blue light thus obtained; this solution was replaced by one of potassium chromate to get yellow light, by one of potassium bichromate to get orange light, and by a plate of deep red glass to get the red light.

	Rate of leak of negative electricity			
Colour of Light	Na	K	Rb	
White	21.0	53.1	537.0	
Blue	7.8	30.3	86.8	
White	22.6	52.9	527.7	
Yellow	8.2	3.5	339.7	
White	21.9	53.9	552.3	
Orange	3.1	2.2	182.0	
White	21.9	52.9	527.7	
Red	•2	0.1	21.0	

Thus we see from this table that though for white and blue lights potassium is much more photo-electric than sodium, it is much less so for yellow and orange light, owing to the strong absorption of these rays by the sodium. The very great sensitiveness of rubidium to light of long wave-length is another instance. Thus while the ratios of the leaks for rubidium and potassium under blue light were only 3 to 1, the ratio for yellow light was about 100 to 1.

<sup>\*</sup> Elster and Geitel, Wied. Ann. lii. p. 433, 1894.

Connection between the rate of leak and strength of Electric Field.

120. The first measurements on this subject were made by Stoletow\*, who used the following arrangement: the light from an arc lamp passed through a hole in a metal screen, and after passing through a perforated plate C fell upon a parallel metal plate D; these plates were connected together through a battery, the negative pole of the battery being connected with D, the plate illuminated by the light. The current passing between the plates was measured by a very sensitive galvanometer. By means of this

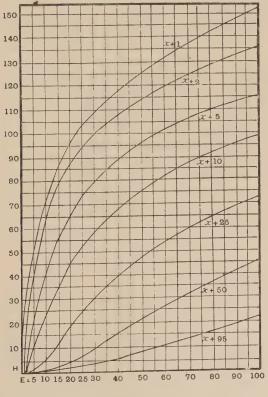


Fig. 55.

arrangement Stoletow measured the relation between the current and the potential difference between the plates, making experi-

<sup>\*</sup> Stoletow, Journal de Physique, ii. 9, p. 468, 1890.

ments with the plates at distances apart varying from about 2.5 millimetres to 100 millimetres; the results of these experiments, in which the gas between the plates was air at atmospheric pressure, are represented by the curves of Fig. 55; the abscissæ represent the potential differences between the plates, the unit being 1.43 volts (the electromotive force of a Clark's cell); the ordinates represent the current passing between the plates, the unit being  $8.6 \times 10^{-11}$  ampères; the symbol on the curve, for example x + 25, indicates that the distance between the plates was x + 25 millimetres, where x is a small distance, about 1.5 mm., that was not very accurately determined; the diameter of the plates was 22 mm. An inspection of the curves shows that when the distance between the plates is small and the electromotive force large the current increases much more slowly than the electromotive force; it is, however, evidently far from saturation; while when the plates were separated by distances greater than 25 mm. there was no approach to saturation. The curves corresponding to the greater distances between the plates show that under small electromotive forces the current increases more rapidly than the potential difference. As far as the measurements represented in the figure go i is approximately the same at all distances d, provided V/d is the same, V being the potential difference, i.e., i is a function of the mean value of the electric force between the plates; this law, as Stoletow showed in a later paper\*, does not apply for any great range of potential differences, at lower pressures especially the departures from it are soon very apparent.

Since in this case the ions are all of one kind we may apply the equation of Art. 99, i.e.,

$$X^{\rm 2} = X_{\rm 0}^{\rm 2} + \frac{8\pi i x}{R} \, , \label{eq:X2}$$

where R is the velocity of the ion under unit electric force, i the intensity of the current,  $X_0$  and X the values of the electric force at the plate and at a point distant x from it.

To form an estimate of the variation in the electric field which is produced by the presence of the negative ions between the plates, let us take one of Stoletow's experiments in which under an electric field of 150 volts per cm. the current was  $3.3 \times 10^{-11}$ 

<sup>\*</sup> Stoletow, Journal de Physique, ii. 9, p. 469, 1890.

ampères. The velocity of the negative ions produced by a field of 1 volt per centimetre has been shown by Rutherford to be about 1.5 cm./sec. Hence using electrostatic units, X and  $X_0$  being the values of X at places a centimetre apart, putting  $i=10^{-1}$ ,  $R=4.5\times10^2$ ,  $X+X_0=1$ , in the preceding equation, we get  $X-X_0=1/180$  or a little less than 2 volts per cm., thus the variation in the strength of the field is comparatively small. Stoletow, who determined the intensity of the field between two parallel plates one of which was illuminated by ultra-violet light, was not able to detect any variation in the intensity. Schweidler\*, who investigated this point at a later period, found that the distribution of potential between the plates when the ultra-violet light was in action, was not quite uniform; his results are shown in Fig. 56, where the curved line represents the distribution of

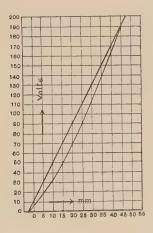


Fig. 56.

potential when the light was shining, the straight one when it was not. The curvature of the potential curve in the light is all in one direction, indicating the presence of an excess of negative ions in every part of the region between the plates. The variation in the intensity of the field between the plates has also been observed and measured by Buisson† and used by him to determine the velocity of the negative ions; he finds that under a potential gradient of a volt per cm. this velocity is about 2.2 cm./sec.

<sup>\*</sup> Schweidler, Wien. Ber. cvii. p. 881, 1898.

<sup>†</sup> Buisson, Comptes Rendus, exxvii. p. 224, 1898.

Schweidler\* has also made experiments on the relation between the current and the strength of the electric field over a wider range than in Stoletow's experiments: his results for air at atmospheric pressure are shown by the curve (Fig. 57). It will be

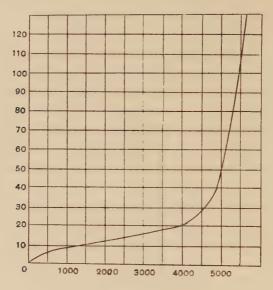


Fig. 57.

noticed that when the strength of the field approaches the value 5730 volts, which is the strength required to spark across the plates which were 3 mm. apart in the dark, there is a very great increase in the current.

This rapid increase of the photo-electric effect in the neighbourhood of the sparking potential was first observed by Kreusler†. The relation between the leak from plates of iron, aluminium, copper, zinc, silver and amalgamated copper, and the strength of field are represented in the curves given in Fig. 58: the abscissæ measured from 0 represent the difference between the electromotive force applied and that required to produce discharge in the dark. The increase in the leak is so great that it cannot be adequately

<sup>\*</sup> Schweidler, Wien. Ber. cviii. p. 273, 1899.

<sup>†</sup> Kreusler, Drude's Ann. vi. p. 398, 1901.

represented in a moderately sized figure, a better idea in the case of the zinc plate can be derived from the following table given by

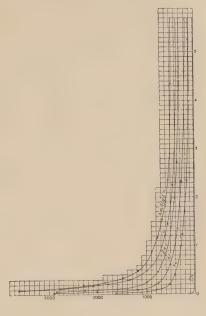


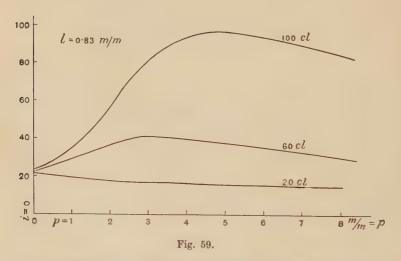
Fig. 58.

Kreusler. V is the potential difference and i the current, the potential required to produce a spark was 4060.

V	i (1=10 <sup>-10</sup> Amp.)	V	i (1=10 <sup>-10</sup> Amp.)	<i>v</i>	i (1=10 <sup>-10</sup> Amp.)
4040	136·39	3050	0·19	3300	0°36
3970	25·67	2540	0·09	3440	0°58
3780	5·88	1760	0·06	3640	1°36
3700	2·40	1170	0·05	3710	1°98
- 3590	1·39	1760	0·06	3760	3°88
3440	0·70	2530	0·08	3970	21°09
3300	0·40	3060	0·17	4040	80°51

These figures also show evidence of an effect often observed when using ultra-violet light—the decrease of sensibility with the time; thus of the two readings taken with the greatest potential difference the later one was very appreciably less than the earlier one. This 'fatigue' of the plates is probably due to oxidation, it does not take place in hydrogen nor at very low pressures, nor when platinum is used instead of zinc.

The increase in the rate of leak when the electric field approaches a certain strength is also very evident when the gas is at lower pressures. The effect of altering the pressure of the gas was first investigated by Stoletow\*, and subsequently by Schweidler† and Lenard‡. Stoletow showed that as the pressure was diminished, starting from atmospheric pressure, the current slightly increased, the change in the current being small compared with that in the pressure; on carrying the reduction of pressure still further, a stage was reached (if the strength of the field was not too small) when the current increased rapidly as the pressure diminished, this went on until the current reached a maximum value, after which it began to decline, but at the lowest obtainable pressures it had a finite value which was independent of the strength of the electric field.



The variation of the current with the pressure when the potential difference remains constant is exhibited in the curves (copied from Stoletow's paper) shown in Fig. 59; the distance

<sup>\*</sup> Stoletow, Journal de Physique, ii. 9, p. 468, 1890.

<sup>+</sup> v. Schweidler, Wien. Ber. cviii. p. 273, 1899.

<sup>‡</sup> Lenard, Drude's Ann. ii. p. 359, 1900.

between the plates was  $\cdot 83$  millimetres and the figures on the curves indicate the potential difference expressed in terms of Clark's cells (1 Clark's cell =  $1\cdot 4$  volts).

The values of the current at a series of pressures when the distance between the plates was 3.71 mm, and the potential difference about 90 volts are shown in the following table:

Pressure in millimetres	Current	Pressure in millimetres	Current	Pressure in millimetres	Current
754 152 21 8·8 3·3	8·46 13·6 26·4 32·2 48·9	2:48 1:01 0:64 0:52 0:275	74.7 105.8 108.2 102.4 82.6	0·105 0·0147 0·0047 0·0031	65·8 53·8 50·7 49·5

We see by an inspection of the curves in Fig. 59 that the pressure at which the current is a maximum increases with the electric force between the plates: Stoletow has shown that  $p_m$ , the pressure at which the current is a maximum, is proportional to E/d, where d is the distance and E the potential difference between the plates; this law may also be expressed by saying that if  $\lambda$  is the mean free path of a molecule at the pressure for maximum current, when the electric force is X, then  $X\lambda$  is constant. The curves in Fig. 59 show that at very low pressures the current is independent of the strength of the electric field, *i.e.* is saturated. This is also well shown by the following numbers taken from Lenard's paper. V is the potential difference in volts and i the current, the vacuum was the best obtainable, the pressure being less than '002 mm. of mercury.

V	i .	V	i	
45000 25000 8900 4100 3110 1300	24·5×10 <sup>-10</sup> Coulomb/sec. 26·6 , , ,, 22·5 ,, ,, 24·8 ,, ,, 24·5 ,, ,,	500 120 14 9 1	23·4 × 10 <sup>-10</sup> Coulomb/sec. 21·9 ,, ,, 19·9 ,, ,, 15·9 ,, ,, 7 ,, ,, 4 ,, ,,	

The critical pressure is of the same order of magnitude as the pressure at which the electric field would be able to produce a

discharge in the dark; in this region of pressure Stoletow has shown that the current does not depend merely upon the value of E/d where E is the potential difference and d the distance between the plates, for with a constant value of E/d the current at these pressures increases rapidly with the distance between the plates.

V. Schweidler\* has given curves representing the relation between the current and the potential difference at several pressures. Similar curves have lately been obtained by Varley at the Cavendish Laboratory, some of these are reproduced in Figs. 60 and 61. The curves show three distinct stages; the first when

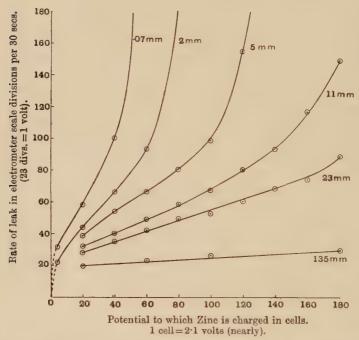


Fig. 60. Variation of ultra-violet light leak from zinc surface with the pressure for constant illumination.

The experiments were conducted in hydrogen. The distance between the electrodes was 1 cm.

the electric force is weak, then the current increases rapidly with the electric force, the rate of increase gradually dies away as the

<sup>\*</sup> v. Schweidler, Wien. Ber. cviii. p. 273, 1899.

electric force increases, and the second stage is reached when the current only varies slowly, at some pressures hardly at all, with the electric field; with still larger electric forces a third stage is

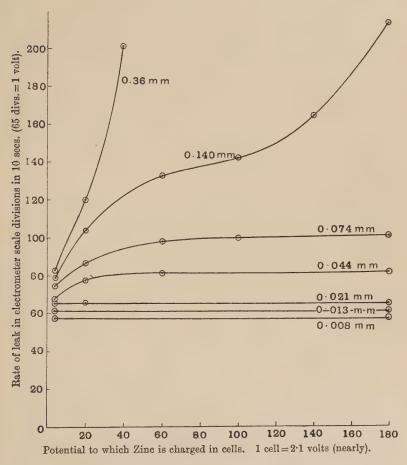


Fig. 61. Variation of ultra-violet light leak from zinc surface with the pressure, when the latter is low, for constant illumination.

The experiments were conducted in air. The distance between the electrodes was 4 mm.

reached when the current increases rapidly with the electric force and also with the distance between the electrodes.

Theoretical considerations relating to the connection between the current and the strength of the electric field.

121. It will be convenient to confine our attention in the first place to electric fields which are weak compared with those required to produce discharge in the dark. The view we take of the action of the ultra-violet light is that under the action of this light the metal emits from each unit area in unit time a certain number of corpuscles; that these soon, when gas surrounds the metal, get attached to one or more molecules of the gas and form negative ions. If there is no electric field to remove these ions they will go on accumulating in front of the metal plate, and as the number of the ions is greater at a little distance from the plate than at the plate itself, there will be diffusion of the ions from the place of greater to the place of less density, i.e. back into the plate, and things will reach a steady state when the accumulation of ions in front of the plate is so great that the number of ions which diffuse back into the plate is equal to the number shot from it by the ultra-violet light. If an electric field acts on the gas some of the ions will move off through the gas, producing a current of electricity; the accumulation of ions will not be so great as in the previous case, and equilibrium will be reached when the number of ions shot off by the ultra-violet light is equal to the number which diffuse back into the plate plus the number which are carried away by the electric field.

To put these considerations in a symbolical form let us take the case when the current is flowing between two parallel plates: let I be the number of negative ions emitted\* by unit area of the illuminated surface in unit time, and  $\sigma$  the number of ions per c.c. at any point between the plates, then if X is the electric force, u the velocity acquired by a negative ion under unit electric force, e the charge on an ion, and i the current flowing through unit area, then  $Xu\sigma e=i$ : we have seen that X is approximately constant between the plates, hence as i is constant it follows that  $\sigma$  will be approximately constant. This constant value of  $\sigma$  will not however hold right up to the illuminated plate, we may suppose that the density of the ions increases from zero to this

<sup>\*</sup> These ions start as corpuscles but are soon converted into ions by adhesion to the molecules of the gas surrounding them.

constant value in a small distance  $\lambda$  from the plate: thus at the surface of the plate there will be a gradient in the density of the ions of the order  $\sigma/\lambda$ , and if D is the coefficient of diffusion of the ions through the gas the number of negative ions flowing back into unit area of the plate in unit time is  $D\sigma/\lambda$ . The number of ions carried away through the gas by the electric field in unit time is i/e, hence we have when things have settled into a steady state.

$$I = \frac{D\sigma}{\lambda} + \frac{i}{e}$$
;

but  $Xu\sigma e = i$ , hence we have

or

this relation between i and X exhibits the chief features of the earlier parts of the curves obtained by Schweidler and Stoletow: when X is small the current is proportional to the electromotive force, it soon however increases less rapidly than X, and when X is very large approximates to the constant value Ie.

We have seen (p. 32) that u = De(n/p), where n is the number of molecules in a cubic centimetre of gas at the pressure p: thus u/D is the same for all gases: hence we see from (1) that any alteration in the current produced by altering the gas through which the current passes must be due to the alteration in  $\lambda$ : so that if this equation were rigorously true then under the same potential difference, provided this were small, the currents through different gases would be proportional to the values of  $\lambda$  for these gases. In this connection it is necessary to remember that the diffusion of the ions back into the metal takes place through a layer of gas in immediate proximity to the metal, and that D refers to this layer, while the u which occurs in equation (1)relates to the gas at a considerable distance away from the plate; if there were anything in the nature of a gaseous layer adhering to the metal, then the gas through which the ions diffuse might be different from the gas in the rest of the field, so that we should not be justified in assuming that the ratio of D to u was a constant independent of the nature of the gas. Again, we have assumed that the only ions available for carrying the

current are those which come out of the metal: now we shall see directly that the motion of ions through a gas with a high velocity ionises the gas, thus if the corpuscles are projected from the metal with a velocity exceeding a certain critical value they will ionise the molecules of the gas against which they strike, and thus the total number of ions produced would exceed the number projected from the metal by an amount depending upon the nature of the gas. The observations hitherto made on different gases are not sufficiently extensive to enable us to decide whether or not an effect of this kind does exist\*. Elster and Geitel+ and Stoletow<sup>+</sup> found that with the strength of electric field used by them the rate of escape of electricity through carbonic acid gas was much greater than that through air or oxygen. Breisig§ on the contrary found that the rate was less through CO2 than through air: and that it was exceptionally large through the vapours of ether and alcohol. The rate of leak varies so much with the potential difference that a comparison of the rates of leak for the different gases with only one value for the potential difference is not satisfactory and gives little information. What is really wanted is a comparison for the different gases of the curves representing the relation between the current and the potential difference. It would also be desirable to have these curves drawn for ultra-violet light of different wave-lengths. The different gases might also cause the currents to differ by altering the surface of the metal either by combining with it or by condensing on its surface.

122. We shall now go on to consider the sudden increase in the current which occurs when the electric field approaches the intensity required to produce a discharge in the dark. We can, I think, explain this by means of some considerations first advanced by the author to explain the ionisation produced when a strong electric field causes a discharge to pass through a gas. When cathode or Lenard rays pass through a gas, the gas becomes a

<sup>\*</sup> Since this was written Varley has made at the Cavendish Laboratory experiments proving the existence of this secondary ionisation.

<sup>+</sup> Elster and Geitel, Wied. Ann. xli. p. 161, 1890.

<sup>‡</sup> Stoletow, C. R. evii. p. 91, 1888.

<sup>§</sup> Breisig, Bonn. Diss. 1891; Wied. Beiblätter, xvii. p. 60.

<sup>||</sup> J. J. Thomson, Proc. Camb. Phil. Soc. Feb. 5, 1900; Phil. Mag. v. 50, p. 278, 1900.

conductor, i.e. it is ionised; hence we see that when very rapidly moving ions pass through a gas and come into collision with its molecules the gas is ionised: the energy required for the ionisation coming from the kinetic energy of the rapidly moving ions. Inasmuch as the ionisation of a molecule of a gas requires the expenditure of a finite amount of work, a moving ion cannot ionise a molecule against which it strikes unless its kinetic energy exceeds a certain critical value, but when its energy does exceed this value then a certain fraction of the number of collisions between the ions and the molecule will result in ionisation. when the ions are moving in an electric field, the kinetic energy acquired by the ions will increase as the strength of the field increases, and when the field is strong enough to make the kinetic energy of the ions exceed the critical value, the ions by their collisions will give rise to new ions, and thus there will be an increase both in the number of ions and the current through the gas: it is this increase which is so marked a feature of the currents produced by ultra-violet light when the electric field is strong.

If l is the mean free path of an ion, X the electric force, e the charge on the ion, then the mean kinetic energy given to the ion by the electric field is Xel; when therefore Xel exceeds a certain critical value, ionisation will take place in a certain fraction of the collisions; let us denote this fraction by f(Xel), f(x) being a function of x which vanishes when x is less than a certain value. If there are n ions per cubic centimetre, then the number of collisions in unit time is equal to nv/l, where v is the average velocity of translation; hence the number of ions produced in unit time per unit volume is  $\frac{nv}{L}f(Xel)$ . A certain number of collisions may result either in the recombination of the ion, or the attachment of the ion to the system against which it collides, so that the ion ceases to be available for carrying the current; let a fraction  $\beta$  of the collisions result in the destruction of the ion as an ionising agent, then the number of these ions which disappear from a cubic centimetre of the gas in unit time is  $\beta \frac{nv}{L}$ \*, hence the

<sup>\*</sup> We have here neglected the loss of ions due to the recombination of positive and negative ions in comparison with that due to the collision of the ions with the molecules.

excess of the ions produced over those which disappear is equal to

$$\frac{nv}{l}\left\{f(Xel)-\beta\right\}.$$

We have by the equation of continuity, if u is the average velocity of translation parallel to the axis of x,

$$\frac{dn}{dt} + \frac{d}{dx}(nu) = \frac{nv}{l} \{ f(Xel) - \beta \}....(2).$$

Now when the ions are moving so rapidly that they have sufficient kinetic energy to act as ionising agents, their velocity must be mainly due to the electric field, since when this field is absent no ionisation is produced. Hence we have approximately

$$v=u$$
.

Hence when things are in a steady state we have by (2)

$$\frac{d}{dx}(nu) = \frac{nu}{l} \{ f(Xel) - \beta \};$$

integrating we get

$$nu = Ce^{\frac{1}{l}\int_0^x (f(Xel) - \beta) dx}.$$

or if as a first approximation we regard X as constant we have

$$nu = C\epsilon^{\frac{x}{l}(f(Xel) - \beta)}$$

If the current has reached the saturation stage before ionisation begins, then nu = I when x = 0 when x is measured from the illuminated plate, hence

$$nu = I\epsilon^{\frac{x}{\tilde{l}}(f(Xel)-\beta)};$$

if d is the distance between the plates, then i the current is the value of nue when x = d, thus

$$i = e^{\int \epsilon^{\frac{d}{l}(f(Xel)-\beta)}}$$
....(3).

thus when this additional ionisation sets in, the current with a constant value of X increases with the distance between the plates; this effect has been observed by Stoletow\*. As long as the ionisation is confined to that produced at the metal plate by the ultra-violet light, the current is determined by the electric force, *i.e.* i is a function of X and not of d; when however the secondary ionisation occurs i is a function of both X and d.

<sup>\*</sup> Stoletow, Journal de Physique [2], ix. p. 468, 1890.

The point at which the secondary ionisation begins is when Xel has a certain definite value; as l the mean free path of an ion is inversely proportional to the pressure, the value of X required to start the secondary ionisation will be directly proportional to the pressure; the curves given by v. Schweidler\* for the relation between the current and electromotive force at different pressures show that his experiments are in fair agreement with this result, he only gives approximate values for the pressures, and there are hardly sufficient points determined on the curve to enable us to determine with accuracy the points at which the secondary ionisation commences; but from an inspection of his curves I should say that at a pressure of 750 mm. secondary ionisation began when the difference of potential between his plates, whose distance apart is given as between 3-5 mm., was equal to 4700 volts, at 130 mm. to 1150 volts, and at 17 mm. to about 140 volts.

It is evident that the current cannot go on continually increasing as the pressure diminishes, for in the limit when the free path gets comparable with the distance between the plates there will be very few collisions, and therefore little if any secondary ionisation; in the limit when the pressure is indefinitely reduced, the number of ions reaching the plate not exposed to the light must equal the number leaving the illuminated plate, hence with our previous notation the limiting current will be equal to *Ie*.

The value of the free path at the pressure when the current is a maximum is by equation (3) determined by finding the value of l which makes  $\{f(Xel) - \beta\}/l$  a maximum, this condition gives  $f'(Xel) Xel = f(Xel) - \beta$ , an equation to determine Xel; thus when the current is a maximum Xl has a constant value, this coincides with Stoletow's result that if  $p_m$  is the pressure at which the current is a maximum  $X/p_m$  is constant.

We alluded before to the question as to whether secondary ionisation was produced close to the surface of the metal by the corpuscles shot out from the metal through the influence of the ultra-violet light; it would seem that this point might be determined by careful measurements of the current under a constant

<sup>\*</sup> v. Schweidler, Wien. Ber. cvii. p. 273, 1899.

electromotive force at different pressures, for if it was found that the current before secondary ionisation began rose to a value greater than that corresponding to an exceedingly low pressure, it would prove that such secondary ionisation at the surface of the metal did occur. In Stoletow's experiments at various pressures the current before secondary ionisation took place did not exceed the value at zero pressure, this point however is one that would repay further examination\*.

The Photo-electric Effect depends upon the orientation of the plane of polarisation of the Light.

123. Elster and Geitel† made the very interesting discovery that when the incident light is plane polarised, the photo-electric effect, the intensity and angle of incidence being the same, is greater when the light is polarised at right angles to the plane of incidence than when it is polarised in that plane. On the Electro-magnetic Theory of Light there is in light polarised at right angles to the plane of incidence an electric force with a component normal to the reflecting surface, when the light is polarised in the plane of incidence the electric force is parallel to this surface. The most convenient way of investigating the effect of polarisation is to use a liquid surface, as it is important that the reflecting surface should be smooth, and to choose a liquid which is sensitive to ordinary light, as it is then possible to use a Nicols prism to polarise the light: the liquids used by Elster and Geitel were the liquid alloy of sodium and potassium, and amalgams of rubidium and caesium, these were placed in vessels from which the air was exhausted and the rate of escape of negative electricity observed with light incident on the surfaces at different angles. Some of the results obtained in this way are given below, data were not given to enable us to say to which stage of the curve connecting the rate of escape of negative electricity with the electromotive force the observations refer.

<sup>\*</sup> See foot-note, p. 230.

<sup>+</sup> Elster and Geitel, Wied. Ann. lii. p. 433, 1894; lv. p. 684, 1895; lxi. p. 445, 1897.

Rate of escape (i) of electricity from sodium potassium amalgam exposed to white light polarised at right angles to the plane of incidence.

Angle of incidence	i	Angle of incidence	i	Angle of incidence	i
0°	2·8	30°	17·4	60°	28·7
10	5·2	40	23·4	70	23·8
20	11·2	50	27·0	80	11·0

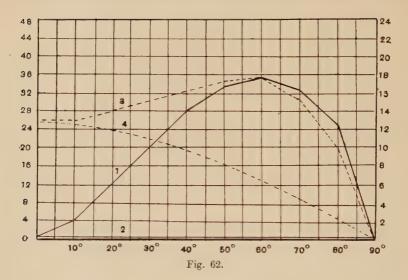
Rate of escape (i) of electricity from the same cell exposed to white light polarised in the plane of incidence.

Angle of incidence	i	Angle of incidence	i	Angle of incidence	i
3°	2·8	30°	2:65	60°	1·51
10	2·78	40	2:24	70	1·01
20	2·87	50	1:80	80	·33

Thus, except at perpendicular incidence when the two are necessarily equal, the leak caused by the light polarised in the plane of incidence is very much smaller than that caused by light polarised at right angles to this plane, and we see too that whereas in the former case the current continually diminishes as the angle of incidence increases, in the latter it increases with the angle of incidence until the latter is about 60°, after this the current decreases.

Elster and Geitel have determined how the amount of light absorbed by the metal varies with the angle of incidence for light polarised in and at right angles to the plane of incidence. The absorptions and the corresponding photo-electric currents are shown in Fig. 62. Curves (1) and (2) represent the photo-electric currents due to light polarised at right angles and in the plane of incidence respectively, curves (3) and (4) the absorptions of the light in these cases. It will be seen that in each case the current and absorption increase and decrease together, but that a given amount of absorbed light is very much more efficacious in producing discharge when its plane of polarisation is at right angles to, than

when it is in, the plane of incidence. The connection between the absorption and current is made clearer by the following considerations given by Elster and Geitel. Suppose the intensity of the incident light polarised at right angles to the plane of incidence is unity, let the amount of light absorbed when the angle of incidence is  $\phi$  be  $a_{\phi}$ , and  $a_{\phi}$  when  $\phi = 0$ , then when the angle of incidence is  $\phi$ , the component of the electric force parallel to the



surface is proportional to  $\cos \phi$ , and the energy corresponding to this component to  $\cos^2 \phi$ ; the amount of this energy absorbed will be  $a_0 \cos^2 \phi$ , hence  $a_\phi - a_0 \cos^2 \phi$  will be the energy due to the electric force at right angles to the surface absorbed by the metal. Suppose  $I_\phi$  is the current when the angle of incidence is  $\phi$ ,  $I_\phi$  the current when the angle of incidence is zero for unit intensity of light, the intensity due to the electric force parallel to the surface is  $\cos^2 \phi$ , the current due to this is  $I_0 \cos^2 \phi$ , hence the current arising from the component of the electric force perpendicular to the surface may be taken to be  $I_\phi - I_0 \cos^2 \phi$ . Now Elster and Geitel have shown that  $a_\phi - a_0 \cos^2 \phi$  and  $I_\phi - I_0 \cos^2 \phi$  are approximately proportional to each other; this is shown by the two curves in Fig. 63, which represent the variation of the two quantities with the angle of incidence. The continuous line represents the variation of the current, the dotted line that of the absorption.

If we take the view that the photo-electric effect is due to the emission of negatively electrified corpuscles from the metal, we can explain the influence of the orientation of the planes of polarisation as follows. We may suppose that the energy from the light absorbed by the metal goes into some of the corpuscles, giving them sufficient kinetic energy to escape from the metal, just as they are able to do at a very high temperature. These corpuscles have acquired from the ultra-violet light very much

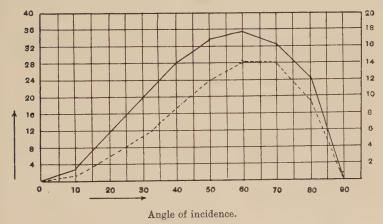


Fig. 63.

more kinetic energy than is possessed by a molecule of a gas at the temperature of the metal; thus every collision a corpuscle makes with the molecules of the metal will result in a loss of kinetic energy, so that if it is to escape from the metal it is important that it should make as few collisions as possible before reaching the surface, *i.e.* that it should move approximately at right angles to the surface. When the light is polarised at right angles to the plane of incidence there is a component of the electric force at right angles to the surface which will direct some of the corpuscles in this direction, when however the light is polarised in the plane of incidence the electric force is parallel to the surface and tends to make the corpuscles move parallel to the surface instead of towards it; thus the corpuscles have in order to escape to make more collisions in this case than the former, and so are less likely to reach the surface with sufficient energy to escape from it.

### Influence of Temperature on the Photo-electric Effect.

124. The influence of the temperature of the metal on the photo-electric effect has been investigated by Hoor\*, Stoletow+, Elster and Geitelt, Righis, and Zeleny Hoor found that the sensitiveness of a zinc plate to light diminished when the temperature was raised from 18° to 55°. Stoletow found on the other hand that raising the temperature to 200° C. increased the sensitiveness, Elster and Geitel that an alteration of temperature had no effect on zinc. Righi found that the positive charge given by light to a previously uncharged plate was greater when the plate was hot than when it was cold: we must remember that a blast of air blowing across the plate increases the positive charge so that part of the effect observed by Righi may have been due to air currents set up by the hot plate. In considering the interpretation of these seemingly discrepant results we must remember that the circumstances which affect the sensitiveness of the metal to the light will depend very much upon the strength of the field. Thus supposing we are dealing with a strong field and the gas surrounding the metal is at an exceedingly low pressure, the photo-electric current is saturated and measures the number of corpuscles given off from the metal in unit time; measurements of the effect of temperature in this case would admit of a perfectly definite interpretation, but when the gas is at a high pressure and the strength of the field is weak, i.e. when we are working on the earlier part of the curve connecting the current and the electromotive force, then the interpretation of the effect of temperature is ambiguous, for the current at this stage depends not only upon the rate of emission of the corpuscles, but also upon the velocity of the ions through the gas. Now the increase in temperature may alter the density of the gas, and hence the velocity of the ions through it, and it would require further experiments to disentangle this effect of the velocity of the ions from the effect on the rate of emission of the corpuscles from the plate. The experiments

<sup>\*</sup> Hoor, Wien. Berichte, xcvii. p. 719, 1888. Exner's Rep. xxv. p. 91, 1889.

<sup>†</sup> Stoletow, Comptes Rendus, cviii. p. 1241, 1889.

<sup>‡</sup> Elster and Geitel, Wied. Ann. xlviii. p. 625, 1893.

<sup>§</sup> Righi, Atti Ist. Ven. vii. Mem. 11.

<sup>||</sup> Zeleny, Physical Review, xii. p. 321, 1901.

of Elster and Geitel on the effect of temperature on the current from a potassium surface in a good vacuum are not open to this objection, as the effect of the gas is eliminated, and in this case they found an increase in the current of about 50 per cent. when the temperature was increased from 20° to 50°: from some experiments made by the writer it appears that when the temperature is raised considerably higher, say to 200°, there is a very great increase in the current from the alkali metals, and that these are very much more sensitive to light at high temperatures than they are at low.

Zeleny, who measured the current from platinum and iron exposed to ultra-violet light and surrounded by air at atmospheric

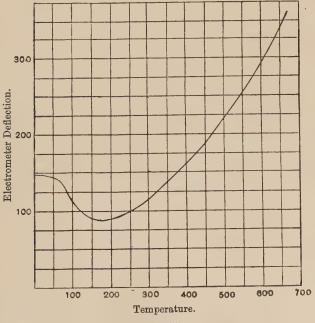


Fig. 64.

pressure, found that from platinum the current first decreased as the temperature increased, reached a minimum, and then increased with the temperature as far as the highest temperature used. The results showed a curious hysteresis effect in the currents obtained, when the metal was cooling they were greater than those at the same temperature when the wire was getting hotter. These

results are indicated in the curves shown in Fig. 65, where (i) represents the currents corresponding to continuously increasing temperatures, (ii) those for continuously decreasing temperatures; (iii) those for increasing temperatures, and (iv) for decreasing temperatures when the wire was cooled to the temperature of the room between each observation. These observations show that heating the wire produces some change in the surface, possibly in the amount of gas condensed upon it or absorbed by the metal, from which it only slowly recovers. With iron the minimum current is not nearly so clearly marked as with platinum, nor is there so great a difference between the curves for increasing as

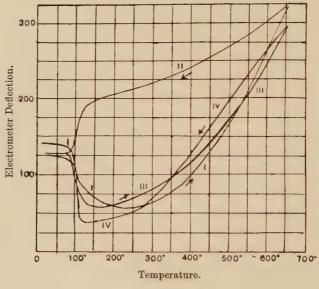


Fig. 65.

those for decreasing temperature; on the other hand the photoelectric current increases more rapidly with the temperature for iron than for platinum, the current at 700° C. being for iron about 40 times the current at 15° C., while for platinum the current at 700° C. was only about 2.5 times that at 15° C.

Zeleny also investigated whether, if the metal were raised to a temperature just below that at which it would begin to give off positive ions in the dark, it could be made to give off positive ions by the incidence upon it of ultra-violet light; the positive ions were however not produced at a lower temperature in the light than in the dark. Nor when the metal was raised to the temperature at which the positive ions were produced was the rate of production increased by the incidence of ultra-violet light.

The experiments of Elster and Geitel and Zeleny seem to establish the fact that the photo-electric effects of metals are greater at a high temperature than at a low one. This is what we should expect if we take the view that the photo-electric effect is due to the acquisition by the corpuscles in the metal under the action of the ultra-violet light of sufficient kinetic energy to enable them to escape from the metal. The higher the temperature the greater would be the initial kinetic energy possessed by the corpuscles, and the smaller the increment required to enable them to move fast enough to escape from the metal.

Nature of the ions produced by the action of ultra-violet light on metals.

125. The experiments made by the author and Lenard (see p. 107) show that in high vacua metals when illuminated with ultra-violet light give out corpuscles, i.e. bodies whose mass is only about \$\frac{1}{1000}\$ of that of the hydrogen atom; when however the metal is surrounded by gas the corpuscles soon strike against the molecules, get attached to them and have to drag them along with them as they move under the action of the electric field. The velocity of the negative ions through different gases has been measured by Rutherford (see p. 52), who showed that the velocity of the ion did not depend upon the nature of the metal on which the light fell, but that it did depend on the nature of the gas through which the ion had to travel, and that the velocity through any gas of the negative ion produced by ultraviolet light was very approximately the same as that of the ion produced by Röntgen rays through the same gas.

The diminution of the photo-electric effect produced when the pressure of the gas is low by a transverse magnetic field, which was discovered by Elster and Geitel\*, has already been discussed on page 107.

The photo-electric effect does not persist after the light is cut off. Stoletow\*, who made a series of experiments on this point, could not obtain any evidence that there was any finite interval between the incidence of the light and the attainment of the full photo-electric effect, or between the eclipse of the light and the total cessation of the effect, and he showed that the interval must at any rate be less than  $\frac{1}{1000}$  of a second.

126. Connection between photo-electric effects and the fluorescence and ionisation of solutions. G. C. Schmidt+ made a series of experiments on this subject, with the result that there was no clear evidence of any intimate relation between photo-electric effects, ionisation and fluorescence: for while in fuchsine there seemed to be clear indications of a connection between ionisation and photo-electric effects-since aqueous solutions of fuchsine are photo-electric, while solutions in alcohol and acetone are not, and fuchsine is ionised in water and not in the other solvents—the results with eosine seemed decisive against this connection, as the addition of neutral salts, such as potassium iodide or sodium chloride, destroys the ionisation, while in aqueous solutions it has no influence upon the photo-electric effects. Again, magdala red fluoresces in alcohol, amyl-alcohol and acetone, the first two solutions are photo-electric, the last is not. Salts which undergo decomposition in the light such as the haloid salts of silver are strongly photo-electric.

In the case of water a change in the physical state seems to be accompanied by a change in the photo-electric properties, as dry ice was found by Brillouin<sup>†</sup> to be photo-electric, while water in the liquid state is not.

The opinion has been advanced by Cantor§ and Knoblauch||, that the photo-electric effect depends upon oxidation, on the ground that the substances, elementary and compound, which exhibit this effect are those which combine with oxygen; it is however, I think, necessary to distinguish between the *power* of

<sup>\*</sup> Stoletow, Aktinoelektrische Untersuchungen, Physikalisch. Revue, i. p. 725, 1892.

<sup>+</sup> G. C. Schmidt, Wied. Ann. lxiv. p. 708, 1898.

<sup>‡</sup> Brillouin, Écl. Électr. xiii. p. 577, 1897.

<sup>§</sup> Cantor, Wien. Sitzungsber. 102, p. 1188, 1893.

<sup>||</sup> Knoblauch, Zeit. f. Physikalische Chemie, xxix. p. 527, 1899.

combining with oxygen and the act of combination. We should expect the photo-electric substances to be oxidisable, as they lose readily negative corpuscles, and thus get positively charged and in a fit state to combine with an electro-negative substance like oxygen; there is no evidence however that the presence of oxygen is necessary for the photo-electric effect, in fact the evidence the other way seems quite conclusive, for substances like rubidium and potassium enclosed in highly exhausted vessels seem to retain their photo-electric power indefinitely, and any trace of oxygen originally present would soon be absorbed by the metals.

## CHAPTER XI.

## IONISATION BY RÖNTGEN RAYS.

127. WE shall in this chapter mainly confine our attention to the ionising properties of the rays, leaving for future consideration the manner of their production and a discussion of their nature; it will however be convenient to enumerate some of their most important properties. Röntgen\* found in 1895 that very remarkable effects occurred in the neighbourhood of a highly exhausted tube through which an electric discharge was passing; the exhaustion of the tube being so great that a vivid green phosphorescence appeared on the glass. He found that a plate covered with a phosphorescent substance such as potassium-platino-cyanide became luminous when placed near the tube, and that a thick plate of metal cast a sharp shadow when placed between the tube and the plate; while light substances, such as thin aluminium, cardboard, wood, cast but slight shadows, showing that the agent which produced the phosphorescence on the plate could traverse with considerable freedom bodies which are opaque to ordinary light. As a general rule the greater the density of a substance the more opaque it is to this agent; thus the bones are much more opaque to this effect than the flesh, so that if the hand is placed between the discharge tube and the plate the outlines of the bones are distinctly visible in the shadow cast on the screen, or if a purse containing coins is placed between the tube and the plate the purse itself casts but little shadow, while the coins cast a very dense one. Röntgen showed that the agent, now called Röntgen rays, producing the phosphorescence on the plate is propagated in straight lines, and is not bent in passing from one medium to

<sup>\*</sup> Röntgen, Wied. Ann. lxiv. p. 1, 1898 (reprinted from the original paper in the Sitzungsberichte der Würzburger. Physik. Med. Gesellsch. 1895).

another; there is thus no refraction of the rays. The rays affect a photographic plate as well as a phosphorescent screen and shadow photographs can readily be taken: the time of exposure depends on the intensity of the rays, and this depends on the discharge through the tube and on the substances traversed by the rays in their passage to the plate; the time of exposure required to produce a photograph may vary from a few seconds to several hours. The power of the rays to penetrate obstacles in their path varies very much with the condition of the discharge tube from which they originate; when the pressure in this tube is not very low, and the potential difference between its electrodes consequently comparatively small, the rays have but little penetrating power and are readily absorbed; such rays are called 'soft rays.' If the exhaustion of the tube is carried much further, so that the potential difference between the electrodes is greatly increased, the Röntgen rays have much greater penetrating power and are called 'hard rays.' With a very highly exhausted bulb and a large induction coil it is possible to get rays which will produce appreciable effects after passing through sheets of brass or iron several millimetres thick. The difference in penetrating power is well shown by observing the changes which take place in the shadow of a hand on a phosphorescent screen, as the pressure of the gas in the discharge tube is gradually reduced. When first the rays appear they are so 'soft' that they are stopped by the flesh as well as the bones, so that the bones are very indistinctly seen; when the exhaustion proceeds further the rays get harder, and are able to penetrate the flesh but not the bones. At this stage the difference between the shadow of the flesh and the bones is most distinct; when the exhaustion proceeds further the rays get so hard that they are able to penetrate the bones as well as the flesh and the shadow again becomes indistinct. Not only may the rays from different discharge tubes be different, but even the same bulb may emit at the same time rays of different degrees of hardness. The property by which it is most convenient to identify a ray is its hardness, and this is conveniently measured by the amount of absorption when it passes through a layer of aluminium or tinfoil of given thickness. Now in some experiments made by the writer and McClelland\* on the absorption

<sup>\*</sup> J. J. Thomson and McClelland, Proc. Camb. Phil. Soc. ix. p. 126, 1899.

produced when the rays passed through one layer of tinfoil after another, it was found that the absorption produced by the first few sheets of tinfoil traversed by the rays was much greater than that due to the same number of sheets after the rays had already travelled through several sheets of tinfoil. This shows that some of the rays are readily absorbed by the tinfoil while others pass through with much greater facility, thus the first few layers of tinfoil would stop the first kind of rays while the remainder pass through with comparatively little absorption. McClelland showed that if he took plates of different metals, the thickness of the plates being chosen so that they gave the same absorption for the rays from one tube, they would not necessarily give the same absorption for the rays from another.

The Röntgen rays when they pass through a gas make it a conductor of electricity, they ionise the gas\*: the number of ions produced in one second in one cubic centimetre of the gas by rays of given intensity depends upon the pressure of the gas, the nature of the gas and its temperature.

128. Effect of Pressure. Perrin + has shown that the rate of production of ions per cubic centimetre by rays of given intensity is proportional to the pressure of the gas. He proved this by showing that the saturation current through a given volume of gas was proportional to the pressure: the current passed between two large plates of metal, care being taken that the rays did not fall upon the plates; this precaution is necessary, because as we shall see when the Röntgen rays fall upon metal secondary rays are produced which ionise the gas, and complicate the effects; in addition to this precaution it is necessary to arrange the electric field so that all the gas exposed to the rays-or at least all of it from which the ions can move to the electrodes-is under the influence of an electric field strong enough to produce saturation, for unless saturation is reached throughout the whole of the gas the current will depend upon the velocity of the ions under the electric field as well as upon the number of ions produced; as the velocity of the ions increases as the pressure diminishes the unsaturated current will diminish less rapidly with the density

<sup>\*</sup> J. J. Thomson, Camb. Univ. Reporter, Feb. 4, 1896. Benoist and Harmozescu, C. R. exxii. p. 235, 1896. Righi, Acc. dei Lincei (5), v. p. 143, 1896.

<sup>+</sup> Perrin, Annales de Chimie et de Physique [7], xi. p. 496, 1897.

than the saturated one. In fact when the electric field is feeble the current will increase as the pressure diminishes, for if n is the number of positive or negative ions per cubic centimetre, q the number of ions produced in one second in a cubic centimetre, then (see p. 15)  $n = (q/\alpha)^{\frac{1}{2}}$ ; the current under a small electric force X is equal to neX (u+v), where e is the charge on an ion, u and v the velocities of the positive and negative ions under unit electric field. Now n is proportional to  $\sqrt{q}$ , and therefore to  $\sqrt{p}$  p being the pressure of the gas, since (see p. 19)  $\alpha$  is independent of p, while u and v are proportional to 1/p; the current under small electric forces will vary as  $1/\sqrt{p}$ .

129. Ionisation of Different Gases. When Röntgen rays of the same intensity pass through different gases at the same pressure the amount of ionisation depends greatly upon the composition of the gas; the number of ions produced, measured by the saturation current, is least in hydrogen, and for the gases hitherto tried greatest in the vapour of methyl iodide: it is also exceedingly large for mercury vapour: the relative values of q—the number of ions produced in one second in a cubic centimetre of the gas at atmospheric pressure and temperature—are given in the following table. The number for air is taken as unity.

		q				q	
Gas	Perrin *	Ruther- ford †	Thom- son ‡	Gas	Perrin	Ruther- ford	Thom- son
$\begin{array}{c} H_2\\N_2\\O_2\\CO_2\\CO\\NO\\N_2O\end{array}$	1·34  1·3	 	·33 ·89 1·1 1·4 ·86 1·08 1·47	$C_2N_2 \\ C_2H_2 \\ H_2S \\ SO_2 \\ HCl \\ Cl_2 \\ NH_3$	6 8 	6 4 11 18	1.05 1 6 6.4 8.9 17.4 1?

We see that though the results of different observers are in fair agreement for most gases, for hydrogen they are very discordant. We must remember that different observers used rays of different degrees of hardness, and that it is probable that the

<sup>\*</sup> Perrin, Annales de Physique et de Chimie [7], xi. p. 496, 1897.

<sup>†</sup> Rutherford, Phil. Mag. v. 43, p. 241, 1897.

<sup>‡</sup> J. J. Thomson, Proc. Camb. Phil. Soc. x. p. 10, 1900.

relative ionisation in two gases depends upon the kind of rays used to ionise them. The gases in which the ionisation is large have also large refractive indices, it does not however seem that a large refractive index necessarily implies large ionisation; for example, the refractive index of acetylene C<sub>2</sub>H<sub>2</sub> as determined by Mascart is very nearly the same as that of sulphuretted hydrogen H<sub>o</sub>S, yet the ionisation in the H<sub>o</sub>S is about six times that in C<sub>o</sub>H<sub>o</sub>. ionisation by the Röntgen rays does not seem to be closely connected with the density of the gas; thus the density of HS is a little greater than that of O2 and considerably less than that of CO<sub>2</sub>, yet the ionisation in either of these gases is small compared with that in H.S. In other cases of ionisation such as that due to radiation from some radio-active substances, or to the passage of cathode rays through a gas, we shall see that the ionisation is much more closely connected with the density of the gas, being (except in the case of hydrogen) directly proportional to the density.

130. The writer\* pointed out that the measurements given in the above table indicate that the ionisation of a gas is approximately an additive property, i.e. if 2[A] is the value of q for a gas  $A_2$ , 2[B] the value for a gas  $B_2$  and so on, then the value of q for a gas  $A_1B_mC_n$  will be l[A] + m[B] + n[C]. Thus if we use the numbers given in the third column of the preceding table for  $H_2$ ,  $N_2$ ,  $O_2$ ,  $CO_2$ ,  $SO_2$ , and  $Cl_2$  to determine the values of 2[H], 2[N], etc., we find

$$[H] = .165,$$
  $[C] = .3,$   $[N] = .445,$   $[S] = 5.3,$   $[O] = .55,$   $[Cl] = 8.7;$ 

if we use these numbers to calculate the ionisation in the other gases in the table using the additive rule we get the following results.

Gas	Ionisation observed	Ionisation calculated	Gas	Ionisation observed	Ionisation calculated
$\begin{array}{c} \text{CO} \\ \text{NO} \\ \text{N}_2\text{O} \\ \text{C}_2\text{N}_2 \end{array}$	*86 1*08 1*47 1*05	·85 ·995 1·44 1·49	$\begin{array}{c} \mathrm{C_2H_2} \\ \mathrm{H_2S} \\ \mathrm{HCl} \\ \mathrm{NH_3} \end{array}$	1 6 8-9 1	*93 5*63 8*86 *94

<sup>\*</sup> Loc. cit.

Thus except in the case of  $C_2N_2$  the agreement is within the limits of the errors of experiment.

Connection between the absorption of the rays by a gas and the ionisation produced in a gas by the rays. The rays are absorbed by gases through which they pass, the amount of this absorption has been measured by Rutherford\*, who used for this purpose the apparatus represented in Fig. 66. Two large and similar conical

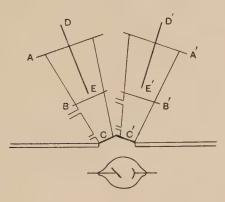


Fig. 66.

vessels ABC, A'B'C', much larger at the top than at the bottom, were placed in such positions that the axis of each cone passed as nearly as possible through the anode of the tube producing the Röntgen rays. The upper parts of the vessels AB, A'B' were made of lead, and were separated from the lower portions, which were made of glass, by thin plates of ebonite, similar plates covered the ends of the glass cylinders at C and C', so that the vessels BC, B'C' were air-tight and could be exhausted when required. The intensities of the rays after they had passed through the glass cylinders were measured by determining the saturation currents through the lead cylinders AB, A'B'. Insulated wires DE, D'E' were used as the electrodes, these were connected with opposite pairs of quadrants of an electrometer, both initially charged to the same potential. The outsides of the vessels AB, A'B' were connected with the earth. The position of the bulb giving the rays was adjusted so that when the glass vessels BC, B'C' were filled with air at the same pressure

<sup>\*</sup> Rutherford, Phil. Mag. v. 43, p. 241, 1897.

or

the needle of the electrometer remained at rest when the rays were passing through the vessel; this showed that the potentials of each pair of quadrants were falling at the same rate, and therefore that the currents through the vessels AB, A'B' were equal. If the gas were removed from one of the vessels BC, B'C' or another gas introduced, the balance was disturbed, thus showing the absorption of the rays by the gas in the vessel. If we assume that the energy absorbed when the rays pass through unit length of the gas is proportional to the energy of the rays I and equal to  $\lambda I$ , then the change  $\delta I$  in the intensity when the rays traversed a distance  $\delta x$  is given by the equation

$$\delta I = -\lambda I \delta x,$$

$$I = I_0 e^{-\lambda x},$$

where  $I_0$  is the intensity of the rays when x=0. Thus if l is the length of path of the rays through the vessel BC, the ratio of the intensity of the radiation in AB when BC is full of a gas whose coefficient of absorption is  $\lambda$ , to the intensity when BC is exhausted is equal to  $\epsilon^{-l\lambda}$ , in this way  $\lambda$  can be determined. Rutherford found that for air  $\lambda$  is about  $10^{-3}$ , so that the rays lose about 1 per cent. of their energy in passing through 10 cm. of air at atmospheric pressure; about 7 cm. of mercury vapour at atmospheric pressure and at the temperature of boiling mercury reduced the intensity of the rays to about  $\frac{1}{2}$ . The values of  $\lambda$  for different gases are given in the following table. The third column of this table contains the relative values of q—the number of ions produced in each volume in unit time by rays of equal intensity.

Gas	λ	q	Gas	λ	q
Hydrogen Air Oxygen Nitrogen Coal gas Carbon dioxide	oo1	·5 1 1·2 ·9 ·8 1·2	Sulphur dioxide Sulphuretted hydrogen Hydrochloric acid Chlorine Mercury vapour Methyl iodide	·0025 ·0037 ·0065 ·0095 ·1 ·07	4 6 11 18 

These numbers show that good conductors under the rays are good absorbers of the radiation: if the conductivity were proportional to the radiation, *i.e.* if  $q/\lambda$  were constant, then if the

whole of the radiation were absorbed by a gas the number of ions produced would be independent of the nature of the gas. For if  $I_0$  is the initial intensity of the rays the intensity after they have passed through a distance x of the gas is  $I_0\epsilon^{-\lambda x}$ , hence the number of ions produced in unit time in the space dx is proportional to  $qI_0\epsilon^{-\lambda x}$ , thus the total number of ions produced in the gas in unit time is proportional to

$$\int_0^\infty q I_0 \epsilon^{-\lambda x}$$

and this is equal to  $qI_0/\lambda$ : thus if  $q/\lambda$  is the same for all gases the total number of ions produced by rays of given intensity will be the same. The numbers given above for  $q/\lambda$  show considerable variations in the different gases: the discrepancies however chiefly occur in the gases for which  $\lambda$  is very small, and in which the errors of experiment are necessarily large.

Rutherford and McClung\* have recently made very careful determinations of the values of  $\lambda$  for carbonic acid and air; they found the ratio for the two gases was 1.59, for the ratio of the currents they found 1.43, but they consider the current through the carbonic acid was not quite saturated. I found the ratio of the currents through the two gases to be 1.53, which is very nearly the ratio of the absorption. The value of  $\lambda$  depends upon the character of the rays, for hard rays it is very much smaller than for soft ones, thus the value of  $\lambda$  for air in Rutherford and McClung's experiments was only about one-quarter of the value in Rutherford's earlier experiments in which softer rays were used. In the case of the radiation from uranium—which is much more easily absorbed than Röntgen rays—Rutherford† has shown that when all the radiation is absorbed by a gas, the total amount of ionisation is approximately the same in all gases.

The absorption depends upon the pressure of the gas: using the vapour of methyl-iodide, Rutherford has shown that down to a pressure of a quarter of an atmosphere the absorption is proportional to the pressure.

131. Benoist; concludes from experiments on the vapours of bromine and iodine, of ethyl-bromide and methyl-iodide that the

<sup>\*</sup> Rutherford and McClung, Phil. Trans. A, exevi. p. 25, 1901.

<sup>+</sup> Rutherford, Phil. Mag. v. 47, p. 109, 1899.

<sup>#</sup> Benoist, Journal de Physique [3], x. p. 653, 1901.

absorption produced by a given mass of a substance is independent of its physical state; that, for example, the vapour of a volatile liquid or solid absorbs the same amount of radiation when in the gaseous state as when condensed into a solid or liquid.

Benoist introduces a quantity which he calls the coefficient of transparency of the substance; it is the weight in milligrammes of a prism of the substance on a base one square centimetre in area which produces the same absorption as a standard prism of paraffin-wax 75 mm. long, when the rays travel along the axes of the prisms. He has proved the very important law, that if we have a mass M of a substance whose transparency is E made up of masses  $M_1, M_2, M_3...$ , of substances whose coefficients of transparency are  $E_1, E_2, E_3...$ , then whether the substances are mechanically mixed or in a state of chemical combination

$$\frac{M}{E} = \frac{M_1}{E_1} + \frac{M_2}{E_2} + \frac{M_3}{E_3} + \dots$$
 (1).

I think the meaning of this law is made clearer by the introduction of a quantity which we may call the molecular absorption of the substance, i.e. the absorption produced by one molecule of the substance, and which is connected with the Benoist coefficient as follows: suppose that the mass of a molecule is m, and that in Benoist's prisms there are N molecules, then Nm = c.E where c is a constant; by the definition of E these N molecules produce a given amount of absorption; hence if a is the absorption due to one molecule Na = C where C is a constant; hence we see that

$$\frac{m}{E} = \lambda a,$$

where  $\lambda$  does not depend on the nature of the substance. Let us now express Benoist's law in terms of the absorption a. If there are  $N_1$  molecules of the first substance,  $N_2$  of the second, and so on

$$\begin{split} M_1 &= N_1 m_1, \quad M_2 &= N_2 m_2, \quad M = N m, \\ \frac{M}{E} &= N \lambda a \ ; \end{split}$$

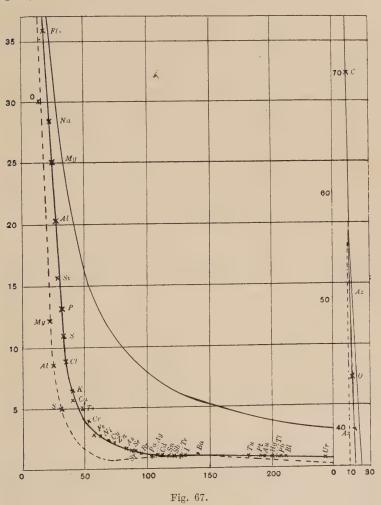
and

thus equation (1) becomes

$$Na = N_1 a_1 + N_2 a_2 + N_3 a_3 + \dots$$

This is equivalent to the statement that the absorption of any substance is equal to the sum of the absorptions of the individual

molecules in that substance, the absorption due to any molecule being independent of the nature of the chemical compound of which it forms a part or its physical state. Benoist states that the absorption does not depend upon the temperature. The absorption of a body for the Röntgen rays is thus an additive property.



There is a very close connection between the absorption of an element and its molecular weight; this is shown by the curve in Fig. 67 (taken from Benoist's paper) in which the ordinates

represent the equivalents of transparency of the elements, the abscissæ the molecular weight; it will be seen that the curve is quite a smooth one, in every case the transparency diminishes as the molecular weight increases. From this it follows that the molecular absorption increases with the molecular weight. Having got the curve connecting the transparency with the molecular weight, it is evident that we have the means of determining its molecular weight by measuring its transparency to Röntgen rays when in a pure state or when combined with elements whose transparency is known. Benoist has applied this method to determine the molecular weight of indium.

From Benoist's results I have calculated the following relative values of a for some of the elements which often occur in gaseous compounds.

Substance	a	Substance	a
$egin{array}{c} O_2 \\ N_2 \\ C_2 \end{array}$	·36 ·27 ·17	$egin{array}{c} \mathbf{S}_2 \\ \mathbf{Cl}_2 \\ \mathbf{Br}_2 \end{array}$	2·8 4 47

Knowing a for these gases we can calculate the absorptions of the gases measured by Rutherford (see page 250), the results are given in the following table:

Gas	a (Benoist)	λ (Rutherford)	<i>a</i> /λ
$\begin{array}{c} O_2\\ CO_2\\ SO_2\\ H_2S\\ HCl\\ Cl_2 \end{array}$	36 45 1.76 1.4 2	·001 ·001 ·0025 ·0037 ·0065 ·0095	360 450 700 378 301 420

In calculating the numbers in the second column I have neglected the absorption due to the hydrogen in the compound, as this is too small to be accurately determined. Benoist showed that the relative values of a depended to some extent upon the nature of the rays; taking this into account Rutherford's results are in fair accordance with Benoist's law except in the case of  $SO_2$ .

The question arises whether the energy absorbed by the gas is wholly accounted for by the work spent in ionising the gas or whether part of the energy of the rays is directly transformed into heat and energy in the gas without the intervention of ionisation: if the ions are allowed to recombine, the work spent in ionisation will ultimately appear as heat energy in the gas; this would however not necessarily be the case if the ions were driven out of the gas by a strong electric field. The evidence is, I think, in favour of the view that the ionisation of the gas is only accountable for a small part of the loss of energy. Rutherford and McClung\* have calculated the work necessary to ionise a molecule of the gas on the assumption that all the loss of energy in the rays was due to the ionisation of the gas; on this hypothesis they found the work necessary to ionise a molecule of air was equal to the work done on the ionic charge when it fell through a potential difference of about 175 volts, this is very much larger than the value of the same quantity, about two volts, obtained by H. A. Wilson and Townsend (see p. 190) by different considerations. Combining these results we conclude that only about 1/80 of the energy of the rays is expended in the ionisation of the gas, the rest being converted into heat.

Variation of the ionisation of a gas with the temperature.

132. This was investigated in the case of air by Perrin† who showed that if the pressure of the gas was kept constant, then between the temperatures  $-12^{\circ}$  and  $+145^{\circ}$  C. the total ionisation was independent of the temperature; as the density of the gas when the pressure is constant varies inversely as the absolute temperature, and, as we have seen, the amount of ionisation is proportional to the density, it follows that the amount of ionisation in a given mass of gas is directly proportional to the absolute temperature.

It is very desirable that further experiments should be made on the variation of the ionisation of different gases with the temperature, as this variation has a direct bearing on the question as to what is the condition of the molecules which are ionised by the Röntgen rays. We must remember that it is only an

<sup>\*</sup> Rutherford and McClung, Phil. Trans. exevi. p. 25, 1901.

<sup>+</sup> Perrin, Annales de Chimie et de Physique [7], xi. p. 496, 1897.

exceedingly small fraction of the molecules which are ionised by the rays; even when the ionisation is exceptionally large the proportion of the number of free ions to the number of molecules of the gas is less than 1 to 10½. Thus if all the molecules of the gas are equally exposed to the rays, since the ionisation is confined to an exceedingly small fraction of the number of molecules the molecules which are ionised must be in some state very far removed from the average condition of the molecules. One supposition which naturally suggests itself is that it is only those molecules which possess an amount of kinetic energy exceeding a certain value which get ionised by the rays: the following investigation however shows that in this case the ionisation ought to vary much more rapidly with the temperature than is consistent with Perrin's results.

For according to the Kinetic Theory of Gases the number of molecules in a cubic centimetre which have velocities between c and c+dc is equal to

$$\frac{4}{\sqrt{\pi}} N\theta^{-\frac{3}{2}} \epsilon^{-\frac{mc^2}{\theta}} c^2 dc,$$

where N is the whole number of molecules per unit volume,  $\theta$  the absolute temperature and m the mass of a molecule of the gas, hence if n is the number of molecules which have velocities greater than c,

 $n = \frac{4}{\sqrt{\pi}} N \theta^{-\frac{3}{2}} \int_{c_1}^{\infty} \epsilon^{-\frac{mc^2}{\theta}} c^2 dc,$ 

or putting  $c^2 = \theta \omega^2$ ,

$$n = \frac{4}{\sqrt{\pi}} N \int_{\frac{C_1}{\sqrt{\alpha}}}^{\infty} e^{-m\omega^2} \omega^2 d\omega ;$$

hence we have

$$\frac{dn}{d\theta} = \frac{2}{\sqrt{\pi}} N \epsilon^{-\frac{mc_1^2}{\theta}} \frac{c_1^3}{\theta^{\frac{9}{2}}}.$$

Now since the number of molecules ionised is an exceedingly small fraction of n, if these are the molecules having a velocity greater than  $c_1$ , then  $e^{-\frac{mc_1^2}{\theta}}$  must be very small, but when this is the case  $dn/d\theta$  will increase very rapidly with  $\theta$ ; thus suppose for a moment that  $e^{-\frac{mc_1^2}{\theta}}$  is equal to  $10^{-12}$ , then if we double  $\theta$  the

value of  $dn/d\theta$  at the higher temperature would be about 120,000 times its value at the lower, while according to Perrin's result the temperature coefficient of the ionisation is constant: hence we conclude that the few molecules that are ionised cannot owe their ionisation to the possession of an abnormal amount of kinetic energy; a similar objection would apply to the ionisation being due to any property of the molecule whose frequency was given by the Maxwell-Boltzmann Law of Distribution.

Another view that at first sight appears as if it might explain the small amount of ionisation is that this is not due to the direct action of the Röntgen rays on the molecules, but that these rays act on the free ions, which as the phenomenon of spontaneous ionisation shows are always present in small numbers, even when the gas is in its normal state; the rays giving to these ions sufficient kinetic energy to enable them to ionise the molecules of the gas against which they strike. To express the results of this hypothesis in an analytical form, let us suppose that the number of free positive or negative ions per cubic centimetre is n, and that in consequence of the kinetic energy given by the rays to an ion, each ion produces  $\omega$  other ions per second, let the number of ions which recombine in one second be  $\alpha n^2$ , and let  $\beta$  be the number of ions produced per second from the spontaneous ionisation of the gas, then when things are in a steady state we have

$$\omega n + \beta - \alpha n^2 = 0,$$

$$n = \frac{\omega}{2\alpha} + \sqrt{\frac{\beta}{\alpha} + \frac{\omega^2}{4\alpha^2}}.$$

or

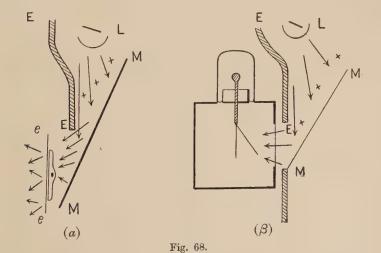
Since the number of ions produced by the rays is large compared with that— $\sqrt{\beta/\alpha}$ —due to the spontaneous ionisation  $\beta/\alpha$  must be small compared with  $\omega^2/4\alpha^2$ , and we have approximately  $n=\omega/\alpha$ , thus we should have a definite value for the number of ions in a cubic centimetre of the gas. This view however leads to a result which is not in accordance with the results of observation, for the saturation current for a cubic centimetre of the gas is proportional to the number of ions produced in one second in a cubic centimetre of the gas, i.e.  $\omega n$ . Now this number being proportional to n, the number of free ions, should be less in a strong electric field than in a weak one, for in a strong field the life of the ion is shorter than it is in a weak one, as it is rapidly driven out of the

gas against the electrodes; hence if the view we are discussing were the true one, the current through a gas when the electric field is strong ought to diminish as the strength of the field increases; as this is not the case we conclude that the ionisation cannot be produced in the way we have been considering.

Other possible explanations of the small number of molecules dissociated by the rays are (1) that the rays are of such a kind that only a small fraction of the molecules are exposed to the full force of their influence: that if for example we consider a plane at right angles to the direction of propagation of the rays the energy is not distributed uniformly over this plane, but that the distribution of energy has as it were a structure, although an exceedingly fine one, places where the energy is large alternating with places where it is small, like the mortar and bricks in a wall; thus if the places where the energy is intense enough to produce ionisation of a molecule occupied but a small fraction of the area of the plane at right angles to the rays, the rays would be able to pass through a gas and yet only a small fraction of the molecules would be exposed to their maximum influence, just as is the case when a beam of cathode rays passes through the gas; we shall return to this point when we consider the nature of the Röntgen rays. Another view which might be taken is that all the molecules of a gas, even though this gas may be like hydrogen an element, are not of the same kind, and that mixed with the ordinary molecules we have a few which are of such a kind as to be very easily ionised, and that the number of molecules of this kind, which are practically molecules of a different gas, is not given by Maxwell's law of distribution. The idea that even a gas is not uniform in composition, but contains, as it were mixed with it, small quantities of other gases—not necessarily as impurities due to its method of preparation but as an essential constituent of itmay appear at first stating so opposed to the ordinary facts of chemistry as not to be worthy of discussion. We may however point out that the quantities of such gases, if we may take the ionisation as their measure, are so small as to be utterly beyond the power of chemical analysis to detect, so that it cannot be by chemical considerations that the truth or falsehood of this hypothesis can be decided.

133. Secondary Röntgen radiation. When the Röntgen rays pass through a substance they cause it to emit Röntgen rays—

called secondary rays—which in many cases at any rate are different in character from the rays—primary rays—which produced them. These secondary rays are produced by solids, liquids and gases. Perrin\* observed that when the rays struck a metal plate, more ionisation was produced than if rays of the same intensity passed through the air without coming into contact with the plate. He arranged two pairs of parallel plates so that the same volume of gas was exposed to rays of the same intensity between each pair of plates, in the one pair however the rays passed between the plates without touching the metal, while in the second pair the rays were incident normally on one of the plates; he found that the saturation current was always greater for the second pair of plates than for the first, the excess depending on the metal struck by the rays. If this plate were made of gold, zinc, lead or tin, the difference was considerable, if it was made of aluminium it was only small, while it was quite inappreciable if the plate were wet with water, alcohol or petroleum.

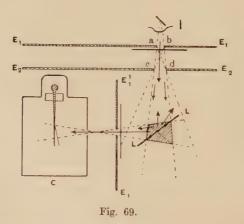


Sagnac† has made some experiments which show very clearly the existence of these secondary rays; the method he used is shown in Fig. 68 a and  $\beta$ ; in the experiment represented in

<sup>\*</sup> Perrin, Annales de Chimie et de Physique [7], xi. p. 496, 1897.

<sup>+</sup> Sagnac, ibid. [7], xxii. p. 493, 1901.

Fig. 68 a the secondary rays were detected by their action on a photographic plate, in that represented in Fig. 68 \$\beta\$ by their action in discharging a gold-leaf electroscope. L is the bulb producing the primary rays, EE a thick lead plate to screen off these rays from the photographic plate or the electroscope, MM the plate struck by the primary rays and emitting the secondary ones, ee in Fig. 68 a the photographic plate; the electroscope is covered with a metal case connected with earth to screen off from the gas exposed to the primary rays the electric field due to the charged gold-leaves, the secondary rays entered this case through a thin aluminium window. The electroscope was discharged and the plate affected even when MM was made of comparatively light and transparent substances, such as paraffin, ebonite, sulphur, or aluminium, while a greater effect was produced by heavy substances. A small effect is produced even when the plate MM is absent, this is due to the secondary rays emitted by the air; the secondary rays emitted by air were first observed by Röntgen\* who detected them by the luminosity they produced in a phosphorescent screen.



134. Sagnac (loc. cit.) showed that the secondary rays were not diffusely reflected primary rays; he did this by proving that the secondary rays were much more easily absorbed than the primary ones. The method he used for this purpose is shown in Fig. 69. The primary rays from the bulb l passed through two openings

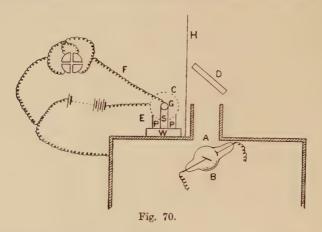
<sup>\*</sup> Röntgen, Wied. Ann. lxiv. p. 18, 1898.

ab, cd in the lead plates  $E_1E_1$ ,  $E_2E_2$ , the secondary rays from the plate LL passed through a hole in a lead plate  $E_1E_1$ , then through a thin aluminium window into the electroscope C. A plate of aluminium AA is placed first in the path of the primary rays and the rate of leak observed, it is then removed from the path of the primary rays and placed at A'A' in the path of the secondary rays, and the rate of leak again observed; the rate of leak in the latter case is always less than that in the former, showing that the secondary rays are more absorbed by the plate than the primary ones. If t is the time taken by the gold-leaves to fall through a certain angle when the plate is at AA, t' the time when the plate is at A'A', then if c = (t'-t)/t, c is called by Sagnac the coefficient of transformation of the rays. This coefficient depends upon the nature of the plate LL; it is much smaller when the plate is made of light substances such as aluminium or paraffin than when it is made of heavy ones such as gold or lead: this shows that the secondary rays emitted by light substances, although not so numerous, are more penetrating than those emitted by heavy ones. Sagnac also showed that when the distance of the electroscope from the plate LL was increased, a much greater diminution was produced in the rate of leak when the plate LL was made of lead than when it was made of zinc or copper, showing that a considerable proportion of the secondary rays from lead were absorbed by a few centimetres of air.

135. Some very interesting experiments on the secondary rays were made by Townsend\* who used the method represented in Fig. 70. The bulb producing the rays and the induction coil by which it was worked were placed inside a box covered with lead, having one aperture at A through which the rays passed up through a lead tube to prevent them from spreading out laterally. C is a cylinder of wire-gauze containing an axial electrode G. The gauze was connected with one terminal of a battery of small storage cells, the other terminal of which was put to earth, the electrode G was connected with an insulated pair of quadrants of an electrometer. The potential difference between the gauze and the electrode G, 85 volts, was sufficient to produce the saturation current. The substance emitting the secondary radiation was placed at D and measurements were made (1) when the secondary

<sup>\*</sup> J. S. Townsend, Proc. Camb. Phil. Soc. x. p. 217, 1899.

radiation passed through nothing but air, (2) when it passed through a plate of aluminium 25 mm. thick. The results are



contained in the following table, the numbers being the deflection of the electrometer in 10 seconds:

Radiator (substance placed at D)	Rays passing through Air	Rays passing through Al	Radiator (substance placed at D)	Rays passing through Air	Rays passing through Al
Air Aluminium . Glass Lead	2 6 7.5 24	1 3·5 3 6	Solid Paraffin BrassZincCopper	30 66 68 70	15.5 2.5 3 2.5

This table shows very clearly the different kinds of radiation given out by different substances, thus the radiation from brass, zinc, and copper is almost completely stopped by the aluminium while the radiation from other substances passes through it comparatively easily. The secondary radiation was found not to be much affected by the state of the surface of the body, thus the radiation from polished brass was only 2 or 3 per cent. greater than from brass coated with oxide: if the brass was covered with wet filter-paper the deflection of the electrometer was reduced from 66 to 46. The secondary radiation is not merely a surface effect, the radiation comes from a layer of the substance of appreciable thickness. This was proved by covering a plate of aluminium

with a thin layer of paraffin; the radiation was reduced to about one-sixth of the amount from a solid block of paraffin. With denser substances such as lead the layer from which the secondary radiation comes will be much thinner than for a light substance like paraffin. In the first place the primary rays can only penetrate to a very small depth below the surface, and in the second place the secondary rays being so much more easily absorbed will only be able to pass through a small fraction of the thickness penetrated by the primary rays. Thus the thickness of the layer from which the radiation comes will always be much less than the thickness which can be penetrated by the primary rays. The arrangements in the preceding experiments were such that the only radiation which would affect the electrometer was that which had passed through several centimetres of air. Townsend showed that in addition to this there was also secondary radiation which was absorbed by a layer of air a few millimetres thick.

The arrangement used for this purpose is shown in Fig. 71. It was arranged to find the saturation-current between two circular plates A and B, 4.8 cm. radius, for different distances

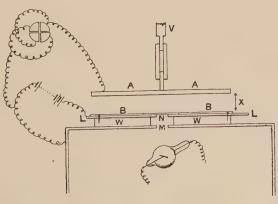


Fig. 71.

between the plates; if there were no secondary radiation this current would be proportional to these distances.

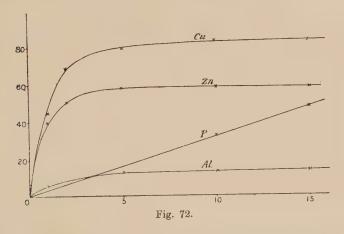
The primary rays passed through a hole M in a lead plate and then through a hole N in another lead plate on which the lower

plate BB, which was made of aluminium, rested. After passing through N the primary rays passed through the air and fell on the plate AA, whose distance from B could be adjusted by means of a screw. A series of experiments were made with plates of different materials at A, the plate B was an aluminium one throughout the experiments; the results of the experiments are given in the following table: t is the distance between the plates in millimetres, and the numbers in the other columns are proportional to the saturation-currents in the various cases. The composition of the upper plate is given in the first row in the table.

t.	Brass	Cu	Zn	Al
1	55	54.4	49	15
$\frac{2}{5}$	81	84 107:5	66	23.7
10	126	128	$\begin{array}{c} 87 \\ 103 \end{array}$	40·8 57
15	142	144	119	73

If there were no secondary radiation the 2, 3, 4 and 5 columns should be identical, and the numbers proportional to the distance between the plates. Let us take the case of brass, then when the distance between the plates is 15 mm., the number of ions produced is proportional to 142; when the distance between the plates is reduced to one millimetre, the number of ions is not reduced to 1/15 but to 1/2.6 only, showing that there are relatively a great many more ions in the millimetre of air next the brass plate than there are in the layers of air at a considerable distance away from it. We see from the table that the ionisation in the millimetre of air nearest the metal is proportional to 55, in the next millimetre it is 26, the average in the next three millimetres is 9.5, in the next five 3.5, and in the last five 3.2: thus by far the greater part of the secondary radiation is absorbed by a layer of air 2 millimetres thick, this part of the radiation would be all absorbed by the air between the plate and the cylinder in the experiment shown in Fig. 70, so that the numbers obtained by the use of this instrument relate to a different class of rays from those detected by the parallel plates. The curves in Fig. 72, taken from Townsend's paper, give a good idea of the rapidity with

which the ionisation diminishes as the distance from the metal surface increases; the ordinates in the curves are proportional to the total amount of ionisation up to a distance from the plate represented by the abscisse. If S is the ratio of the number of ions produced by the easily absorbable secondary rays in the air to the number of ions produced by the primary rays when they traverse a layer of air 1 cm. thick, then Townsend found that for



copper S=2.5, for zinc S=1.84, for aluminium S=4: these numbers are considerably larger than those previously obtained by Perrin, and this and the difference between these results and those obtained by Sagnac indicate that the character of the secondary radiation depends very largely upon that of the primary. H. S. Allen\* has compared the number of ions produced by the secondary ionisation with those which would be produced if the primary rays were entirely absorbed by the gas; using brass as the metal and sulphuretted hydrogen as the gas, he found that the number of ions produced by the secondary radiation was about 1/2000 of the number which would have been produced if the primary rays had been absorbed by the sulphuretted hydrogen.

136. The effect of the secondary ionisation has to be taken into account in all investigations on the relation between the ionisation and the pressure. Thus suppose we were investigating the relation between the saturation-current and the pressure, the

<sup>\*</sup> H. S. Allen, Phil. Mag. vi. 3, p. 126, 1902.

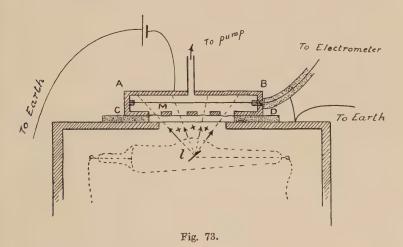
current passing between two parallel plates, one of these being exposed to the primary rays and giving out secondary radiation. The secondary radiation is absorbed within a short distance from the plate, and though when we diminish the pressure we increase this distance the total amount of ionisation will not be affected until the pressure gets so low that the secondary rays can travel from one plate to the other. Thus if S is the secondary and P the primary ionisation, the latter is proportional to the pressure p, equal say to  $\alpha p$ , then, until the pressure gets so low that the secondary radiation extends from one plate to the other, the saturation-current will be proportional to  $S + \alpha p$ ; thus if the secondary ionisation is large compared with the primary, there will be at first very little change in the saturation-current due to a change in pressure; when the pressure gets so low that the secondary radiation is not nearly absorbed between the plates, then both secondary ionisation and primary ionisation, and therefore the saturation-current, will be proportional to the pressures.

137. A metal plate when struck by Röntgen rays emits, in addition to the easily absorbed secondary radiation, negatively electrified particles, or, as we may express it, the metal gives out cathode as well as Röntgen rays. The cathode rays can be distinguished from the others by being deflected by a magnetic field. and by carrying with them a charge of negative electricity so that the metal plate from which they start would, if insulated, acquire a charge of positive electricity. Dorn\* has shown that rays which can be deflected by a magnet are emitted by plates of lead and platinum, and to a smaller extent by plates of copper and zinc when exposed to Röntgen rays. The direction of the deflection is the same as that of cathode rays coming from the metal. Curie and Sagnac+ have shown that the metal plate emits negative electricity and acquires a positive charge; in order to demonstrate this effect it is necessary to work in a good vacuum, as if the plate is surrounded by air at an appreciable pressure, the conductivity of the air due to the primary and secondary radiations is so great that any charge on the plate leaks away before it can be observed. One of the methods used by Curie and Sagnac to demonstrate the charge on the plate is shown in Fig. 73.

<sup>\*</sup> Dorn, Abhand. d. naturf. Ges. zu Halle, xxii. p. 39, 1900, Beiblätter, 24, p. 572.

<sup>†</sup> Curie and Sagnac, Journal de Physique, [4], i. p. 13, 1902.

A thin piece of metal M is insulated and connected with one pair of quadrants of an electrometer; M is enclosed in a metal box ABCD which is connected with the earth, the lower face of the box is pierced with windows closed with thin foil of the same material as the box; the bulb l which produces the rays is enclosed in a box covered with lead. When the plate M and the box ABCD are made of different metals, then at atmospheric pressure the conductivity of the air is considerable, and the arrangement acts like a galvanic battery, a potential difference equal to the contact difference of potential being established between M and the box; as we exhaust the air from the box this



difference remains at first unaltered, but when a very good vacuum is obtained the potential difference is greatly increased; thus when the plate M is made of platinum and the box of aluminium, Curie and Sagnac found that at atmospheric pressure M was positive to the box by less than 1 volt, but at a high vacuum the potential of M was greater than that of the box by about 30 volts. This shows that the platinum emits more negative electricity than it receives from the aluminium. If the plate M is aluminium, and the box platinum, the plate acquired a negative charge. Curie and Sagnac showed that the penetrating power of these negatively charged rays was of the same order as that of the Lenard rays, a piece of aluminium foil about  $46 \times 10^{-6}$  cm. thick reducing the stream of negative electricity about 40 per cent.: from this we

may conclude that the velocity of the secondary rays is of the same order as that of cathode rays in a highly exhausted tube, say between  $10^9$  and  $10^{10}$  cm./sec. Dorn\* has measured the magnetic deflection of these rays and finds velocities varying from  $1.8 \times 10^9$  to  $8.5 \times 10^9$  cm./sec., the values depending upon that assumed for e/m.

We may compare the effects produced when Röntgen rays fall on a metal plate with those produced by the incidence of ultraviolet light; in both cases cathode rays are emitted by the metal. The secondary Röntgen rays may be compared with the reflected light or perhaps with greater accuracy with the phosphorescent light given out by certain substances under the influence of ultra-violet light, for which the reflected light is of the same quality as the incident light; the secondary Röntgen rays are not of the same nature as the primary rays, part at least of the secondary rays being much more easily absorbed than the primary ones.

On account of the great absorption of the secondary and cathode rays, the layer from which they come must be very close to the surface: thus suppose AB is the face of a metal plate on which Röntgen rays are incident, let the primary rays penetrate to CD, then all the metal between AB and CD will be emitting secondary and cathode rays, but it is only the secondary rays which come from a thin layer ABEF which escape extinction before reaching the surface, and as the cathode rays are still more easily absorbed it is only those from a still thinner layer ABE'F' which emerge into the air.

138. Theory of the Secondary Radiation. The secondary radiation is readily explained if we take the view, which we shall discuss later, that the Röntgen rays consist of exceedingly thin pulses of very intense electric and magnetic force. Let us suppose that such a pulse is travelling through a medium containing ions—it is not necessary that the ions should be free: when the pulse reaches a charged ion the ion will be acted on by a very intense force and its motion accelerated. Now when the velocity of a charged body is changing pulses of electric and magnetic force proceed from the body, the magnitude of these forces being pro-

<sup>\*</sup> Dorn, Lorentz Jubilee volume, p. 595, 1900.

portional to the acceleration of the body: thus while the primary Röntgen pulse is passing over the ion and accelerating its motion, the ion gives out a pulse of electric and magnetic force—the secondary Röntgen pulse—the secondary pulse ceasing as soon as the acceleration of the ion vanishes, i.e. as soon as the primary pulse has passed over. It is easy to compare the energy in the secondary pulse with that in the primary. For suppose the ion O is moving parallel to the axis of x, let f be its acceleration, then the ion emits a pulse of magnetic force such that when the pulse reaches the point P, the magnitude of the force is equal to fe sin  $\theta/V$ . OP, V being the velocity of light,  $\theta$  the angle between OP and the axis of x, and e the charge on the ion in electromagnetic units; the direction of the force is at right angles to OP and the axis of x; this magnetic force is accompanied by an electric force at right angles to OP in the plane containing OPand the axis of x, and equal in magnitude to  $fe \sin \theta/OP$ : hence by Poynting's theorem the flow of energy is along OP, and since the quantity of energy flowing across unit area in unit time is, when as in this case the electric and magnetic forces are at right angles to each other, equal to the product of the electric and magnetic forces divided by  $4\pi$ , the rate at which energy flows across unit surface is equal to

 $rac{1}{4\pi} rac{e^2f^2\sin^2 heta}{V.\ OP^2}$  :

integrating this expression over the surface of a sphere with the ion as centre, we see that the rate at which energy is leaving the ion is equal to

 $\frac{1}{3} \stackrel{e^2f^2}{V}$ ,

and the total amount of energy emitted by the ion is equal to

$$\frac{1}{3} \frac{e^2}{V} \int f^2 dt.$$

Now suppose that the electric force in the primary Röntgen pulse is parallel to x and equal to X, then if m is the mass of the ion  $f = \frac{Xe}{m}$ ; substituting this expression for f we find that the energy emitted by the ion is equal to

$$\frac{1}{3}\frac{e^{4}}{m^{2}V}\int\!\!X^{2}dt,$$

the integration extending over the time taken by the pulse to pass over the ion; if d is the thickness of the pulse and if X is constant from the front to the back of it, then

$$\int X^2 dt = \frac{X^2 d}{V} ,$$

and thus the total energy in the secondary radiation emitted by the ion is equal to

 $\frac{1}{3}\,\frac{e^{\!{}^{4}}}{m^{\!{}^{2}}}\,\frac{X^{2}\!d}{V^{2}}\,;$ 

if E is the energy per unit area of the pulse, then

$$E = \frac{1}{4\pi} \frac{X^2 d}{V^2};$$

thus the energy emitted by the ion is equal to

$$\frac{4\pi}{3} \; \frac{e^4}{m^2} E,$$

and if there are N ions per unit volume the energy of the secondary radiation per unit volume is

$$\frac{4\pi}{3}\,\frac{Ne^4}{m^2}\,E.$$

Though each pulse of secondary radiation given out by an ion is of the same thickness as the primary pulse, yet the properties of the secondary radiation may be very different from those of the primary, for each pulse of primary radiation causes each ion to emit a pulse of secondary radiation, so that the single primary pulse produces a great number of secondary pulses following each other at intervals which depend upon the proximity of the ions in the medium traversed by the primary waves; the properties of this train of pulses would depend upon  $\lambda$  the average distance between the ions: they would approximate to those of light of wave-length  $\lambda$  and might thus differ materially from those of the primary rays. In fact on this point of view there is much the same difference between the primary and secondary rays, as there is between the sharp crack of lightning and the prolonged roll of thunder.

We see from the preceding equations that in passing over a distance dx, the primary pulse causes the ions to emit secondary radiation whose energy is

$$\frac{4\pi}{3} \frac{Ne^4}{m^2} Edx;$$

if this were the only loss of energy experienced by the primary rays, we should have

$$dE = -\frac{4\pi}{3} \frac{Ne^4}{m^2} E dx,$$

or

$$E = C \epsilon^{-\frac{4\pi}{3} \frac{Ne^4}{m^2} x} \, , \label{eq:energy}$$

so that the opacity of the substance to the primary rays would be measured by

$$rac{4\pi}{3}rac{Ne^4}{m^2}$$
 ,

this is independent of d, the thickness of the pulse, and depends merely upon the medium and not upon the kind of rays passing through it: the very great difference between the penetrating power of hard and soft rays shows that the energy spent in the secondary radiation cannot be the chief cause of the absorption of the primary rays. Another source of loss of energy is the energy given to the ions and retained by them: the energy of the secondary rays is energy radiated from the ions, but in addition to this energy the ions under the action of the rays retain an amount of energy which is large compared with the energy they give out as radiant energy. To calculate the energy acquired by the ions from the primary Röntgen radiation, we regard that radiation as consisting of a succession of pulses. In some of these the electric force is in one direction, in others in the opposite, and we suppose that there are as many pulses with the force in one direction as there are with the force in the opposite.

Let us consider the effect produced on an ion when a pair of pulses, one positive and the other negative, pass over it. Let X, -X be respectively the electric forces in the positive and negative pulses, d the thickness of either pulse, D the distance between the pulses; then the positive pulse gives to the ion a velocity Xed/Vm, and the ion on the arrival of the second pulse will have moved through a distance (Xed/Vm)(D/V) (if we assume that the time interval between the arrival of the two pulses at the ion is small compared with the free time of vibration of the ion). The second pulse gives to the ion a momentum equal and opposite to that given to it by the first pulse and thus reduces it to rest: the joint action of the two pulses is thus to leave the

velocity of the ion unaltered, and to displace the ion through a distance  $\xi$  given by the equation

$$\xi = \frac{Xe}{m} \, \frac{d}{V} \, \frac{D}{V} \, .$$

If we suppose that the ion was in equilibrium in the position  $\xi = 0$ , and that when displaced from this position the force tending to bring it back is  $\mu \xi$ , the work done in displacing the ion through the distance  $\xi$  is  $\frac{1}{2}\mu \xi^2$ , thus the energy communicated by the positive and negative pulses to the ion is

$$\frac{1}{2}\mu \frac{X^2e^2}{m^2} \frac{d^2}{V^2} \frac{D^2}{V^2}.$$

If E is the energy in the two pulses per unit area, we have

$$E = \frac{1}{2\pi} \, \frac{X^2 d}{V^2} \, .$$

Thus the work done on the ion is equal to

$$\pi \mu \, rac{e^2}{m^2} \, rac{dD^2}{V^2} \, E.$$

If n is the frequency of the free vibration of the ion,  $n^2 = \mu/m$ , so that the work done on the ion is

$$\pi n^2 \frac{e^2}{m} \frac{dD^2}{V^2} E$$

$$=4\pi^3\frac{e^2}{m}\,\frac{dD^2}{\lambda^2}E,$$

where  $\lambda$  is the wave-length of the free vibration of the ion. Thus the work done on the ions when the two pulses travel over a distance  $\delta x$ , is equal to

$$4\pi^3 \frac{e^2}{m} d \cdot D^2 \sum_{\lambda} \frac{N}{\lambda^2} E \delta x = h E \delta x$$
, say,

where N is the number of ions giving out light of the wave-length  $\lambda$  in unit volume, hence we have

$$\frac{dE}{dx} = -hE,$$

or  $E = E_0 e^{-hx}$ ;

h is thus the coefficient of absorption of the medium for the Röntgen rays: when we take into account the energy absorbed by

the ions and neglect that radiated by them, we see that h increases with the thickness of each pulse and the distance between the pulses, it thus depends upon the character of the primary rays; the broader the pulses the greater the absorption. Thus on this view of the nature of the Röntgen rays the soft rays correspond to broad pulses, the hard rays to narrow ones.

Sagnac, by allowing secondary rays to fall on metal, has obtained tertiary rays, which are even more easily absorbed than the secondary; he suggests that by a repetition of this process we might ultimately get rays having the properties of ordinary light. As yet however no Röntgen rays have been obtained which show any trace of refraction when passing from one medium to another.

## CHAPTER XII.

## BECQUEREL RAYS.

THE very marked phosphorescence produced in certain substances by Röntgen rays led to a series of investigations whose object was to see whether phosphorescence was accompanied by the emission of Röntgen rays: since Röntgen rays produced phosphorescence the question naturally suggested itself, may not phosphorescence be accompanied by Röntgen rays? Early in 1896 Henry\* showed that the phosphorescent substance sulphide of zinc, after exposure to sunlight or magnesium light, acted photographically on a plate protected by black paper or by thin aluminium foil. A little later Becquerel found that if the double sulphate of uranium and potassium was placed on a photographic plate protected by light-proof paper and the system exposed to the sun the plate was affected: he thought at first that this was due to the phosphorescence emitted by the uranium while in the light, he soon found however that exposure to the sunlight was not necessary, and that the plate was equally affected in the dark. To test whether this effect was due to a phosphorescence which had persisted from some previous exposure of the uranium salt to light \ he took a crystal of uranium nitrate and dissolved it in water in the dark; he then, keeping it still in the dark, allowed it to recrystallise, and tested its action on the photographic plate without ever exposing the crystal to light; he found that it acted strongly on the plate; he found also that the solution of uranium nitrate which is not phosphorescent is active. On these grounds Becquerel came to the conclusion that the

<sup>\*</sup> Henry, Comptes Rendus, exxii. p. 312, 1896.

<sup>+</sup> Becquerel, Comptes Rendus, exxii. p. 420, 1896.

<sup>‡</sup> Ibid. p. 501.

<sup>§</sup> Ibid. pp. 691, 765.

effect is not due to phosphorescence but is a property of the metal itself. He found too that the salts of uranium as well as the metal itself retained this radio-active property without sensible diminution after being kept in the dark, some of them in lead boxes, for more than a year. In addition to affecting a photographic plate protected by a covering opaque to ordinary light, the radiation from uranium, like the Röntgen rays, makes the gas through which it passes a conductor; thus a charged electroscope with a piece of uranium placed on the disc slowly loses its charge, whether this be positive or negative. Becquerel at first thought that the rays from uranium differed from the Röntgen rays in being capable of refraction and polarisation; subsequent investigations made by himself and others have shown however that this is not the case.

140. Rutherford\* made a very extensive series of experiments on the radiation from uranium and its compounds, using the electrical method of investigation, i.e. measuring the intensity of the radiation by the ionisation produced by the rays. He made the very interesting discovery that the radiation from uranium, like the secondary Röntgen radiation, is a mixture of two types of radiation, one type  $\alpha$  being absorbed by a few millimetres of air at atmospheric pressure, the other type  $\beta$  having a penetrating power comparable with the rays from a Röntgen tube of moderate exhaustion. This fact is illustrated by the following table, which shows the effect of successive layers of very thin aluminium foil in cutting down the intensity of the radiation.

Thickness of aluminium foil, '0005 cm.

Number of layers of Aluminium foil	Leak per minute in scale divisions	Proportion in which the leak is diminished by one layer of foil
0 1 2 3 4 12	182 77 33 14·6 9·4 7	·42 ·43 ·44 ·65

From these numbers we see that the first layer of aluminium foil cuts down the intensity of the radiation to about one-half of

<sup>\*</sup> Rutherford, Phil. Mag. v. 47, p. 109, 1899.

its original value, the second and third layers each diminish it in much the same proportion, the fourth layer however produces sensibly less effect, while the joint effect of the next eight layers is small; in fact to reduce the intensity of the radiation to onehalf the value it has after passing through four layers of foil requires the interposition of one hundred additional layers. Thus before the rays had been filtered by the foil, one layer of foil produces as much absorption as one hundred layers after the filtering has taken place. These results show that part of the radiation emitted from the uranium is almost entirely absorbed by about four layers of foil, while there is another part of very much greater penetrating power which can pass through about one hundred layers of foil before its intensity is reduced to onehalf. Rutherford calls the easily absorbable radiation the  $\alpha$ radiation, the other the  $\beta$  radiation. The penetrating power of the  $\beta$  radiation is of the same order as that of Röntgen rays emitted by an average bulb. Rutherford found that the absorption by the different gases of the a type of radiation emitted by uranium or any of its compounds was such that the intensity of the radiation was reduced to one-half its value after passing through

3 mm. of carbonic acid gas, 4·3 mm. of air, 7·5 mm. of coal gas, 16·3 mm. of hydrogen.

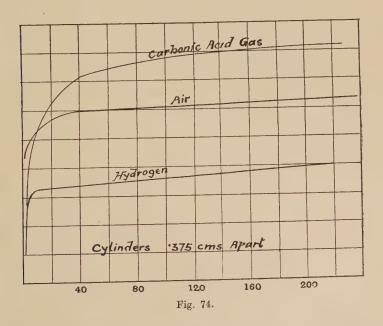
The pressure in all cases was that due to 760 mm. of mercury. The penetrating power of the  $\alpha$  radiation is thus intermediate between that of ordinary primary and secondary Röntgen rays.

The absorption of the  $\alpha$  rays was shown by Rutherford to be proportional to the density of the gas.

Near a layer of uranium we have thus a region of very intense ionisation extending over the few millimetres necessary to absorb all the  $\alpha$  rays, beyond this only the  $\beta$  rays penetrate, and as these have only small ionising power compared with the  $\alpha$  rays there is in this region very much less ionisation than in the layers close to the uranium. Thus if we have two parallel metal plates over one of which a layer of uranium is spread, then if the distance between the plates is greater than that required to absorb the  $\alpha$  radiation, the total amount of ionisation between the plates and

therefore the value of the saturation current which can pass from one plate to the other will not increase much as the distance between the plates is increased, while as long as the distance between the plates is less than that required to absorb the  $\alpha$  radiation the saturation current will be approximately proportional to the distance between the plates; this illustration will suffice to show that the phenomena of electric conduction under uranium radiation are somewhat intricate, they can however be readily explained by the existence of the two types of radiation, one very easily absorbed, the other much more penetrating.

Since the intensity of the ionisation is much greater close to the plate covered with uranium than at some distance away, the electric force near to the uranium will be less than the average value between the plates; this fall in the electric force at the place where there is most ionisation makes it more difficult to produce a saturation current than it would be if the ionisation



were uniform between the plates; this may account for the fact discovered by Rutherford (l.c.) that even with large potential differences between the plates the current shows an increase,

though only a small one, when the potential difference is increased. This is illustrated in the curves in Fig. 74 which represent the relation between the potential difference and the current under uranium radiation.

The proportion between the amounts of the  $\beta$  and  $\alpha$  radiations emitted by a layer of a salt of uranium was found by Rutherford (l.c.) to depend upon the thickness of the layer of salt, the thicker the layer the larger the ratio of the  $\beta$  to the  $\alpha$  radiation. what we should expect if we regard the  $\alpha$  and  $\beta$  radiations as independent of each other: for if the a radiation is stopped by a thickness  $t_1$  of the salt, while the  $\beta$  radiation is not stopped until the thickness is  $t_2$ , the  $\alpha$  radiation will not increase with the thickness of the layer when this is greater than  $t_1$ , while the  $\beta$ radiation will go on increasing until the thickness is equal to  $t_2$ . If one of the radiations was produced by the other, if for example the  $\beta$  radiation corresponded to primary Röntgen rays, the  $\alpha$  to the more absorbable secondary rays produced by the impact of the primary ones with the uranium close to the surface, then we should expect the proportion between the radiations to be independent of the thickness of the layer.

141. Ionisation in different gases. Since the  $\alpha$  radiation is absorbed by a few millimetres of most gases, the total amount of ionisation produced on different gases when it is completely absorbed can be readily determined: the result of such a determination made by Rutherford (l, c) is given in the following table.

Gas	Total Ionisation	Gas	Total Ionisation
Air	100 95 106 96	Coal gas	111 102 101

The salt used to produce the rays was uranium oxide, and as its radiating power was slightly affected by ammonia and hydrochloric acid the numbers for these gases must be regarded as only approximately true. It will be seen that the numbers expressing the total ionisation produced in the various gases when all the radiation is absorbed are very nearly equal; so nearly indeed that

we cannot say with certainty that the differences are not due to experimental errors. The experiments thus point very distinctly to the conclusion that the absorption of a fixed quantity of Becquerel rays gives rise to the same number of ions whatever may be the nature of the gas ionised; we saw (p. 251) that Rutherford's experiments on the absorption of Röntgen rays indicated that a similar result was true for these rays. We may express this result in the form that when all the rays whether Becquerel or Röntgen are absorbed in a certain volume of gas, the maximum quantity of electricity which can be forced through the gas depends only upon the intensity of the rays and not upon either the composition or pressure of the gas. This result is so interesting that it is worth while discussing it a little more closely. The energy absorbed may be spent (1) in ionising the gas, (2) in raising the temperature of the gas. Suppose that the rays are travelling parallel to the axis of x, let I be the intensity of the rays at the distance x from the origin,  $I + \delta I$  the intensity at  $x + \delta x$ ;  $-\delta I$  is the energy absorbed in the layer  $\delta x$ .

Suppose that the number of ions produced is proportional to the energy of the rays, and that the number produced in the layer  $\delta x$  is equal to  $\lambda I \delta x$ , let the work required to produce an ion be  $\alpha$ , then the energy absorbed in ionising the gas is  $\alpha \lambda I \delta x$ ; let the amount absorbed as heat\* in the layer be  $qI\delta x$ , then we have

$$-\delta I = (q + \alpha \lambda) I \delta x \text{ or } I = C \epsilon^{-(q + \alpha \lambda) x},$$

where C is the value of I when x = 0.

The number of ions produced when the radiation is all absorbed is equal to

 $\int_{0}^{\infty} \lambda I dx = \int_{0}^{\infty} C \lambda \epsilon^{-(q+a\lambda)x} dx = \frac{C\lambda}{q+a\lambda}.$ 

Rutherford's experiments show that as long as C is constant this number is independent of the nature of the gas; this shows that the production of each pair of positive and negative ions abstracts from the energy of the rays an amount of energy which is independent of the nature of the gas ionised: if all the energy absorbed were spent in ionising the gas this result would imply that the energy required to produce a given number of ions was

<sup>\*</sup> If the ions are allowed to recombine all the energy will ultimately appear as heat.

independent of the nature of the gas from which the ions are obtained. The evidence seems however to be against the view that the separation of ions from the molecules of the gas is the only source by which the rays lose energy. Rutherford and McClung\* have measured the energy in Röntgen rays, and also the total amount of ionisation these rays would produce if they were completely absorbed by a gas. The energy in the rays was measured by absorbing them in thin strips of platinum used in a bolometer and determining the heating effect from the change in resistance. Dorn + had previously shown that appreciable thermal effects were produced by the absorption of Röntgen rays in thin sheets of metal, and had by this means measured the energy in the rays. Measurements of this kind give us C, while the measurement of the total number of ions gives us  $C\lambda/(q + \alpha\lambda)$ , combining the two we get  $(q + \alpha \lambda)/\lambda$ . Rutherford and McClung assumed that the energy of the Röntgen rays was entirely spent in ionising the gas, so that if the ions were prevented from recombining by means of a strong electric field no heat was developed in the gas; on this supposition q = 0, so that  $(q + \alpha \lambda)/\lambda$  is equal to  $\alpha$ , the work required to produce an ion. Making this supposition Rutherford and McClung found that the work required to ionise a gas was equivalent to the work done when each ion was moved through a potential difference of about 95 volts, so that since the ions are produced in pairs it would require a potential difference of at least 190 volts to separate the ions. We saw however (p. 190) that the experiments made by H. A. Wilson on the ionisation of hot gases indicated that a much smaller difference of potentialabout 2 volts—is all that is required to ionise a gas, this conclusion is confirmed by other lines of argument. If we take Wilson's value for the work required to ionise a gas, we see that a is the work done when the ionic charge is moved through the potential difference of about 1 volt. Rutherford's and McClung's experiments show that in the case of the Röntgen rays used by them

$$\alpha + \frac{q}{\lambda} = 95\alpha,$$

 $\frac{q}{\lambda} = 94\alpha$ .

or

† Dorn, Wied. Ann. lxiii. p. 160, 1897.

<sup>\*</sup> Rutherford and McClung, Phil. Trans. A. excvi. p. 25, 1902.

Thus for each ion produced the mechanical equivalent of the heat developed in the gas is about 94 times the work required to separate the ion from the molecule.

Rutherford's experiments on the ionisation produced by the complete absorption of the  $\alpha$  radiation from uranium show that if the number of ions produced is proportional to the energy in the rays, then as long as the rays remain the same the liberation of an ion always abstracts the same amount of energy from the rays whatever may be the nature of the gas. This, since by far the greater part of the absorption of energy is apparently due to the heating of the gas, is a very remarkable result. We do not know however whether or not the amount of energy absorbed when an ion is produced depends upon the nature of the rays, whether for example it is the same for Becquerel as for Röntgen rays, for hard Röntgen rays as for soft. It is much to be desired that experiments of the type of those made by Rutherford and M°Clung should be made with as many kinds of rays as possible.

If we regard the Röntgen and Becquerel rays as pulses of electric and magnetic force made up of Faraday tubes, we may see why the amount of ionisation should not depend upon the nature of the gas: for when a pair of ions is separated the ends of one of the Faraday tubes in the pulse will now be on the ions, one end on the positive, the other end on the negative ion; this Faraday tube gets anchored as it were by the ions, and is dragged back from the pulse which passes on without it. Thus each pair of ions means the abstraction of one Faraday tube from the pulse, and when all the tubes are extracted, the number of ions produced will be twice the number of Faraday tubes originally in the pulse and independent of the nature of the gas.

142. The total amount of ionisation produced when the α rays of uranium and its salts are completely absorbed has been determined by Monsieur and Madame Curie\* and by Rutherford and McClung†, it increases somewhat with the thickness of the layer, as the following table given by the latter observers shows. The amount of ionisation is expressed in terms of the saturation current which is given in ampères per square centimetre of surface.

<sup>\*</sup> Curie, Rapports présentés au Congres de Physique à Paris, t. iii. p. 79, 1900.

<sup>+</sup> Rutherford and McClung, Phil. Trans. A. exevi. p. 25.

Surface of Uranium Oxide = 38 sq. cms.

Weight of Uranium Oxide spread over this surface in grammes	Current in Ampères per sq. cm. of surface
·138	$1.7 \times 10^{-13}$
365	$3.2 \times 10^{-13}$
•718	$4 \times 10^{-13}$
1.33	$4.4 \times 10^{-13}$
3.63	$4.7 \times 10^{-13}$

Taking the value given by Rutherford and M<sup>c</sup>Clung for the energy absorbed when each ion is produced, we find that when the saturation current is  $4.7 \times 10^{-13}$  ampères per square centimetre the energy emitted from a square centimetre is about  $10^{-11}$  calories per second, or at the rate of 1 calorie in about 3000 years. If we take the radiation corresponding to the thinnest layer we find that for each gramme in the layer it is about 1 calorie in 30 years.

## Magnetic Deflection of the more penetrating Uranium Rays.

143. The fact that some of the rays given out by some radioactive substances are deflected by a magnet was first discovered for the radiation from radium, we shall give an account of these experiments when we discuss the radiation from that body. Becquerel\* subsequently found that the  $\beta$  rays from uranium were deflected by a magnet, the direction of the deflection being the same as that of the cathode rays: so that for this and other reasons we conclude that the  $\beta$  rays consist of negatively charged particles. Assuming that the ratio of the mass to the charge for the  $\beta$  rays is the same as for the cathode rays, Becquerel from his determination of the magnetic deflection of these rays concluded that they were moving with a velocity of  $2 \times 10^{10}$  cm. per sec.: this velocity, which is two-thirds of that of light, is considerably greater than that of any eathode rays hitherto produced by electrical means.

The  $\alpha$  rays from radium have been shown by Rutherford† to carry a positive charge, and Becquerel‡ has shown that they are deflected by a strong magnetic field in the direction corresponding to a charge of this sign.

<sup>\*</sup> Becquerel, Comptes Rendus, cxxx. p. 1583; cxxxi. p. 137, 1900.

<sup>+</sup> Rutherford, Phil. Mag. vi. 5, p. 177, 1903.

<sup>#</sup> Becquerel, Comptes Rendus, exxxvi. p. 431, 1903.

144. Sir William Crookes\* concludes that the radiation from uranium does not proceed from uranium itself, but from some unknown impurity. The reason for this conclusion is that by a process of fractionation he has obtained, starting from uranium salts, two products, one of which is radio-active, while the other is not.

One of these processes consists in dissolving crystallised uranium nitrate in ether, the uranium divides itself unequally between the ether and the water present, the larger part which is in the ether layer does not affect a photographic plate, while the smaller portion which is in the water layer possesses all the photographic activity of the original nitrate. Soddy+, who repeated this experiment using for the radio-activity the electrical test, i.e. the amount of ionisation produced, found that both portions were equally active, so that apparently no separation had been effected. The explanation of this discrepancy is that in the photographic method the rays have to pass through glass or card before reaching the film, so that all the absorbable α rays are stopped and only the  $\beta$  rays are detected: in the electrical method however the ionisation is practically entirely produced by the  $\alpha$  radiation, thus the photographic method detects the  $\beta$ , the electrical method the a radiation, so that the experiments show the separation is confined to the substance producing the  $\beta$  radiation. Another process employed by Crookes to separate the active constituent—UrX—from the other consisted in precipitating solutions of uranium nitrate with ammonium carbonate in excess, the small amount of precipitate was collected and the filtrate evaporated, another and much larger precipitate came down; the first of these precipitates strongly affected a photographic plate, while the second was almost inactive. On testing these by the electrical method Soddy found that the second precipitate produced a considerable ionisation, while the effect of the small quantity of the first was barely perceptible; the explanation of this is the same as before, and Rutherford and Grier have shown by direct experiment that the first precipitate emits nothing but the cathodic-magnetically deflectable  $\beta$  radiation, while the second precipitate emits nothing but the a radiation.

<sup>\*</sup> Crookes, Proc. Roy. Soc. lxvi. p. 409, 1900.

<sup>+</sup> Soddy, Chem. Soc. Journ. lxxxi., lxxxii. p. 860, 1902.

<sup>‡</sup> Rutherford and Grier, Phil. Mag. vi. 4, p. 315, 1902.

145. Becquerel\* made the very interesting observation that when he had enfeebled the radio-activity of uranium by precipitating barium as sulphate from uranium solutions and transferred most of the  $(\beta)$  activity to the barium, on allowing the products to stand for several months the enfeebled uranium had recovered its normal activity, while the barium which had been made radioactive had entirely lost this property; a similar phenomenon was discovered by Rutherford and Soddy in the case of thorium, and their investigations on this point led to very important considerations as to the production of radio-activity; these are discussed on p. 292.

#### Radiation from Thorium.

146. Soon after the discovery of the Becquerel rays Schmidt<sup>†</sup> discovered that thorium gave out rays having very similar properties. This radiation was subsequently studied by Rutherford<sup>‡</sup> and by Owens§, and was found to present many features of great interest.

When a thin layer of thorium oxide is used the radiation is approximately homogeneous, as the following results given by Rutherford show: successive layers of thin paper were placed over a thin layer of thorium oxide, and the intensity of radiation determined by measuring the rate of discharge through a volume of gas sufficient to absorb the radiation completely.

Thickness of paper = 0027 cm.

Number of layers of thin paper	Rate of Discharge	
0	1	
1	•37	
2	·16	
3	.08	
3	.08	

The intensity of the radiation, which is proportional to the rate of discharge, thus diminishes in approximately geometrical progression with the addition of equal thicknesses of paper, this shows

<sup>\*</sup> Becquerel, Comptes Rendus, exxxiii. p. 977, 1901.

<sup>+</sup> Schmidt, Wied. Ann. lxv. p. 141, 1898.

<sup>‡</sup> Rutherford, Phil. Mag. v. 49, pp. 1, 161, 1900.

<sup>§</sup> Owens, Phil. Mag. v. 48, p. 360, 1899.

that the radiation is roughly homogeneous. When however a thick layer of the oxide is used there is in addition to the radiation of the type given out by the thin layer other radiation of a much more penetrating type; this is proved by the following results, which were also given by Rutherford.

Thick layer of oxide.

Thickness of paper = .008 cm.

Number of layers of paper	Rate of Discharge	
0	1	
1	•74	
2	•74	
5	*72	
10	*67	
20	*55	

Thus the first layer of paper produces an appreciable diminution in the intensity of the radiation due to the absorption of the radiation of the type given out by the thin layer, but after this is absorbed there is an appreciable amount of radiation left which can pass through a considerable thickness of paper without suffering much absorption.

147. The radiation from thick layers of thorium oxide when first measured by Rutherford seemed to be extremely capricious; thus, for example, when its intensity was measured by the conductivity it communicated to a gas, the slightest draught in the vessel through which the current of electricity passed was sufficient to produce a very sensible diminution in the current; indeed so sensitive was the current to external disturbances, that it was found exceedingly difficult to get consistent results. Rutherford showed that those irregularities had a most interesting cause, as he was able to trace them to an 'emanation' given off by the thorium. He found that the thorium gave off something which was wafted about by currents of air like a vapour; in order to avoid prejudging the question as to the physical state in which the substance given off by the thorium existed, Rutherford called it an emanation. This emanation is radio-active, i.e. it gives off rays that can penetrate a photographic plate or ionise a gas; it can penetrate, apparently by diffusion, thin sheets of metal or pieces of paper; it cannot, however, get through glass or mica, even when they are in very thin films: in fact, its power of getting through substances seems much more selective than the corresponding power possessed by either Röntgen, Becquerel, or cathode rays; in this respect it resembles the effect coming from certain metals and resinous substances studied by Russell. That the passage of the emanation through solids is analogous to the slow diffusion of gas through metal, as, for example, hydrogen through red-hot platinum, is suggested by the fact that if the thorium oxide is covered up with paper it takes a considerable time for the emanation to get through.

The following experiment is one by which Rutherford demonstrated the existence of the 'emanation,' and studied many of its properties.

A thick layer of thorium oxide was enclosed in a narrow rectangular vessel A, made up of two thicknesses of foolscap paper. This paper was sufficiently thick to stop all the radiation from a thin layer of thorium. The vessel containing the thorium

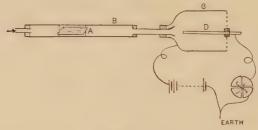


Fig. 75.

was placed inside a long metal tube B. One end of this tube was connected with a large insulated vessel C, the end of this vessel was perforated to allow air to pass through. An insulated electrode D was inserted in C, and connected with one pair of quadrants of an electrometer. C was connected with one terminal of a battery giving an electromotive force of 100 volts, the other terminal of this battery was put to earth.

A slow current of dust-free air was passed through the apparatus. After a short time a current began to pass between C and D, and gradually increased until it reached a certain value, when it became steady. The flow of air was then stopped, and

it was found that the current between C and D persisted for about 10 minutes. As long as the current of air was passing through the apparatus there would have been a current of electricity between C and D, if ordinary radiation and no emanation had been coming from the thorium, for the radiation would have produced ionised gas in the neighbourhood of A, and this would have been carried by the current into C: but in this case the current of electricity would have stopped within a fraction of a second after the stoppage of the current of air, whereas, as we have seen, the effect persisted for 10 minutes. This shows that fresh ions must be continually produced in C, in other words, the substance carried over from A must be radio-active, and though its radio-activity diminishes with time there is enough left to be appreciable after an interval of 10 minutes.

Rutherford measured the leak between C and D at regular intervals after the stoppage of the current of air, and so was able to measure the rate at which the intensity of the radiation from the emanation died away: the intensity diminishes in geometrical progression with the time, and is thus proportional to  $e^{-\lambda t}$ , where t is the time and  $\lambda$  a constant: the intensity is reduced to about one-half its value in one minute, so that  $\lambda$  is about 1/86. The rate at which the radiation falls off is not affected by exposing the emanation to a strong electric field, nor could any motion of the emanation as a whole be detected in such a field: Rutherford showed that the average velocity of the particles of the emanation, under an electric field of one volt per centimetre, must be less than  $10^{-6}$  cm./sec.

In consequence of the diffusion of the emanation from the thorium the radiation from thick layers of this substance does not cast shadows, the emanation getting by diffusion round the opaque body and obliterating the shadow.

The emanation can pass through plugs of porous substances, can bubble through water or the strongest acids, and can be raised to temperatures far above a red-heat without losing its radio-activity\*: in fact, when once the 'emanation' has been produced no physical or chemical process which has yet been tried has any effect upon its radio-activity: in this inertness it

<sup>\*</sup> Rutherford and Soddy, Journal of Chemical Society, lxxxi. p. 321, 1902.

resembles the gases argon and helium, the latter of which occurs along with thorium in many minerals.

Since the emanation can penetrate several millimetres of a thorium compound, the radiation from a layer of such a compound will increase with the thickness of the layer when this is less than a few millimetres; above a certain thickness the radiation becomes practically constant.

The fact that the 'emanation' can pass through porous plugs and water traps, and can withstand temperatures which alter the properties of thorium, is strong evidence that the emanation is not thorium dust, *i.e.* not small particles of thorium in the solid state; this conclusion is strengthened by the fact that the emanation does not give rise to a cloud when the air through which it is diffused suffers an expansion sufficient to produce a fog in dusty air.

No alteration has been detected in the pressure of an exhausted bulb when the emanation is allowed to diffuse into it, nor does this intrusion of the emanation produce apparently any change in the spectrum given out by the bulb.

## Effect of Physical Conditions on Emanating Power.

148. Effect of Temperature. This has been investigated by Rutherford\* and by Rutherford and Soddy†, who have shown that an increase of temperature up to a certain limit—about a red-heat—increases the emanating power of thorium oxide. The maximum reached is between three and four times the value at ordinary atmospheric temperatures, and is maintained at this value for several hours without any sign of diminution with time. When the thorium is allowed to cool the emanating power returns to about the original value. When the thoria is heated beyond a certain temperature the emanating power rapidly falls off to a fraction of its former value, and on cooling the emanation is found to be small compared with its previous value; by heating thoria to the highest temperature which could be safely employed with platinum vessels and then allowing it to cool, the emanating power was reduced to about 8 per cent. of its original value.

<sup>\*</sup> Rutherford, Physikalische Zeitschrift, ii. p. 429, 1901.

<sup>+</sup> Rutherford and Soddy, Journal of Chemical Soc. lxxxi. p. 321, 1902.

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This change in the rate of emanation is accompanied by changes in the physical and chemical properties of the thoria; when first the de-emanation sets in the thoria changes in colour from pure white to a light brown, and then at the very highest temperatures to a pure pink; and at the same time the solubility of the substance in sulphuric acid is greatly diminished. Though the emanation is so greatly diminished by this intense heating, the radiation from thin layers of the substance—which, following Rutherford, we shall call the 'straight line' radiation—is not affected.

Rutherford and Soddy have shown that the loss of emanating power of thoria can be remedied by chemical treatment, they found that if the de-emanated thoria was dissolved up and reprecipitated it recovered completely its emanating power.

In another experiment made by Rutherford and Soddy the thoria was cooled by a mixture of solid carbonic acid and ether, the emanation fell to about 10 °/ $_{\circ}$  of its value at the temperature of the room, but it recovered its original value when the cooling agent was removed. Thus though all changes of temperature produce marked temporary effects, no permanent ones are produced unless the temperature exceeds red-heat.

149. Effects of Moisture. Dorn\* showed that the emanation from thoria was greater in a moist atmosphere than in a dry one. Rutherford and Soddy subsequently confirmed this, and found that the emanation in an atmosphere saturated with water vapour was about 20 °/<sub>o</sub> greater than in a very dry atmosphere.

There are many phenomena which show that the emanating power of a thorium compound does not depend merely upon the quantity of thorium and other elements in the material; the way in which the different elements are combined and the previous treatment and history of the compound have a great influence upon the result. Thus, for example, the emanating power of freshly prepared hydroxide goes on increasing for some time after it has been dried, until when it reaches the steady state the value may be three times that when it was first tested. This seems to indicate that the emanation may be due to some compound which is formed but slowly: the effect produced by

<sup>\*</sup> Dorn, Abh. der Naturforsch. Ges. für Halle-a-S. 1900. Beiblätter, xxiv. p. 1343.

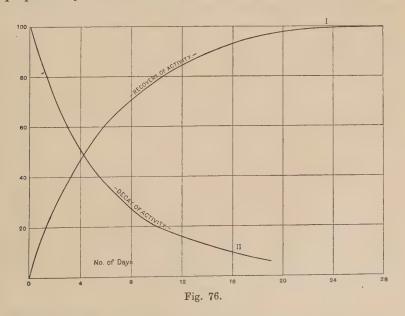
intense heating could be explained by supposing that at high temperatures this compound is changed into one not giving the emanation, the change being a permanent one, the new substance not being destroyed by the subsequent cooling.

A good illustration of the effect of changes in the physical condition of the substance on its emanating power is afforded by the nitrate; this salt when in the solid state gives out but little emanation, when however the salt is dissolved in water and air bubbled through the solution the air carries off more than 200 times the quantity of emanation that could be obtained by passing the air over an equal quantity of the solid; the quantity of emanation obtained by bubbling depends only upon the quantity of the salt and not upon the degree of dilution.

## Source of the Emanation.

150. Rutherford and Soddy have made a series of experiments to see whether the emission of the emanation is a property of thorium itself, or whether it is due to some impurity. The conclusion they came to was that it was not emitted directly from the thorium, since they could obtain from thorium salts substances whose emanating power was enormously greater than that of the original salt. One method of doing this was to dissolve a quantity -in the experiment 70 grams-of thorium nitrate in water and precipitate the thorium by adding ammonia. The filtrate was then evaporated down to about 60 c.c., and was found to possess when air was bubbled through it as much emanating power as 146 grams of thoria; on evaporating to complete dryness and getting rid of the ammonium salts the residue left only weighed 0583 gram. Thus this residue consisted of a substance which when in solution gave with a weight of 0583 gram as much emanation as 146 grams of thoria, or weight for weight its emanating power was 2500 times that of thoria. The separation of this substance was accompanied by a loss in the emanating power of the substance from which it was produced, for when the hydroxide precipitated in this experiment was converted into oxide, the emanating power of this was only about one-third that of oxide prepared from nitrate which had not been dissolved. Similar results were obtained by testing the water used to wash the oxide, Residues were obtained by evaporating the washings to dryness, and some of these residues were 1800 times more radio-active than the original thoria. No substance other than thorium could be detected in these residues; the quantity of material available was however too small to admit of a very searching examination.

151. In a subsequent paper Rutherford and Soddy\* have shown that the very active residues they obtain by those methods gradually lose their radio-activity, while the thorium hydroxide which had been deprived of its power by the abstraction of this residue gradually recovers and ultimately regains its normal activity; thus in one case they found that in about three weeks the recovery of the hydroxide whose strength had been reduced to about 36 % of its normal value was practically complete, while the residue which originally was so abnormally active had in the same time lost the whole of its activity. This led to a series of experiments on the rate of recovery of the hydroxide and the rate of loss of the residue called by them Th X, the residue was prepared by the ammonia process described on p. 290. The



results of these experiments are shown in the curves given in Fig. 76: it will be seen that the time taken by the hydroxide

<sup>\*</sup> Rutherford and Soddy, Phil. Mag. vi. 4, pp. 370, 569, 1902.

to recover half of its lost radio-activity is about the same as that taken for the radio-activity of the Th X (the residue) to lose half of its original activity. Rutherford and Soddy by these experiments were led to a theory of radio-activity which explains this and many other phenomena. This view is as follows; the radio-active constituent in the thorium compounds is not an accidental impurity, but is a substance which we may call Th X, which is being manufactured at a constant rate from the thorium; after its manufacture its radio-activity gradually dies away. The normal radio-activity of a thorium compound is due to a state of dynamical equilibrium in which the increase in radio-activity due to the production of fresh Th X just balances the loss due to the fading away of the activity of the Th X previously produced.

To put this in a mathematical form suppose that T is the amount of thorium present at any time, let the amount of Th X produced by this in unit time be  $\alpha T$ ; let the initial radio-activity of unit mass of Th X be r, then the rate at which the radio-activity of the mixture is increasing in consequence of the production of fresh Th X is  $r\alpha T$ ; let R be the radio-activity of the mixture, let this in consequence of the loss of energy by radiation be decreasing at the rate  $\lambda R$ ; then we have

$$\frac{dR}{dt} = r\alpha T - \lambda R....(1);$$

when things are in a steady state dR/dt vanishes and we have

$$R = \frac{r \alpha T}{\lambda}.$$

The general solution of (1) is, regarding T as constant,

$$R = \frac{r \pi T}{\lambda} + C \epsilon^{-\lambda t} \dots (2)$$

where C is a constant. Let us suppose that we remove all the Th X and so deprive the substance of its radio-activity, then initially when t=0, R=0 and (2) becomes

$$R = \frac{r\alpha T}{\lambda} (1 - \epsilon^{-\lambda t}),$$

thus the compound will have recovered half of its normal activity when  $e^{-\lambda t} = \frac{1}{2}$  or when  $t = \frac{1}{\lambda} \log 2$ .

Let us now consider the radio-activity of the Th X removed from the mixture, as there is no thorium in the mixture T=0 so (2) becomes

 $R = C\epsilon^{-\lambda t}$ ,

thus the intensity of the radiation will fall to half its original value when  $e^{-\lambda t} = \frac{1}{2}$  or when  $t = \frac{1}{\lambda} \log 2$ ; thus the time taken for the Th X to lose half its radio-activity is equal to the time taken for the salt from which the Th X was removed to recover half of its lost activity, and this as we have seen is approximately the case.

On this view the energy required to maintain the radiation is obtained from the chemical change which is taking place in the thorium, the change from thorium to thorium X being accompanied by a loss of energy.

Rutherford and Soddy consider that Th X is a distinct substance and not merely some chance substance that may have been present along with the thorium in the salt. Their reason for thinking that the latter view is not tenable is that if it were true then any method of precipitating the thorium from a solution ought to leave the solution radio-active after the loss of the thorium; this is not however the case, it is only certain special methods of precipitation which deprive the precipitated thorium of its activity and leave the solution radio-active; this implies that the substance which is the origin of the radio-activity is one having definite chemical properties.

152. Emanating Power. The loss of radio-activity of the thorium hydroxide treated in the way described above is accompanied also by a loss of emanating power, while the Th X possesses this power to a very large extent when first formed: it is found that as the thorium hydroxide recovers its radio-activity it also recovers pari passu its emanating power, while the emanation from the Th X becomes smaller and smaller and finally disappears. This is what would happen if the Th X split up after its formation, one of the products of the decomposition being the emanation.

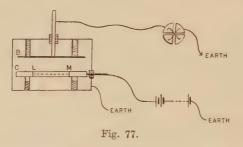
An interesting question is what becomes of the dead Th X and the dead emanation; since the Th X is only active for about

a week, the amount of the spent Th X to the active will be the ratio of the age of the thorium compound to one week. As the life of the emanation is very much shorter the proportion of the spent emanation to the active will be very much larger. Is it possible that the gases like helium and argon which are so often found in minerals containing radio-active substances represent the accumulations of spent emanations? The chemical inertness which is so marked a feature of these gases is also as we have seen a characteristic of the emanation.

153. Debierne\* by extracting the thorium from pitchblende obtained an exceedingly radio-active product, he ascribed this activity to the presence of a new element, which he named 'actinium'; he was not able to separate the actinium from the thorium.

### Induced Radio-activity produced by Thorium Emanation.

154. Rutherford† discovered that the emanation from thorium makes any substance with which it comes in contact radioactive. This can be shown by the following experiment (Fig. 77).



Two isolated plates B and C are placed parallel to one another in a closed metallic vessel connected with the earth. In a shallow depression, LM, in the plate C, a layer of thorium oxide is placed and covered with several layers of foolscap paper. The plate C is connected to the positive pole of a battery, giving a potential difference of at least 50 volts, and the other pole of this battery is connected with the earth. The plate B is connected with an electrometer. If this is left for several hours, and then the

<sup>\*</sup> Debierne, Comptes Rendus, exxix. p. 563, 1899; exxx. p. 906, 1900.

<sup>+</sup> Rutherford, Phil. Mag. v. 49, p. 161, 1900.

plate C with the thorium removed, and replaced by a clean metallic plate, it will be found that the gas between the plates now possesses considerable conductivity; this will gradually diminish with lapse of time and after a few days become inappreciable. If, instead of leaving B in the vessel when C is removed, both B and C are replaced by fresh plates, there will be no conductivity; the ionisation is thus due to some change produced in the plate B by the action of the thorium. The plate B has been made radio-active. That this effect is due to the action of the emanation and not of the straight line radiation may be proved in several ways. In the first place, the effect is absent if we use a thin layer of thorium oxide, which emits plenty of straight line radiation but very little emanation. Again, when we de-emanate thorium oxide by intense heating (see p. 289), we destroy its power of producing induced radio-activity, although we do not affect its power of emitting straight line radiation.

The close connection between the emanation and the induced radio-activity is shown by the following experiment made by Rutherford.

A slow current of air from a gas-bag passed down a rectangular wooden pipe, 60 cm. long; the air passed through sulphuric acid to dry it, and through a plug of cotton-wool in the pipe at W, this plug removed spray and equalised the flow of air over the cross section of the tube. A metal plate charged with positive electricity covered the bottom of the tube, four insulated metal plates A, B, C, D, placed at equal intervals, had a negative charge induced on them by being connected with the earth. When the current of air passed through the vessel with the velocity 2 cm./sec. for 7 hours, with a potential difference of 300 volts between the lower and upper plates, the following results were obtained:

	Relative current due to emanation	Relative excited radio-activity
Plate A " B " C " D	16 *55 *18 *072	1 ·43 ·16 ·061

Thus the induced radio-activity is approximately proportional to the intensity of the radiation given out by the emanation.

The experiment shows that the emanation is in some way the cause of the induced radio-activity; it does not enable us to decide whether the radio-activity is due to a deposit of the substance of the emanation on the plate, or whether it is due to a change in the surface layers of the plate produced by the radiation coming from the emanation. We shall return to this point when we have discussed more fully the properties of the induced radio-activity.

If in the inclosure containing the thorium and the emanation there is a conductor strongly charged with negative electricity, the induced radio-activity will be concentrated on this conductor and there will be less on the walls of the inclosure than there would be if the conductor were uncharged; thus the excess of radio-activity on the wire is obtained at the expense of that on the surrounding objects.

The amount and quality of the induced radio-activity seem to be independent of the material of which the walls of the inclosure are made; the substitution of paper or cardboard for metal makes no appreciable difference in the result. The radio-activity does not depend upon the nature of the gas in the inclosure, nor upon the pressure of the gas, although the concentration of the induced radio-activity on negatively electrified surfaces is less complete at low pressures than it is at high. Thus, for example, in an experiment made by Rutherford the induced radio-activity on a negatively electrified wire was practically unchanged when the pressure was reduced from 760 mm. to 16 mm.; at a pressure of 5 mm. however, it was about 1/20 of its value at the higher pressure; this diminution in the radio-activity of the wire is accompanied by an increase in that of the walls of the inclosure.

155. Duration of the induced radio-activity. This induced radio-activity dies away gradually with the time; the rate of decrease is, however, very slow, as Rutherford's measurements show that it takes about 11 hours for the intensity of the radiation to fall to 1/2 of its original value. The rate at which the radiation dies away does not depend upon the nature of the material which is made radio-active. The duration of the induced radio-activity

is thus very much greater than that of the emanation which produced it, as we have seen that this fades away to one-half its original value in one minute. We must remember, however, that this relates to the emanation when it has escaped from solids and is in a form analogous to that of a free gas, we do not know whether the rate of decay is as great as this when the emanation is diffusing through a solid: the results of experiments seem rather to indicate that it is not, for the emanation is still active after passing through a great many sheets of paper; if its rate of decay when in the paper is as rapid as it is when in the air it must be able to diffuse through these in a very few minutes.

A surface once made radio-active can be exposed to very rough usage without losing this property; thus Rutherford raised a piece of radio-active platinum to a white heat and found after cooling that it had lost little if any of its activity. Washing the surface with hot or cold water, caustic soda, or nitric acid has no effect upon the activity; if, however, the wire is dipped in sulphuric or hydrochloric acid the radio-activity is removed in a few minutes: the radio-activity is however only removed from the metal to the acid, for on evaporating down to dryness the residue left was found to be strongly radio-active. It would thus appear that the radio-activity substance is dissolved in the acid and retains its radio-activity.

No change in weight due to the induced radio-activity can be detected, nor does microscopic examination of the metal reveal the presence of any dust or any change in the surface. The radio-activity can be removed by long scouring with sand or emery paper, the pieces removed are radio-active.

156. Time taken to produce the Radio-activity. The radio-activity takes considerable time to produce. On first exposure to the emanation it increases nearly proportionally with the time, afterwards the rate of increase falls off, and it ultimately attains a constant value. The following diagram (from Rutherford's paper) shows how the intensity of the induced radiation increases with the time of exposure to the thorium.

The time taken to attain a steady state is fixed by the rate at which the induced radiation fades away. For let I be the intensity of the induced radio-activity at any time t, q the rate at which

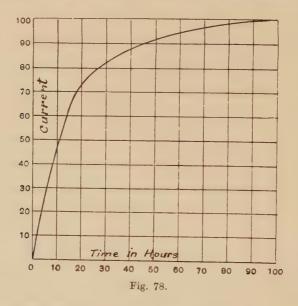
this is increasing in consequence of the presence of the thorium, I/T the rate at which it would decay if no thorium were present, then we have

$$\frac{dI}{dt} = q - \frac{I}{T},$$

$$I = qT\left(1 - e^{-\frac{t}{T}}\right) \dots (1),$$

or

thus the radio-activity will not reach a steady state until t is considerably greater than T. Now T has been determined by



Rutherford by measuring the rate at which the activity of the surface disappears when it is not exposed to the action of thorium; putting q = 0 we get

$$I = I_0 e^{-\frac{t}{T}},$$

where  $I_0$  is the value of I when t=0; Rutherford found that I fell to  $\frac{1}{2}I_0$  in about 11 hours, so that T=16 hours; thus it will take a time greater than 11 hours but comparable with it for the induced radio-activity to reach a steady state. We see from equation (1) that the induced radio-activity should reach half its final value in about 11 hours; an inspection of Fig. 78 will show that this is the case.

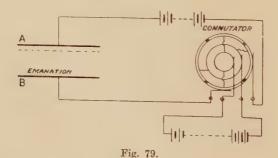
# Penetrating power of the induced Radio-activity.

157. Rutherford measured the penetrating power of the induced radiation and found that it was considerably greater than that from thin layers of the thorium itself. Thus the latter is reduced to half its intensity after passing through about 1 cm. of air at atmospheric pressure, while the induced radio-activity can pass through 1.65 cm. before its intensity is reduced by the same The penetrating power of the induced radio-activity is independent of the nature of the substance made radio-active; this is a strong indication that the induced radio-activity is due to a deposit of the emanation and not to an alteration of the surface of the substance by radiation from the emanation. Further evidence on this point could probably be obtained by observing at different air pressures the distances from the thorium at which a substance can be made radio-active. For if it is due to a deposit of the emanation the experiment described on p. 295 shows that the emanation must be deposited while it is radio-active, i.e., not much longer than a minute after it has left the thorium. If the substance to be made radio-active is placed so far away from the thorium that the emanation takes much more than a minute to diffuse to it, the emanation will be spent before it reaches the surface and this will not become radio-active. Now the distance through which the emanation can diffuse in a time Tis proportional to  $\sqrt{DT}$  where D is the coefficient of diffusion of the emanation; as D varies inversely as the pressure of the gas the distance at which a surface could become radio-active would be inversely proportional to the square root of the pressure. If, however, the induced radio-activity were due to the radiation given out by the emanation, then since the transparency of a gas to the radiation is inversely proportional to the pressure the distance at which a surface could be made radio-active would be inversely proportional to the pressure and not, as in the preceding case, to the square root of the pressure.

The effect produced by negative electrification in increasing the induced radio-activity on a surface thus electrified is, I think, probably connected with the property possessed by several radioactive substances, for example uranium and radium, of emitting negatively electrified corpuscles. Let us trace the consequences of supposing that the radio-active emanation from thorium possesses this property. As the radio-activity of the particles we have seen only lasts for a short time, it is probable that most of the particles will be spent before they have time to emit these negative corpuscles. But the particles which succeed in doing this and which thereby acquire a charge of positive electricity will now be attracted by the negatively electrified surface and will move rapidly up to it. The velocity with which the particle moves in the electric field is very great compared with the velocity with which it would have moved towards the surface if only diffusion had come into play. Thus the emanation will in consequence of the charge on the surface arrive at the surface very much sooner than it would have done if there had been no charge; it thus arrives very much fresher and is much more efficient as a producer of induced radio-activity.

158. The velocity acquired by the positively charged particles of the emanation when in the electric field has been measured by Rutherford\*, using the following method, which is based on the assumption—justified by the extent to which the induced radio-activity can be concentrated on a negatively electrified surface—that the radio-activity of the surface is almost wholly due to the number of positively electrified particles which reach it.

The emanation spreads between two parallel plates A and B, Fig. 79, an electric field is produced between the plates, this field



consists of two parts, (1) a constant potential difference equal to  $E_0$  making the top plate +, the lower plate -, (2) a field in which

<sup>\*</sup> Rutherford, Physikalische Zeitschrift, iii. p. 210, 1902; Phil. Mag. vi. 5, p. 95, 1903.

the direction of the force is reversed at equal intervals of time T; thus it is equal to  $E_1$  for a time T, then changes to  $-E_1$  which lasts for a time T, when it changes again to  $+E_1$  and so on. This variable potential difference is placed in series with the constant potential difference, so that in the first half of the alternation the electric force acting downwards is  $(E_0 + E_1)/d$  where d is the distance between the plates, while in the second half of the alternation it is equal to  $(E_1 - E_0)/d$  and acts upwards:  $E_1$  is supposed to be greater than  $E_0$ . There is thus on the average a tendency to make the positive ions go to the lower plate, but during the second half of the alternation some of the particles will be attracted to the upper plate and will make it radio-active: the number of such particles will depend upon the velocity of the particles and may be calculated as follows.

Let K be the velocity of the particles under unit electric force and let us suppose that the positive particles are being produced uniformly between the plates, the number produced in one second in a layer of unit thickness between the plates being q. The particles which reach the upper plate when negatively electrified will be of two classes: (1) those produced whilst the plate is negatively electrified, and (2) those which were present between the plates at the beginning of the alternation. Let us take first the number in the first class; consider the number sent to the top plate by a layer of thickness dx at a distance x away from it, any particle from this layer, since it moves with the velocity  $KX_1$ , will take the time  $x/KX_1$  to reach the plate.  $X_1$  is the electric force between the plates and is equal to  $(E_1 - E_0)/d$ . Since the particle must reach the plate before the end of the alternation the latest time it can start is  $x/KX_1$  before the end, and thus the particles reaching the layer are only formed for a time  $T - x/KX_1$ ; thus the number of particles reaching the plate from this layer is  $q(T-x/KX_1) dx$  and the total number of particles in class (1) is equal to

 $\int_0^{KX_1T} q(T - x/KX_1) dx$   $= \frac{1}{2} qKX_1T^2.$ 

The number in class (2) will be the number of positive particles at the beginning of the alternation in a layer next the upper plate whose thickness is  $KX_1T$ . The force in the preceding alternation

tending to drive the particles from the upper plate is  $X_2$  where  $X_2 = (E_0 + E_1)/d$ : hence the velocity of the particles is  $KX_2$ : the number of particles produced in a layer of thickness dx, at a distance x from the upper plate, which have not moved by the end of the alternation to a distance from the upper plate greater than

 $KX_1T$  is  $q\frac{(KX_1T-x)}{KX_2}dx$ ; hence the number of particles in the second class is equal to

$$\int_0^{KX_1T} q \, \frac{(KX_1T - x)}{KX_2} \, dx$$
$$= \frac{1}{2} q \, \frac{K \cdot X_1^2 T^2}{X_2}.$$

Thus the total number of positive particles reaching the upper plate in the time of a double alternation of length 2T

$$= \frac{1}{2} q K X_1 T^2 \left( 1 + \frac{X_1}{X_2} \right).$$

In this time the total number of positive particles produced is 2qdT, and if care is taken to make the electric field sufficiently strong all these particles will reach one or other of the plates. Hence  $\rho$  the ratio of the number of particles reaching the upper plate to the sum of the numbers reaching the upper and lower plates is given by the equation

$$\rho = \frac{1}{4} \frac{K X_1 T^2}{d} \left( 1 + \frac{X_1}{X_2} \right),$$

or substituting for  $X_1$  and  $X_2$  their values we get

$$\rho = \frac{1}{2} K T^2 \frac{(E_1 - E_0)}{d^2} \frac{E_1}{E_1 + E_0} \dots (1).$$

On the hypothesis already mentioned, that the induced radio-activity is almost entirely caused by the positively charged particles which come up to the plate,  $\rho$  is the ratio of the radio-activity of the upper plate to the sum of the activities of the upper and lower plates, and by measuring these activities  $\rho$  can be determined; when  $\rho$  is known equation (1) gives us the means of determining K and hence the velocity of the positively charged particles in an electric field. By this method Rutherford got the following results.

Plates 1:3 cm. apart.

$E_1 + E \\ \text{volts}$	$E_1 - E_{ m volts}$	Alternations per sec.	ρ	Velocity for one volt per cm.
152	101	57	·27	1·25
225	150	57	·38	1·17
		Plates 2 cm. a	part.	
272	207 200	44	·37	1·47
300		53	·286	1·45

These results relate to air at atmospheric pressure. Zeleny (p. 47) found that the velocity of the positive ion produced by Röntgen rays in air at this pressure was 1.36 cm./sec. for the potential gradient of a volt per cm.: the velocity of the positive particles in the thorium emanation is thus within the limits of experimental errors equal to the velocity of the ordinary positive ions.

Rutherford has shown that at low pressures, say less than 1 mm., of mercury there is less tendency for the radio-activity to be concentrated on the negative electrode than there is when the pressure is higher. We see that if the mean free path of the particle were comparable with the size of the vessel there ought not on the preceding view to be much concentration unless the particles were at rest, or at any rate were moving with a velocity small compared with that which would be developed by the movement of the charged particles through a fall of potential equal to that between the negatively electrified body and the walls of the vessel: for it is only in the latter case that the particle would strike the attracting body, in all others it would describe an orbit round it and would strike the walls of the vessel and not the electrode itself.

# Radio-activity of Radium, Polonium, Actinium.

The Becquerel rays have led to the discovery of some new substances possessing the power of radio-activity to a far greater extent than uranium—the original source of these rays. After Becquerel's discovery Monsieur and Madame Curie\* made a very

<sup>\*</sup> Curie, Rapports, Congrès International de Physique, t. iii. p. 79, Paris, 1900.

systematic and extensive examination of a great number of chemical elements and compounds, and also of minerals, to see if other elements possessed powers similar to uranium; the examination of the elements and compounds (which included the rare elements, gallium, germanium, neodydymium, praseodydymium, mobium, scandium, gadolinium, erbium, samarium, rubidium, yttrium, ytterbium, holmium) did not lead to the discovery of any substances other than uranium possessing this property. The investigation of the minerals was more fruitful, for they found that several minerals containing uranium were more active than the same bulk of uranium. This is shown by the following table in which  $\iota$  is the saturation current in ampères between two circular plates 8 cm. in diameter and 3 cm. apart when one of the plates is covered with the substance under consideration:

	$\iota \times 10^{11} \mathrm{ampères}$		$\iota \times 10^{11} \mathrm{ampères}$
Metallic Uranium Pitch-blende from	2.3	Thorite	1·4 2·0
Johanngeorgenstadt		Monazite	0.5
Joachimstal Pribran	7·0 6·5	Xenotime	0.03
Cornwall	1.6	Fergusonite	- ,
Cleocite	1·4 5·2	Samarskite Niobite	1·1 0·3
Autunite	2.7	Carnotite	

All these minerals contain uranium and thorium, but it will be seen that several of them are more radio-active than the pure metals: this suggests that they may contain some exceedingly active substantives other than uranium, this supposition was strengthened when Monsieur and Madame Curie prepared Chalcolite artificially from pure substances and found that it was only about one-fifth as radio-active as the natural mineral. They then set to work to search pitch-blende systematically; they tested the radio-activity of a certain piece, then separated this chemically and tested that of the constituents, and thus gradually separated the active from the inert parts of the pitch-blende. This treatment has led to the discovery of three different strongly radio-active constituents of pitch-blende; radium discovered by Monsieur and Madame Curie and Monsieur Bemont\*, polonium discovered

<sup>\*</sup> Curie and Bemont, Comptes Rendus, exxvii. p. 1515, 1898.

by Monsieur and Madame Curie\*, and actinium by Monsieur Debierne†. Radium accompanies the barium prepared from pitch-blende, and in its chemical actions is similar to that metal; it can, however, be separated from barium by fractionation, as its chloride is less soluble in water, in alcohol and in hydrochloric acid. The amount of radium in pitch-blende is exceedingly small, many thousand kilograms of this mineral only yielding a few decigrams of a radio-active substance, of which only a small fraction is radium. The spectrum of radium was examined by Demarçay‡: the following are the principal lines between wave-lengths 5000 and 3500.

Wave-length	Intensity	Wave-length	Intensity
4826.3	10	4600.3 ?	3
4726.9	5	4533.5	9
4699.8	3	4436.1	8
4692.1	7	4340.6	12
4683.0	14	3814.7	16
4641.9	4	3649.6	12

There are also two nebulous bands in the spectrum, one extending from 4631.0 to 4621.9 with the maximum at 4627.5;



Fig. 80.

the second begins suddenly at 4463.7, has a maximum from 4455.2 to 4453.4, fading away at 4390. The appearance of the spectrum is shown in Fig. 80.

The sensitiveness of the test by radio-activity is shown by the fact that it required several thousand times more radium to give

<sup>\*</sup> Curie, op. cit. p. 175.

<sup>+</sup> Debierne, Comptes Rendus, exxix. p. 593, 1899; exxx. p. 906, 1900.

<sup>†</sup> Demarcay, Ib. cxxvii. p. 1218, 1898; cxxix. p. 116, 1899; cxxxi. p. 258, 1900.

an appreciable spectrum than to give an amount of radio-activity quite appreciable by electrical methods.

The atomic weight of radium has been determined by Monsieur and Madame Curie\* to be 225. Runge and Precht from consideration based on its spectrum estimate the atomic weight as 257.8.

The radiation from radium is extraordinarily intense. Monsieur and Madame Curie have prepared specimens of radium which when enclosed in a lead tube '5 cm. thick will discharge an electroscope more readily than uranium, even although the latter is brought without any covering close up to the electroscope.

The radiation comprises rays of three classes: (1) easily absorbed rays not deflected by a magnet nor by an electric field, (2) much more penetrating rays which are deflected by magnetic or electric fields and which carry a charge of negative electricity, (3) rays still more penetrating which are not deflected.

All the radium salts are luminous and retain this property for long periods: Giesel§ found that the luminosity diminished in damp air but recovered its brightness on drying.

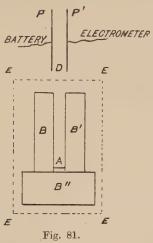
The activity of the radium salts like some of those of thorium (see p. 289) increases for some time after precipitation. The following numbers are given by Curie; initial activity 95, after 1 day 120, after 2 days 165, after 3 days 210, after 9 days 310, after 24 days 381, after 300 days 410. If the chloride after attaining its maximum activity is dissolved and reprecipitated the activity of the new product diminishes as the time it is kept in solution increases; it reaches, however, a limit after the salt has been four or five days in solution. It would be interesting to know if the increase in activity observed for some time after the preparation of the radium compounds occurs in all the three classes of rays given out by these substances or is confined to one class.

- \* Curie, Comptes Rendus, July 21, 1902.
- † Runge and Precht, Physik. Zeit. iv. p. 285, 1903.

<sup>‡</sup> Rutherford has quite recently shown that the rays of class 1 are slightly deflected by magnetic or electric fields and that they carry a positive charge; he found that the velocity of these rays was of the order  $2 \times 10^9$  cm./sec. and e/m of the order  $6 \times 10^3$ . Phil. Mag. vi. 5, p. 177, 1903. Strutt (Phil. Trans., A, 1901, vol. exevi. p. 525) had previously suggested that the undeflected rays consisted of positive ions.

<sup>§</sup> Giesel, Wied. Ann. lxix. p. 91, 1899.

159. The magnetic deflection of rays given out by some radioactive substances was observed almost simultaneously by Giesel\*, Meyer and v. Schweidler†, and Becquerel‡. Giesel used impure polonium (polonium free from radium does not give deviable rays), Meyer and v. Schweidler impure polonium and radium, and Becquerel radium. Becquerel's experiments on radium, proving both the magnetic and electric deflections of the rays and showing that these deviable rays consist of corpuscles projected with a velocity about two-thirds of that of light, have already been described. M. and Mme Curie§ showed that radium gave out non-deviable as well as deviable rays and that the former were much more easily absorbed than the latter. The arrangement they used is represented in Fig. 81. A is the radio-active substance placed



between blocks of lead, B, B', the radiation from A passes between these blocks into the space between the parallel plates P, P', making the air between these a conductor and allowing a current to pass between the plates, the magnitude of the current serving as a measure of the intensity of the radiation reaching the space between the plates. P is charged up to 500 volts and P' connected with an electrometer. The arrangement B, B', B'' can

<sup>\*</sup> Giesel, Wied. Ann. lxix. p. 831, 1899.

<sup>†</sup> Meyer and v. Schweidler, Wien. Ber. p. 323, 1899. Physik. Zeitschr. i. p. 113, 1899.

<sup>‡</sup> Becquerel, Comptes Rendus, cxxix. p. 997, 1899.

<sup>§</sup> Curie, Ib. cxxx. p. 73, 1900.

be placed between the poles of an electro-magnet which produces a strong magnetic field at right angles to the plane of the paper; if the rays are deflected even to a slight extent they will strike against the block B, B' and be suppressed.

The effects produced by the magnet depend essentially upon the distance AD between the radio-active substance and the place where it is tested; if this distance is greater than 7 cm. all the rays are suppressed by a magnetic field of 2500 units; at a distance of 6.5 centimetres only a portion of the rays are suppressed and this portion gets smaller and smaller as the plates P and P' approach the radio-active substance A; that the escape of the rays from the magnetic field is not due to a deficiency in the strength of the field is shown by the fact that when the magnetic field is on no further diminution in the current is produced when the strength of the field is increased from 2500 to 7000 units. The following numbers show the effects observed at different distances, the current when the magnetic field is off being taken as 100, so that the numbers representing the current with the field on may be taken as the percentage of non-deviable rays which are able to penetrate the various distances through air at atmospheric pressure.

> Distance AD in centimetres 7.1, 6.9, 6.5, 6.0, 5.1, 3.4 Current with magnet on 0, 0, 11, 33, 56, 74

If the radio-active substance is covered with a piece of thin aluminium foil or a piece of black paper all the non-deviable rays are absorbed by it and the current is completely stopped by the magnetic field. It will be seen from the preceding figures that only a small fraction of the total ionisation produced by the radium is due to the rays which are deflected by a magnet; by far the larger part of it is produced by the non-deviable easily absorbed rays.

160. That these deviable rays carry a charge of electricity is proved by the fact discovered by Becquerel (see p. 111) that they are deflected when placed in an electric field, a fact also observed by Dorn\*. M. and Mme Curie+ had previously shown by direct experiment the existence of the negative charge on these rays. If we place a body near a sample of radium surrounded by air at

<sup>\*</sup> Dorn, Comptes Rendus, cxxx. p. 1126, 1900.

<sup>+</sup> Curie, Ib. p. 647.

atmospheric pressure we cannot expect to observe any appreciable negative charge on the body, for the radium makes the air a conductor so that the electricity escapes from the body through the air as fast as it arrives. To observe the effect we must work in a high vacuum where there is not enough gas to produce appreciable conductivity or else replace the air by a solid dielectric; the Curies employed the latter method; the arrangement they used is shown in Fig. 82. A metal disc MM is connected by a wire with an

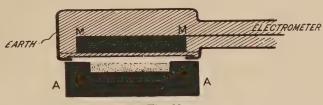


Fig. 82.

electrometer, the disc and wire being completely surrounded by a solid insulator,—ebonite or paraffin,—the whole is placed in a metallic case connected with the earth, the layer of insulating material and the metal of the case are very thin next the lower face of the disc MM. This lower face is exposed to the radiation from the radium R placed in a cavity in a block of lead AA. It is found that under these circumstances the disc receives a constant stream of negative electricity. This current is only small; from a layer of radium with a surface of 2.5 sq. cm. and 2 cm. thick, and with the rays passing on their way to the disc through aluminium foil 01 mm. thick and a layer of ebonite 3 mm., the current was  $10^{-11}$  ampères.

The Curies also detected the positive charge left behind on the radium; to do this they connected the lead containing the radium with the electrometer and surrounded it by an insulating substance as is shown in Fig. 82; under these circumstances they found that the electrometer received a positive charge.

Since  $e/m = 10^{-7}$  a current of  $10^{-11}$  ampères from the radium corresponds to a loss in weight of about one three-hundredth part of a milligram in a million years.

No charge could be detected on the non-deviable rays, but with those rays on account of the great absorption the experiment is exceedingly difficult.

161. The properties of the deviable rays, i.e. their deflection by magnetic and electric fields, and the possession of a negative charge show that like the cathode rays they consist of negatively electrified corpuscles moving with great velocities; the velocity of some of the particles projected from radium, viz.  $2 \times 10^{10}$  cm./sec., is greater than that we have yet been able to give to any corpuscles by purely electrical means. Additional confirmation of the similarity between the deviable radium rays and cathode rays is given by the study of the absorption of these rays by various bodies. Lenard\* showed that if a bundle of cathode rays is travelling parallel to the axis of x, and if  $I_0$  is the intensity of the rays when x = 0 and I the intensity after travelling a distance x, then  $I = I_0 e^{-\lambda x}$ , where  $\lambda$  is a constant, called the coefficient of absorption of the cathode rays. By testing a great number of substances with densities varying from that of solid platinum to that of hydrogen gas at 3 mm. pressure, Lenard found that whatever the state of the substance might be, solid or gaseous,  $\lambda$  was very approximately proportional to the density of the substance; how nearly this law holds will be seen from the following table in which  $\lambda$  is the coefficient of absorption and d the density; the

Substance	λ cm1	d . gr./cm. <sup>3</sup>	$\lambda/d$
Hydrogen at 3 mm. pressure Air at '78 mm. pressure	00149	3.6 × 10 <sup>-7</sup>	4040
Hydrogen at 760 mm. pressure	*00416 *476	$1.2 \times 10^{-6}$ $8.5 \times 10^{-5}$	3330 5610
Air " " " " " " " " " " " " " " " " " " "	3·42 8·51	$1.2 \times 10^{-3}$ $2.7 \times 10^{-3}$	2780 3110
Collodium	3310 2690	1·1 1·30	3010 2070
Glass	7810 7150	2·47 2·70	3160
Mica Dutch Metal	7250	2.80	2650 2590
Silver	23800 32200	8·90 10·5	2670 3070
Gold	55600	19:3	2880

rays were produced by a tube for which the potential difference between the electrodes was about that which would produce a spark in air about 2.8 cm. long: from some later determinations

<sup>\*</sup> Lenard, Wied. Ann. lvi. p. 255, 1895.

made by Lenard\*, I should conclude that this corresponded to a velocity of the cathode rays of about  $6 \times 10^9$  cm./sec.

Thus though the density of the lightest substance is only about one sixty-millionth of that of the heaviest, the values of  $\lambda/d$  only range from 2070 to 5610: and if we leave out hydrogen, which as we shall see exhibits peculiarities in its absorption of all rays, the range is only from 2070 to 3330; considering the difficulties of the experiment this is strong evidence in favour of  $\lambda/d$  being very nearly constant.

R. J. Strutt<sup>†</sup> has measured the coefficient of absorption of the deviable radium rays for a considerable number of substances; his results are given in the following table.

Substance	λ	d	$\lambda/d$
Platinum	157.6	21.5	7.34
Lead	62.5	11.4	5.48
Silver	65.7	10.6	6.20
Copper	49.2	8.95	5.50
Iron	52.2	7.76	6.74
Tin	51.2	7.3	7.01
Zinc	40.3	7.2	5.58
Mica	10.8	2.74	3.94
Glass	12.5	2.73	4.58
Aluminium	11.6	2.7	4:30
Celluloid	5.45	1:36	4.01
	4.77	1.14	4.18
Ebonite	3.84	1.0	3.84
Card	0413	00758	5.45

Thus though there is a very wide range in the values of  $\lambda$  and d, the values of  $\lambda/d$  differ comparatively little from each other. The coefficients of absorption for the cathode rays are roughly about 500 times those for the radium rays; this difference is probably due to the much greater velocity of the radium rays, which was found by Becquerel to be as great as  $2 \times 10^{10}$  cm./sec., while the velocity of the cathode rays used by Lenard was probably only about one-quarter of this.

Strutt<sup>†</sup> has made a series of measurements of the amount of ionisation produced by the two types of radium rays and the

<sup>\*</sup> Lenard, Wied. Ann. lxv. p. 504, 1898.

<sup>+</sup> Hon. R. J. Strutt, Nature, lxi. p. 539, 1900.

<sup>‡</sup> Hon. R. J. Strutt, Phil. Trans. A. 196, p. 507, 1901.

rays from polonium when they pass through different gases. Rutherford's results (see p. 249) indicate that the amount of ionisation would be proportional to the coefficient of absorption of the rays in the gas. Strutt's results are given in the following table (p. 313), which for convenience of comparison contains the relative ionisation produced by Röntgen rays as determined by Perrin and J. J. Thomson and also the relative ionisation produced by cathode rays as determined by McClennan\*.

162. Thus for the cathode rays and the deflectable Becquerel rays, the coefficient of absorption depends only upon the density and not upon the chemical composition or physical state of the substances; the non-deviable, easily absorbable Becquerel rays approximate to this law but deviate from it sensibly more than the deflectable rays, while in the case of the Röntgen rays there is no approximation to this law. An inspection of the result shows that hydrogen is anomalous, the ionisation for the deflectable rays being very considerably greater than its density warrants. The law of absorption for those rays which consist of rapidly moving negatively electrified corpuscles is of great interest in connection with the theory of the structure of matter. For it is exactly the result we should expect if the molecules of the different chemical elements consisted of differently arranged aggregations of a primordial atom, the number of these atoms in the molecule being proportional to the mass of the molecule, i.e. to its molecular weight; then if the corpuscles forming the cathode or deflectable Becquerel rays are so small that they can thread their way between the individual primordial atoms in the molecules of the chemical elements, the collisions the corpuscles make when passing through any body are collisions with the primordial atoms in the molecule rather than with the molecule as a whole. Thus the mean free path of a corpuscle will be inversely proportional to the number of primordial atoms in unit volume; this number since all these atoms are to be considered as having the same mass will be proportional to the mass of unit volume of the substance, hence the mean free path of the corpuscles will be inversely proportional to the mass of the substance and will, if the mass is kept constant, not be affected by any changes in its chemical composition or physical state. If L is the

<sup>\*</sup> McClennan, Phil. Trans. A. 195, p. 49, 1901.

RELATIVE IONISATIONS.

Gas         Helative donsity         J. J. J. J. J. J. A.         Permin type         Permin type			Röntgen rays	ı rays		Radium rays	ı rays	Polonium rays	m rays	
0693         .33         .026         .069         .157         .218         .226         .219           1.00         1.0		Relative density	J. J. THOMSON	Perrin	Cathode	Penetrating type	Absorbable type	H	ii.	Uranium
1.00         1.00 <th< td=""><td></td><td>6690</td><td>.33</td><td>970.</td><td>690-</td><td>151</td><td>.218</td><td>.226</td><td>219</td><td>213</td></th<>		6690	.33	970.	690-	151	.218	.226	219	213
1.11       —       —       1.106       1.21       —       1.16       —         1.27       8.9       8       —       1.46?       —       —       —         1.53       1.4       1.34       1.53       1.57       —       —       —         1.86       1.05       —       —       1.86       —       1.94       —         2.19       6.4       6       —       2.32       1.92       2.04       2.03         4.32       —       —       4.89       —       4.44       —         5.05       —       —       4.89       —       4.44       —         5.31       —       —       6.18       3.74       —         5.31       —       —       5.83       —       5.34       —	:	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
1.27     8.9     8     —     1.46?     —     —     —     —       1.53     1.4     1.34     1.53     1.57     —     —     —       1.86     1.05     —     —     1.94     —       2.19     6.4     6     —     2.32     1.92     2.04     2.03       4.32     —     —     4.89     —     4.44     —       5.05     —     —     6.18     3.74     3.51     3.47       5.31     —     —     5.83     —     6.34     —	:	11.11		1	1.106	1.21		1.16	1	I
1.53     1.4     1.34     1.53     1.57     —     1.54     —       1.86     —     —     1.94     —       2.19     6.4     6     —     2.32     1.92     2.04     2.03       4.32     —     —     4.89     —     4.44     —       5.05     —     —     6.489     —     4.44     —       5.31     —     —     5.18     3.74     3.51     3.47       5.31     —     —     5.83     —     5.34     —	gas	1.27	6.8	œ	1	1.46 ?	1			-
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2·19     6·4     6     -     2·32     1·92     2·04     2·03       4·32     -     -     4·89     -     4·44     -       5·05     -     -     -     5·18     3·74     3·51     3·47       5·31     -     -     -     5·83     -     5·34     -	:	1.86	1.05	l	-	1.86	[	1.94	ementes	1
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5.05     -     -     -     5.18     3.74     3.51     3.47       5.31     -     -     -     5.83     -     5.34     -		4.32			1	4.89	1	4.44		
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	ide	5.31	1	ŀ	-	5.83	l	5.34	1	

mean free path of a corpuscle and if we suppose that at each collision the corpuscle loses the fraction  $\beta$  of its kinetic energy, then  $\lambda$  the coefficient of absorption  $= \beta/L$ , and as L is inversely proportional to the density of the substance we see that  $\lambda$  ought to be proportional to the density, a law which the results we have quoted show to be very approximately true.

163. The penetrating power of the radium rays is much greater than that of the cathode rays produced by electrical means; this can readily be accounted for by the greater velocity of the corpuscles in the former rays if we regard the collisions which take place between the corpuscles and the primordial atom as analogous to the deflection two bodies exerting forces on each other experience when they pass one another at close quarters. Taking this view of a collision let us define a collision as a case where the corpuscle and the primordial atom come so close together that the angle through which the direction of motion of the path of the former is twisted exceeds a certain value. This deflection depends upon the initial velocity of the corpuscle and its minimum distance from the atom; and the theory of central forces shows that a collision will not occur if the kinetic energy of the corpuscle, when so far away from the atom that the force between them is inappreciable, exceeds a certain multiple of the work done on the corpuscle by the atom when the former moves from an infinite distance to its point of nearest approach to the atom. To take a definite case, let us suppose that the forces between the corpuscle and the atom are electrical in their origin and that the charges on the atom and corpuscle are equal, then if m is the mass of a corpuscle, e its charge in electrostatic measure, v its velocity at an infinite distance from the atom, d the least distance between the atom and corpuscle; then the work done on the corpuscle is  $e^2/d$  and the condition for a collision is that

 $\frac{e^2}{d}$  should not be less than  $\frac{1}{2}kmv^2$ ,

where k is a numerical constant. Thus d cannot be greater than  $2e^2/kmv^2$ . We may get a rough idea of the effect due to the velocity if we take this value of d as the radius of the sphere of action of the atom, and suppose a collision to occur whenever a corpuscle passes through this sphere. Now the mean free path

varies inversely as the square of the radius of the sphere of action, thus for this law of force the mean free path will be directly proportional to the fourth power of the velocity. The coefficient of absorption (which see p. 314) is equal to  $\beta/L$ , where L is the mean free path, hence neglecting any variation in  $\beta$  the coefficient of absorption will vary inversely as the fourth power of the velocity of the corpuscles: thus a theory of this kind will explain why the penetrating power of the more rapidly moving corpuscles in the deflectable radiation is so much greater than that of the cathode rays in Lenard's experiments. The essential condition for the penetrating power of the corpuscles to be independent of everything except the density of the substances through which they are passing is that the collisions which impede the progress of the corpuscles should be collisions with the individual primordial atoms and not collisions with the molecule as a whole; for this condition to be satisfied it is evident that the sphere of action of one primordial atom must not include other atoms, or if D is the distance between two atoms, D must be greater than  $2e^2/kmv^2$ , or  $v^2$  must be greater than  $2e^2/kmD$ . If  $v^2$  is smaller than this we cannot expect the simple law of absorption which holds for the very rapidly moving corpuscles to apply. Now in electrostatic measure  $e/m = 3 \times 10^{17}$ ,  $e = 3.4 \times 10^{-10}$ , and we shall assume that D is 10<sup>-9</sup>. Substituting these values we see that  $v^2$  must be greater than  $2 \times 10^{16}/k$  or v greater than  $1.4 \times 10^8/k^{\frac{1}{2}}$ . Thus if the velocity of the corpuscle falls below a value somewhere between  $10^8$  and  $10^7$  cm./sec., we should expect the law  $\lambda/d = {\rm constant}$  to fail

For velocities smaller than this the collisions made by a corpuscle are to be regarded as taking place between the corpuscle and the molecule of the substance rather than with the constituent primordial atoms of the molecule, and when this is the case the mean free path of the corpuscle, say in hydrogen, will be four times that of a molecule of hydrogen at the same pressure: the factor 4 has to be introduced because the size of a corpuscle is negligible compared with that of a molecule, so that the radius of the sphere of action in a collision between a corpuscle and a molecule is one-half of that between two molecules.

It is of some interest to form an estimate of the mean free path of a rapidly moving corpuscle, although we are not yet in a

position to evaluate all the constants that occur in the expression for the free path. By the Kinetic Theory of Gases, L, the mean free path of a particle, is given by the equation

$$L = \frac{1}{n\pi\sqrt{2}\,\sigma^2},$$

where  $\sigma$  is the radius of the sphere of action in a collision, n the number of systems in unit volume of the gas through which the particle is moving. Putting for  $\sigma$  the value  $2e^2/kmv^2$ , we find for the value of L the free path of a corpuscle

$$L = \frac{k^2 m^2 v^4}{4e^4 n\pi \sqrt{2}}.$$

Let us suppose that the gas through which the corpuscle is moving is hydrogen at atmospheric pressure, and assume further that the mass of the primordial atom is the same as that of a corpuscle, then  $nm = 8.5 \times 10^{-5}$  and we get

$$L = \frac{k^2 m^3 v^4}{4e^4 \pi \sqrt{2}} \, 8.5 \times 10^{-5} \,;$$

since e is measured in electrostatic units  $m/e = \frac{1}{3}10^{-17}$ ,  $e = 3.4 \times 10^{-10}$ , substituting these values we get

$$L = \frac{k^2 \, 10^{-40}}{1.4} \, v^4;$$

for a velocity equal to that of some of the corpuscles in the radium rays, i.e.  $2 \times 10^{10}$ , L is equal to  $7k^2$  centimetres.

The influence of the velocity of a corpuscle on the effects of a collision is considered more fully on p. 344.

# Emanation from Radium and induced Radio-activity produced by it.

164. M. and Mme Curie\* have shown that the walls of a vessel containing radium become radio-active. Radium, like thorium, gives out an emanation which is also radio-active. The persistence of the radio-activity of the emanation from radium is, however, very much greater than that from thorium: the latter, as we have seen, falls to half its value in about one minute, while the activity of the radium emanation lasts for several

<sup>\*</sup> Curie, Rapports présentés au Congrès International de Physique, iii. p. 108, 1900.

hours; this has been shown by Dorn\* and Rutherford †. The latter filled a cylinder with the emanation and observed the saturation current from time to time; after the lapse of 3.5 hours the current was 1:31 times its initial value, after 20 hours the current had sunk to its initial value. On blowing out the air from the cylinder and refilling with air free from the emanation the current fell to half its value, showing that half the current was due to the emanation and half to the induced radio-activity on the walls of the vessel. Thus, in this experiment, it took 20 hours for the activity of the emanation to fall to one-half of its original value, a great contrast to the 1 minute required for the same fall in the thorium emanation. On the other hand the radio-activity induced on neighbouring bodies by the radium emanation dies away more rapidly than that due to the thorium emanation. The induced radio-activity due to radium, like that due to thorium, concentrates on negatively electrified bodies.

Rutherford † has shown that heating has an enormous effect on the issue of the emanation from radium. The radium to be heated was placed in a platinum tube, and a constant current of air passed over the radium and through a testing vat in which the saturation current was measured: this current was due to the ionisation of the air in the vat by the radiation from the emanation, and also by the radiation from the walls of the vessel which became radio-active. On heating the tube containing the radium with a small gas flame, the saturation current in the vat was increased 300 times; blowing the emanation from the vat reduced the current to 1/20 of its value when the emanation was present, showing that 19/20 of the ionisation was due to the emanation, the remaining 1/20 being due to induced radioactivity on the walls of the vat. The experiment was repeated with a larger gas flame, when the current in the vat increased to 650 times the value when the radium was cold; with a still larger flame the current increased to 1800 times its value, and when the platinum tube was red-hot it increased to 5000 times the value when cold. Heating the tube to a white heat produced no further increase in the current. Blowing out the emanation from the vat when the current was greatest reduced the current

<sup>\*</sup> Dorn, Abh. d. naturf. Ges. Halle, 1900.

<sup>+</sup> Rutherford, Physikalische Zeitschr. ii. p. 429, 1901.

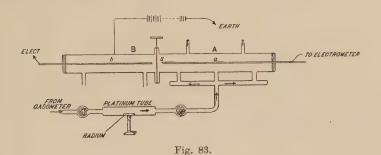
to one-fourth, showing that three-fourths of the ionisation was due to the emanation and one-fourth to the induced radio-activity. The radium was then allowed to cool; on heating it to a red heat the next day the current was only increased 65 times, and this increase was maintained on subsequent coolings and heatings. This experiment suggests that the radium contains a radio-active gas which can be driven out by heating, and which ordinarily supplies a part of the emanation. M. and Mme Curie (l.c.) obtained from radium a radio-active gas, producing phosphorescence on the walls of the glass vessel in which it was contained; the radiation from this gas was sufficiently powerful to penetrate the walls of the tube and ionise the gas in the neighbourhood. No new lines were found when the spectrum of the gas was examined.

165. Molecular Weight of the Emanation from Radium. We can form some estimate as to the molecular weight of the radium emanation from the determination made by Rutherford and Miss Brooks\* of its coefficient of diffusion through air. The measurements which have been made of the coefficients of inter-diffusion of a large number of simple gases have shown that the coefficient of diffusion of one gas into another is approximately inversely proportional to the square root of the product of their molecular weights: if then we know the rate of diffusion of the radium emanation through air we can, by the aid of the preceding rule, determine its molecular weight.

The method used by Rutherford and Miss Brooks to determine the coefficient of diffusion through air was as follows. A long brass cylinder AB, Fig. 83, was divided into two equal parts by a smooth metal slide S, the ends of the cylinder were closed by ebonite stoppers, which supported the brass tubes a and b: the cylinder was insulated and connected with one pole of a battery of 300 volts, the other pole of the battery was earthed: the rods a and b were connected with a sensitive electrometer. The cylinder was packed round with felt, so as to keep the temperature as constant as possible. To get sufficient emanation into the cylinder the radium was slightly heated, and the emanation was carried by a slow current of air into the cylinder.

<sup>\*</sup> Rutherford and Brooks, Trans. Roy. Soc. Canada, vii. p. 21, 1901.

When a sufficient quantity of the emanation had been obtained the current was stopped, and the apparatus left to stand for several hours: the slide S was then opened and the current began to diffuse from a to b. The electrical currents through a and b were measured at regular intervals. Initially there is no current in B, but after opening the slide the current in B begins



to increase and that in A to decrease: measurements were made of the currents at regular intervals, these currents (when corrected for the part due to the induced radio-activity on the electrodes and walls of the vessel) give the amount of emanation present in the two cylinders. From the ratio of the amounts of the emanation in the two cylinders, the coefficient of diffusion K through air can be calculated from the formula

$$\frac{S_1 - S_2}{S_1 + S_2} = \frac{8}{\pi^2} \left\{ e^{-\frac{\pi^2 K t}{a^2}} + \frac{1}{9} e^{-\frac{4\pi^2 K t}{a^2}} + \ldots \right\};$$

here a is the length of the cylinder, t the duration of the experiment in seconds,  $S_1$  and  $S_2$  the amounts of the emanation in the cylinders A and B respectively at the end of the experiment. The values obtained for K varied between 08 and 15. The authors state that the emanation given off when the radium is first exposed to the air diffuses more rapidly than that given off at a later period. Applying the law that the coefficient of diffusion of one gas into another varies inversely as the square root of product of the molecular weights of the gases, the values of K found for radium would indicate a molecular weight between 40 and 100. This shows that the emanation is not the vapour of radium, as M and M me Curie have shown that the atomic weight of that substance is about 225.

166. Chemical Effects produced by Radium\*. Radium discolours glass with which it is in contact; the discoloration seems analogous to that which is observed in the glass of a discharge tube exhausted to a very high vacuum: it produces in the chlorides of the alkali metals changes in colour like those produced by the impact of cathode rays on these salts, it also gives rise to ozone, a strong smell of which is perceptible on opening a bottle in which strong radium has been kept.

#### Polonium.

- 167. Polonium, discovered by M. and Mme Curie\*, is found in company with the bismuth extracted from pitch-blende: they obtained bismuth richer and richer in polonium by the following methods of fractionation:
- 1. Sublimation of the sulphide in vacuo. The sulphide of polonium is much more volatile than that of bismuth.
- 2. Precipitation of solutions in nitric acid by water. The precipitated nitrate is much more active than that remaining behind in the solution.
- 3. Precipitation by hydrogen sulphide from a solution in hydrochloric acid. The precipitated sulphide is much more active than the salt which remains behind.

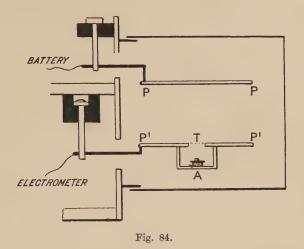
Polonium has not been obtained in a pure enough state to give a spectrum. As far as is known the radiation from it is entirely of the non-deviable kind: polonium does not give out negative corpuscles, and its radiation is very easily absorbed, a thin sheet of aluminium being able to stop it. The radiating power of polonium is not permanent, it continually gets weaker and weaker. Mme Curie†, who measured the absorption by a thin plate of aluminium of the radiation from polonium after it had traversed a certain thickness of air, found the very remarkable result that the further the polonium rays go through air the more easily are they absorbed by aluminium.

The arrangement they used to show this is represented in Fig. 84: PP, P'P' are two metallic plates between which the

<sup>\*</sup> Curie, Comptes Rendus, exxvii. p. 175, 1898.

<sup>†</sup> Ib. cxxx. p. 76, 1900.

current produced by a considerable potential difference is measured in the usual way: the polonium is placed at A and the rays from it go through wire-gauze at T. When the polonium is



covered with a thin layer of aluminium foil the absorption of the rays increases with the distance AT, and if a second layer of aluminium foil is placed over the polonium the absorption produced by the second layer is greater than that produced by the first; this is the opposite to what is observed with the Röntgen rays, but in the Röntgen rays we have a mixture of rays of very varying powers of penetration, and when this is the case the first layer must as we have seen (p. 246) produce greater absorption than the second. The effects observed with polonium (and they also occur as Mme Curie has shown with the non-deflectable rays of radium) are those which would be produced if the polonium rays were homogeneous but became less penetrating after passing through an absorbing medium. We should expect rays which consist of rapidly moving negatively charged particles to become more easily absorbed after passing through an absorbing medium, as the velocity of the particles diminishes in consequence of the absorption, and we have seen that slow particles are more absorbed than fast ones. The rays from polonium however resemble Röntgen rather than cathode rays, as they are not deflected either by electric or magnetic forces. We shall see reasons for thinking that these rays consist of pulses of electric and magnetic force, the thickness of the pulse determining the nature of the rays; thick pulses corresponding to easily absorbed rays, thin ones to penetrating rays. Thus, if the thickness of a pulse increased as the rays passed through an absorbing medium we should get the results observed by Mme Curie. Now, if we suppose that the absorption of the rays is due to the communication of kinetic energy to charged ions struck by the pulse we can see that such a thickening of the pulse would take place, as some of the tubes of force in the pulse would be temporarily attached to the ion; thus the ion would tend to hold them back after the pulse passed on; the tubes would ultimately break away from the ion, but the result of the temporary detention would be a separation of the tubes and a broadening of the pulse. If this effect is produced in air it will evidently have the effect of making the intensity of the rays die away very rapidly as they get weaker and thus make the appearance of measurable effect more abrupt than it is in cases where the ordinary law of absorption holds: as an illustration of this point Mme Curie found that a very slight change in the distance AT (Fig. 84) was sufficient to make the current between the plates increase from a value too small to be measurable to one of very considerable magnitude.

#### Actinium.

168. Actinium, which is the name given to a very radio-active substance which accompanies the thorium extracted from pitchblende, was discovered by Debierne\*; it occurs in such minute quantities that its investigation presents great difficulties. It seems to possess to a very high degree the power of producing induced radio-activity, in this it resembles Th X (see p. 291) and it seems not improbable that it may turn out to be this substance.

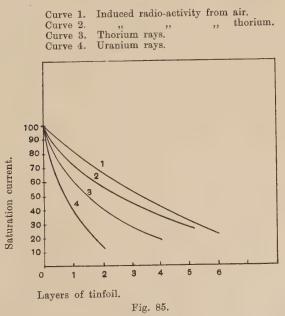
Induced Radio-activity on Negatively Electrified Bodies in Air.

169. Elster and Geitel† have found that a strongly negatively electrified body suspended in the open air or in a large room becomes temporarily radio-active. They showed that if a body was connected with the negative terminal of a Wimshurst machine for

<sup>\*</sup> Debierne, Comptes Rendus, 129, p. 593, 1899; 130, p. 906, 1900.

<sup>†</sup> Elster and Geitel, Physikalische Zeitschr. iii. p. 76, 1901.

some hours, on detaching the body from the machine it was found to be radio-active, ionising the air in its neighbourhood and affecting a photographic plate. It is necessary for the success of this experiment that a very large volume of air should be exposed to the electric field, thus the wire must be in the open air or in a large room. I was not able to get any induced radio-activity with the air in the normal state when the wire was placed in a closed vessel of about 500 litres capacity. The material of which the negatively electrified body is made does not seem to have much effect upon the amount of induced radio-activity, paper giving as large an effect as metal. A piece of metal made radioactive in this way can be heated to redness without losing its activity; if the surface of the radio-active metal is dissolved in acid the acid becomes radio-active; this is most conveniently proved by evaporating the acid to dryness and testing the residue. The radio-activity produced in this way gradually dies away. Rutherford and Allen\*, who have measured the rate at which it decays,



found that the induced radio-activity falls to about half its value in three-quarters of an hour; the induced radio-activity due to

<sup>\*</sup> Rutherford and Allen, Physikalische Zeitschr. iii. p. 225, 1902.

thorium emanation is as we have seen much more persistent than this. Rutherford has also compared the penetrating power of the radiation from the negatively electrified wire in air with that of the rays from substances made active by the thorium emanation and with the non-deviable rays from thorium and uranium; the results which represent the proportion which pass through 1, 2, 3, 4 layers of tinfoil each  $3.4 \times 10^{-4}$  cm. thick are represented in Fig. 85; it will be seen that of the radiations tested that induced in air is the most penetrating. Elster and Geitel ascribe the induced radio-activity to the deposition on the wire of some unknown radio-active substance which is diffused through the atmosphere.

IONISATION DUE TO PHOSPHORUS; IN NEWLY PREPARED GASES AND IN AIR WHICH HAS BEEN IN CONTACT WITH WATER.

## Ionisation due to Phosphorus.

170. Air which has passed over phosphorus at not too low a temperature has the power of discharging both positively and negatively electrified bodies. This was known by Matteucci\*, it was also studied by Naccari†, and was subsequently independently discovered by Shelford Bidwell‡. Barus§, who has made a very extensive series of observations on this phenomenon, found that air which had been treated in this way was very active as a cloud producer. If hydrogen is passed over phosphorus it does not become a conductor of electricity.

There are two points of view from which we may regard the action of the phosphorus: the first is that the air in passing over the phosphorus gets ionised, and after its escape from the phosphorus consists of a mixture of positive and negative ions uniformly distributed through the gas; in fact, that the gas is in much the same condition as if it had been drawn past an incandescent metal whose temperature was high enough to produce both positive and negative ions at its surface. The other view is that the air passing over the phosphorus carries off phosphorus

<sup>\*</sup> Matteucci, Encyclopædia Britannica (1855 edition), viii. p. 622.

<sup>+</sup> Naccari, Atti della Scienze de Torino, xxv. p. 252, 1890.

<sup>‡</sup> Bidwell, Nature, xlix. p. 212, 1893.

<sup>§</sup> Barus, Experiments with Ionised Air, Washington, 1901.

dust or nuclei, and that each of these nuclei acts as a centre of ionisation, ionising the gas in its immediate neighbourhood; the state of the gas on this view would be similar to that of a gas containing a large number of incandescent metallic particles, each of these particles being surrounded by an envelope of conducting gas. On this view, when the conducting gas was placed in an electric field, the conduction would be due to the motion of ions dragged out of the gas in contact with the nuclei by the electric force, while the nuclei themselves would not be displaced. The evidence is hardly sufficient to enable us to decide with certainty between these two views: the second one, however, seems to me the more probable, for Barus found that the rate at which the conductivity died away from the phosphorised air was not increased by the application of a strong electric field. The decrease in conductivity seems consistent with the view that it arises from the diffusion of the nuclei to the sides of the vessel, a nucleus ceasing to be active as soon as it becomes attached to the walls of the vessel. The rate of decay of conductivity would thus be proportional to the number of nuclei striking the walls of the vessel in one second; in the case of a gas of density  $\rho$ , and whose average velocity of translation is v, this number is per unit area of surface equal to  $\frac{1}{6}\rho v$ ; from measurements of the rate at which the phosphorised gas lost its conductivity Barus concluded that the nuclei moved about like the molecules of a gas, only very much more slowly, the average velocity of the nuclei being only about 3 cm. per second. Another reason for supposing that the phosphorus supplies the gas which has passed over it with nuclei capable of producing ions rather than with ready-made ions, is the very considerable analogy that exists between the behaviour of the phosphorised air and that of air which has passed through water; the properties of the latter we shall consider in the next paragraph.

Barus made experiments to see if the ionising properties of the phosphorised air could be exerted through thin films of various materials: the only films which he found to transmit any appreciable effect were those made of thin tissue-paper, and here the effect seemed to make its way through the pores rather than through the material itself, as on oiling the paper so as to stop up the pores the transmission ceased. Conductivity produced by bubbling air through water.

171. As we have seen (Chap. I.) air when in its normal state conducts electricity to a certain extent, the saturation current through the air in a small closed vessel being proportional to the mass of the air contained in the vessel, the saturation current per unit mass of air showing but little variation in samples of air taken from different places. I have found, however, that air which has passed through tap water acquires and retains for some time very much greater conductivity than normal air. One way in which this was proved was to use as the vat containing the air a cylindrical gasometer about 103 cm. high and 75 cm. in diameter, down the axis of which was a conducting wire; the conductivity of the air was tested by measuring the saturation current between this wire and the walls of the vat. If now the air in this vat was made to bubble through water the conductivity increased to a very large extent. One way of forcing the air through water was to pump the air from the vat by means of a water pump into a second vessel (the process of pumping of course making the air bubble vigorously through the water), and then force the air back from this vessel into the vat; when this circulation had been kept up for about an hour it was found on stopping the circulation that the conductivity of the air was very much greater than it was before. I often found, for example, that it had increased 30 or 40 times, and I have no reason for supposing that this increase was any approach to a limit. Another convenient way of putting a gas into this conducting condition is by passing it through a Gouy sprayer. When once a gas has got into this condition it remains in it for a very considerable time; thus, for example, I found that after the lapse of several days after the passage of the gas through water, the conductivity was still many times its value before the bubbling through the water had occurred.

This conducting gas can be transferred from one vessel to another, it can pass through plugs of glass-wool without losing its conductivity, nor does it lose this property when passed over wire-gauze heated to a red heat or through white-hot platinum tubes or over hot copper.

The conductivity of the gas is due to the continued pro-

duction of ions around some nuclei introduced into the gas by its passage through the water; it cannot be explained by the simple ionisation of the gas by this process, i.e. by a production of ions while the air is bubbling through the water, this production ceasing as soon as the air leaves the water, for if this were the cause of the conductivity the current through the gas would continue to increase as the electromotive force was increased: there would in this case be no 'saturation' of the current. If no fresh ions were being produced the increase of electric force would at first produce a continual increase in the current, but as the old ions got used up by the current, and no fresh ones being by hypothesis produced, the current would gradually decrease. The relation between the current and the potential difference is not of this character, but, as the following numbers show, exhibits all the characteristics of conduction through a medium in which ions are being generated at an approximately constant rate; the numbers in the following table are proportional to the current passing between a wire placed along the axis of the cylindrical gasometer in which the gas was contained and the walls of the gasometer, when differences of potential, indicated by the numbers in the first column of the table, were maintained between the wire and the walls of the vessel. It will be noticed that for equal differences of potential, the current is greater when the wire is the positive electrode than when it is the negative.

Potential difference between the wire and sides of the	Current		
vessel in volts	wire +	wire -	
1000 800 600 400 200 160 120 80 40	250 220 205 150 125 105 80 67 40	150 140 140 128 97 80 70 45 30	

The difference can be explained by supposing that the negative ions produced round the nuclei can be more easily detached by

the electric field from its neighbourhood than the positive ions; this is what we should expect from the greater mobility of the negative ions, part of the positive ions may get attached to the nuclei and as these are almost immovable the positive ions engaged in this way could not take any part in carrying the current.

The behaviour of the gas when it contains the nuclei introduced into it by bubbling through water is very analogous to that of a gas containing the emanation from thorium; the ionising power of the nuclei introduced by the water is however much more persistent than that of the emanation; on the other hand the radiation from the nuclei is very much less penetrating than that from the emanation: for gas which had been bubbled through water was passed for 6 hours over a photographic plate without producing any effect upon it. No increase in conductivity was found by bubbling air through alcohol, ether, or turpentine. The increase in conductivity produced in air by the nuclei introduced into it by contact with water may explain the interesting result found by Elster and Geitel\*, that the air in closed caves in which there is no circulation has a much higher conductivity than the air in open spaces, for these nuclei might slowly diffuse from the walls of the cave and so increase the ionisation in the air. If the explanation given below of the action of the nuclei is correct, then the increase in conductivity might be produced by nuclei of many substances besides water; all that is required on this explanation is that there should be chemical action between the air and the substance forming the nuclei.

Effects produced on a negatively electrified wire immersed in the conducting gas.

172. We have seen (p. 294) that a negatively electrified wire in a gas containing the emanation from thorium acquires the power of ionising the air in its neighbourhood and retains this power for a considerable time. Elster and Geitel have shown that the same property is acquired by a negatively electrified rod exposed to the open air, or to the air in a large cave or cellar, the effect in the latter case being considerably greater than in the open air. I have found that effects of a similar character are produced by

<sup>\*</sup> Elster and Geitel, Physikalische Zeitschrift, iii. p. 76, 1901.

negatively electrifying a wire in air whose conductivity has been increased by bubbling it through water. I first tested the effect of negatively electrifying the central wire in the cylindrical gasometer when the gas in it was in the normal state; the wire was connected to the negative pole of a Wimshurst machine, the other terminal of which was put to earth and maintained at a potential of about 30000 volts for 6 hours, the outside of the gasometer was kept connected with the earth; in this case no change could be detected in the wire, the saturation current in the gasometer was the same after the electrification of the wire as it had been before, while if the wire had ionised the air around it the saturation current would have been increased; the volume of air in the vessel, about  $5 \times 10^5$  c.c., is thus too small to give the effect observed by Elster and Geitel in the open air and in large rooms. I next tried the effect of largely increasing the current passing through the gas during the negative electrification of the wire; this was done by exposing the air in the gasometer to Röntgen rays during the whole of the time the wire was kept connected with the Wimshurst machine; the rays make the conductivity of the gas very much greater than when it is in the normal state, and so largely increase the number of positive ions which come up to the negatively electrified wire. In this case after disconnecting the wire from the Wimshurst machine and stopping the rays the saturation current was found to have slightly increased, the increase being from 15 to 20 per cent.; that this was due to a change in the property of the wire and not of the gas in the vessel was shown by replacing the wire by one which had not been electrified, when the saturation current was found to have its normal value. The ionisation due to the negatively electrified wire (shown by the increase in the saturation current) gradually died away and was not perceptible after about 45 minutes. The experiment was repeated with the wire connected with the positive instead of the negative terminal of the Wimshurst machine, but in this case not the slightest increase in the saturation current could be detected. When the air was made a conductor by bubbling it through tap water very much larger effects were obtained. To measure these effects a second vessel was used in which the air was kept in its normal state, the wire to be electrified was placed in this vessel and the saturation current through the vessel measured, (1) before the wire had been electrified, (2) after the wire had

been placed in the gasometer containing the conducting air and negatively electrified: in most cases the wire itself was used as one of the electrodes in the second vessel. When the air in the gasometer had been got into a highly conducting state by bubbling through water, the wire to be tested was placed in it and negatively electrified by connecting it with the negative terminal of a Wimshurst machine; it was found that even with no more than half-an-hour's electrification the wire acquired strong ionising power. Thus, to give an example, the saturation current in the second vessel before the wire was electrified (the wire being used as one of the electrodes) was 15, after 30 minutes' negative electrification in the gasometer the saturation current rose to 75, a five-fold increase. If the wire was positively electrified when in the gasometer the saturation current through the second vessel was increased but to a very much smaller extent than if it had been negatively electrified; no increase was produced if the wire was not electrified. The ionising power given to the wire by its negative electrification gradually dies away after the electrification has ceased; the rate of decay varied somewhat in different cases, it generally took about 40 minutes for the ionisation to fall to one-half its initial value. Though it is convenient to use the electrified wire as the electrode in the second vessel, it is not necessary to do this, an increase in the saturation current is produced when the wire is merely placed in the second vessel and another wire used as the electrode. The ionising power does not seem to depend much upon the material of which the negatively electrified body is made; the following experiment illustrates this. Four wires, one copper, one zinc, one copper covered with sodium amalgam and the other copper covered with a layer of glycerine and water, were metallically connected together and placed in symmetrical positions in the gasometer and negatively electrified, these wires were then used separately as electrodes in the second vessel when they all gave approximately equal currents, much larger than the normal one.

173. When the wire has by negative electrification once been put in the state in which it ionises the surrounding gas it remains in this state in spite of very rough treatment. Thus it can be washed with water and then dried with filter-paper without losing this property; it can be heated to a bright red heat without much

detriment to its ionising power; an amalgamated wire was heated until the mercury was driven off and still retained its activity. If, however, the active wire is rubbed with emery-paper so as to remove the outside layers, or if in the case of a wire covered with a layer of water the water is wiped off, then the activity of the wire is destroyed. The ionising power of the wire corresponds to a very easily absorbed type of radiation, about half the radiation being absorbed by a layer of air at atmospheric pressure about 2 cm. thick, its effects can be detected through thin layers of aluminium foil.

The properties of the wire after having been negatively electrified in the conducting gas are very analogous to those possessed by a wire after negative electrification in the open air or in air containing an emanation; the radio-activity in these cases has usually been ascribed to some radio-active substance adhering to the wire. There are indications that when air bubbles through water it carries away with it a radio-active gas which can also be extracted by boiling the water. For I have found that the conductivity acquired by the air varies considerably with different samples of water. The conductivity produced by Cambridge tap water is very large, although the deposit obtained when the water is evaporated to dryness is not appreciably radio-active; with rainwater the increase in conductivity is very small, it is increased when certain salts such as lead nitrate are dissolved in the water. I have found a small but appreciable increase in conductivity from the water produced by the combustion of coal gas.

The conductivity is retained by the air after it has passed through a porous plug. As the radio-active constituent can diffuse through a porous plug it is possible by measuring the rate of diffusion to determine the density of the emanation. By comparing the rates at which the emanation and carbonic acid gas diffused through the same plate I found that the density of the emanation was between 5 and 6 times that of carbonic acid.

The following considerations indicate that certain changes in the physical conditions might make a body radio-active independently of the deposition of an intrinsically radio-active substance. We have, when considering the phenomena of electrification by incandescent metals and of photo-electricity, regarded a metal

when in its normal state as being full of negatively electrified corpuscles: at ordinary temperatures these corpuscles have not sufficient kinetic energy to enable them to overcome the attraction of the metal and shoot out from the metal into the surrounding gas; when, however, the kinetic energy of the corpuscles is sufficiently increased, either by raising the temperature of the metal or by the action of ultra-violet light, they escape into the gas and produce electrical effects. Now in the case of a negatively electrified wire placed in a conducting gas a state of things will be set up at the surface of the metal which will assist the corpuscles to escape into the gas. For in consequence of the negative electrification of the wire positive ions travel up to it: let us suppose that some at least of these do not get discharged but stick to the wire, forming a layer of positive electrification close to the surface of the metal, the positive electrification will induce negative on the metal so that there will be at the surface of the wire two oppositely electrified layers close together, the negative layer on the wire, the positive layer outside; there will thus be a very intense electric field, tending to pull the negative electricity out of the wire and thus making the metal into a cathode emitting cathode rays; if these corpuscles are moving with sufficient rapidity to ionise the gas through which they pass the gas around the metal will be surrounded by positive and negative ions and will thus be able to discharge both positive and negative electricity from the wire; if the corpuscles come out, but with so little kinetic energy that they are not able to ionise the molecules of the gas against which they strike, then we should expect the wire to discharge negative electricity more easily than positive, for the positive electricity in this case would have to be carried by the positive ions in the outer coating of the double layer and the experiments we have described show that this is only detached with great difficulty.

174. The measurements made by H. A. Wilson (see p. 190) show that to ionise a molecule requires the expenditure of an amount of energy equal to the work required to move the charge on an ion through about 2 volts, hence we see that to give to the corpuscles from the ions sufficient energy to ionise the gas through which they pass, there must be a difference of potential between the positive and the negative layers of at least 2 volts.

If the potential difference between these layers exceeds this value the corpuscles dragged out of the metal may ionise the gas; the corpuscles in the cathode rays in a vacuum tube acquire a velocity equivalent to that due to a fall through several hundred volts; hence their velocity will greatly exceed that of the corpuscles extracted from the metal by the double layer, the latter correspond to very slow and easily absorbed cathode rays. If these views are correct it is not necessary to suppose that all cases of induced radio-activity are due to the deposit of a radio-active substance; the formation of a suitable double layer of electrification at the surface of any substance would impart this property to that substance.

175. The existence of a double layer of electrification has long been recognised in certain cases, it is by means of such a layer that the polarisation of the electrodes immersed in an electrolyte is usually explained; it seemed therefore of interest to try whether such electrodes possessed any properties analogous to those possessed by a wire which has been negatively electrified in a conducting gas. Two platinum wires were immersed in dilute sulphuric acid, and a current of about 1 ampère was sent through the acid; these wires were used as electrodes for about half-an-hour and then taken out, dried with filter-paper, and then tested to see whether any ionisation was produced by them in the air around them; in many cases considerable ionisation was found in the air round the wire which had been used as the negative terminal (the one at which the hydrogen ions arrive), but in no case was any such effect observed near the wire which had been used as the positive terminal. amount of ionisation round the wire used as the negative terminal varied a good deal, even when the intensity and the duration of the current between the electrodes was kept the same, in some few cases it seemed to be absent altogether; when present the ionising power died away more rapidly than for a wire which had been negatively electrified in the air, and was destroyed by processes which hardly affected the wire.

Electrification produced by the bubbling of air through water, the splashing of drops, the liberation of gases by chemical action or by electrolysis.

176. The preceding experiments relate to the conductivity of the gas, and show that the process of bubbling through water produces both positive and negative ions in the gas; the electrification in the gas, i.e. the excess of the number of positive over that of the negative ions, had previously been the subject of many investigations. Thus Lord Kelvin\* showed that air bubbled through water carried with it a negative charge, the amount of this charge depending upon the purity of the water, the addition of salts or acids to the water diminishing the effect, and in some cases reversing the sign of the electrification. The closely connected effect connected with the splashing of drops had previously been investigated by Lenard+, whose attention was called to the question by the well-known fact that there is something exceptional in the phenomena of atmospheric electricity at the foot of a waterfall when the water falls upon the rocks and breaks into spray. Lenard found that when a drop of water splashes against a plate, a positive charge goes to the water, while the surrounding air is negatively electrified. The amount of the electrification is influenced to a remarkable extent by the purity of the water; thus Lenard found that while the effect was very marked with the exceptionally pure water at Heidelberg, it was almost insensible with the less pure water at Bonn. He found too that the splashing of a weak solution of sodium chloride produced positive instead of negative electrification in the air; thus while the splashing of rain electrifies the air negatively, the breaking of waves on the sea-shore will electrify it positively.

In some experiments that I made on the subject<sup>+</sup>, I found that the effects produced by exceedingly minute traces of some substances were exceedingly large; thus, although rosaniline is a very powerful colouring agent, I found that its presence in

<sup>\*</sup> Lord Kelvin, Proc. Roy. Soc. lvii. p. 335, 1894.

<sup>†</sup> Lenard, Wied. Ann. xlvi. p. 584, 1892.

<sup>‡</sup> J. J. Thomson, Phil. Mag. v. 37, p. 341, 1894.

water could be detected by the electrical effect before any change in the colour was apparent.

Kosters\* found that while air bubbled through pure water was negatively electrified, the addition of '007 per cent. of sulphuric acid to the water made the air coming through electrically neutral, while the addition of more acid caused the air to be positively electrified, although the amount of this was small compared with the negative electrification due to pure water.

The effect produced by the addition of salts and acids to the water on the electrification of air passing through, has also been investigated by Lord Kelvin, Maclean, and Galt†.

The increased conductivity of air, produced by its passage through water, is not nearly so sensitive to impurities in the water as the charge carried away by the air. Thus I could find no appreciable difference in the conductivity when salt, rosaniline or methyl violet was added to the water, although the amount and even the sign of the charges carried away by air passing through the solution are very different. Very different considerations are involved in the case of the conductivity given to air by the water, and the amount of charge given to it by splashing and bubbling. The former corresponds to a steady state which continues for hours and even days after the passage of the air through the water: the latter is no doubt largely influenced by what occurs at the instant when a fresh liquid surface, due either to the bubbles forcing their way through the liquid or by the large increase in area produced by the splashing of a drop, is exposed to the gas.

Lenard<sup>†</sup> found that electrification was produced by many liquids besides water and aqueous solutions; thus, mercury produced a very large effect of the same sign as water; if mercury is vigorously shaken up in a bottle, and the air drawn off, it is found to be strongly charged with negative electricity; turpentine, too, gives a large effect of the opposite sign to that of water, the air being positively, the turpentine negatively, electrified. The splashing of carbon bisulphide also gives rise to considerable

<sup>\*</sup> Kosters, Wied. Ann. lxix. p. 12, 1899.

<sup>†</sup> Lord Kelvin, Maclean, and Galt, Phil. Trans. A. 1898.

<sup>#</sup> Lenard, Wied. Ann. xlvi. p. 584, 1892.

electrification, the sign of the electrification being the same as for water.

The nature of the gas surrounding the liquid has also a very considerable effect upon the electrification; thus Lenard found that the electrification due to the splashing of water surrounded by hydrogen was much less than when the water was surrounded by air; using very carefully purified hydrogen, I got only a very small electrification, and that of the opposite sign to the effect in air.

## Electrification due to Chemical Action.

In many cases of chemical combination in which gases take part we get electrification of the gas; Pouillet\* was the first to discover an example of this effect; he found that while a carbon cylinder is burning, the air round the cylinder is positively while the cylinder itself is negatively electrified. Lavoisier and Laplace+ showed that the same effect occurs with glowing coal. Pouillet+ also found that when a jet of hydrogen burns in air, there is positive electrification in the surrounding air, negative electrification in the hydrogen. Lavoisier and Laplace§ found that when hydrogen is rapidly liberated by the action of sulphuric acid on iron there is considerable positive electrification in the gas; in this case the interpretation of the results is made difficult by the electrical effects produced by the bubbling of the gas through the liquid, these we should expect to be very considerable as the gas is liberated in small bubbles, which is the most favourable case for getting a considerable electrification in a given volume of air. This and other cases of electrification by chemical action have been investigated by Enright | and by Townsend¶; the latter showed that the hydrogen produced by the action of sulphuric acid on iron retained its electrification after passing through tubes filled with tightly packed glass-wool, thus proving that the electrification could not be carried by the coarse spray produced by the bursting of the bubbles, as this is

- \* Pouillet, Pogg. Ann. ii. p. 422.
- † Lavoisier and Laplace, Phil. Trans. 1782.
- ‡ Pouillet, Pogg. Ann. ii. p. 426.
- § Lavoisier and Laplace, Mémoires de l'Académie des Sciences, 1782.
- || Enright, Phil. Mag. v. 29, p. 56, 1890.
- ¶ Townsend, Proc. Camb. Phil. Soc. ix. p. 345, 1898; Phil. Mag. v. 45, p. 125, 1898.

stopped by the wool. Townsend also showed that when chlorine is liberated by the action of hydrochloric acid on manganese dioxide the chlorine has a strong positive electrification; and that the oxygen produced by heating potassium permanganate carries with it a strong positive charge.

Townsend has shown that gases liberated by electrolysis carry with them considerable charges of electricity. Thus the hydrogen evolved by the electrolysis of sulphuric acid at temperatures as high as 40° or 50°C. has a considerable positive charge; the charge on the oxygen is exceedingly small in comparison, it is also positive. When these gases are liberated by the electrolysis of a solution of caustic potash the electrification on the hydrogen is very small, while the oxygen has a much larger negative charge the amount of which rapidly increases with the temperature; the nature of the electrode too has a considerable influence on the amount of electrification which comes off in the gas. The interpretation of these results, like those of the evolution of gases by the action of acids on metals, is made difficult by the electrical effects produced by the bubbling of the gases through the liquid. Kosters\*, who has also investigated this subject, ascribes most of the electrification to the bubbling.

Townsend+ found that these electrified gases possess the remarkable property of producing a cloud when they pass into a vessel containing aqueous vapour; this cloud is produced even when the air in the vessel is far from saturated with moisture, and does not require any lowering of temperature such as would be produced by the expansion of the air in the vessel. Townsend found that when the gas liberated by electrolysis was not charged no cloud was produced, and that the weight of cloud produced, other circumstances being the same, was proportional to the charge in the gas. Clouds are produced, however, in some cases in which no charges are perceptible; thus H. A. Wilson‡ has shown that if solutions of salts or acids, or even of sugar or glycerine, are sprayed by a Gouy sprayer into a vessel and the air from this vessel passed through sulphuric acid a cloud is formed when this air emerges into a damp atmosphere. The cause of this seems fairly clear,

<sup>\*</sup> Kosters, Wied. Ann. lxix. p. 12, 1899.

<sup>†</sup> Townsend, Proc. Camb. Phil. Soc. ix. p. 345, 1897.

<sup>‡</sup> H. A. Wilson, Phil. Mag. v. 45, p. 454, 1898.

although the passage through the sulphuric acid robs the drops of the solution of the water, the acid or salt in the drop is carried along with the air through the sulphuric acid; when this emerges into the moist atmosphere the water condenses round the salt or acid and forms a drop of the solution, thus the drops in the cloud are not pure water, but solutions, and as the vapour pressure for these solutions is smaller than that for pure water the drops do not evaporate, even although the atmosphere is not saturated with moisture. Meissner\* has also described clouds not accompanied by electrification which are produced when air containing ozone is passed through a solution of potassium iodide: these can be explained in a similar way by supposing that the ozone acting on the potassium iodide produces some substance which readily dissolves in water when it comes into contact with it. I think that a similar explanation may hold for the clouds produced by the electrified gas, for the carriers of the electricity are evidently complex bodies of very considerable size, since Townsend+ found that the velocity of these carriers under a potential gradient of 1 volt per cm. was only about 1/8000 of the velocity under the same electric field of the ions produced by the action of the Röntgen rays on the gases: if we suppose that these systems can dissolve in water like an acid or salt and lower the vapour pressure, the process by which the cloud is formed would be the same as that in H. A. Wilson's experiment.

Townsend measured the rate of fall, the weight of the cloud, and the amount of electrification carried by it; the first of these measurements gives the size of a drop, the second the number of drops, and the third the charge on a drop; he found, assuming each drop to be charged, that the magnitude of the charge on the carrier of the electricity in electrolytic oxygen was about  $5.1 \times 10^{-10}$  electrostatic units.

Ionisation produced by the motion of negatively electrified corpuscles.

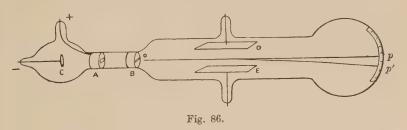
177. The motion of negatively electrified corpuscles plays an exceedingly important part in the electrical properties of gases;

<sup>\*</sup> Meissner, Jahresber. f. Chem. 1863, p. 126; see also Townsend, Proc. Camb. Phil. Soc. x. p. 52, 1899.

<sup>†</sup> Ib. ix. p. 345, 1897.

we have already seen that it is of fundamental importance in the phenomena connected with incandescent solids and with photoelectric effects, and we shall find subsequently that it is of equal importance in the phenomena connected with sparks and discharges through vacuum tubes where the conductivity of the gas is produced by the electric field itself: it is therefore desirable to consider the laws of ionisation by moving corpuscles independently of the method of production of the corpuscles.

The fact that gas traversed by Lenard rays can discharge electrified bodies whether the electrification is positive or negative shows that the rapidly moving corpuscles constituting those rays ionise a gas when they pass through it. The ionisation of a gas due to the passage through it of cathode rays inside a vacuum tube was shown by the author\* using the arrangement represented in Fig. 86. A pencil of cathode rays from the cathode C passed



through holes in two metal plugs connected with the earth and then between two parallel metal plates D,E; one of these plates was connected with one pole of a battery, the other pole of which was put to earth, and the other plate to one pair of quadrants of an electrometer, the other pair of quadrants being to earth; the plates were so arranged that the pencil of cathode rays did not strike against either of them. When the cathode rays were not passing between the plates there was no appreciable current of electricity between the plates, but when the rays passed between the plates the current if the pressure of gas was not too low was very appreciable. The relation between the current and the potential difference between the plates was of the character typical of an ionised gas; the current very soon reached a maximum value, beyond which it did not increase for a considerable range of poten-

tial difference; when the pressure was very low the current between the plates got very small, as now there were very few molecules for the cathode rays to strike against and ionise. This and the case of the Lenard rays show that rapidly moving corpuscles ionise the gas through which they pass. Since it requires a definite amount of energy to ionise a molecule of a gas it is evident that ionisation will not occur unless the corpuscles possess more than a certain amount of energy, i.e. are moving above a certain speed: if we assume that the work required to ionise a gas is that required to move the charge on an ion through a potential difference of 2 volts the minimum velocity which must be possessed by a corpuscle before it can ionise the molecules of a gas by colliding against them is about 6.3 × 10<sup>7</sup> cm./sec. If any corpuscles are present in a gas acted upon by an electric field the corpuscles will move under the electric force, and if under this force they acquire a velocity greater than the minimum velocity required to ionise the gas these corpuscles will produce fresh ions, and these again will generate other ions, so the gas will rapidly become a conductor. The velocity acquired by a corpuscle in an electric field will depend not only upon the intensity of the electric field but also upon the free path of the corpuscle; after a collision the direction of motion of the corpuscle will be changed, it may be that it is reversed, in which case the action of the electric field after the collision will be to destroy the velocity communicated to the particle by the field before the collision took place: these considerations show that the maximum kinetic energy communicated to the corpuscles will be the work done on the corpuscle by the electric field when the corpuscle moves over a space comparable with its mean free path. Thus the kinetic energy communicated to a corpuscle by a given electric field when the free path is long. i.e. when the pressure of the gas is low, will be greater than when the free path is short, i.e., when the pressure of the gas is high; thus it is much easier to make a gas a conductor by this means when the pressure is low than when it is high: these considerations were first given by the writer in a paper read before the Cambridge Philosophical Society, Jan., 1900.

178. The mathematical development of this conception has already been given on page 231; it is shown there that in the case when the ions are all moving parallel to the axis of x, under

an electric force X, and when the only source of ionisation in the gas is the negative corpuscles,

$$\frac{d}{dx}(nu) = \frac{nu}{\lambda} \left\{ f(Xe\lambda) - \gamma \right\},\,$$

where n is the number of corpuscles, u is the velocity of a corpuscle parallel to the axis of x and the electric force,  $\lambda$  the mean free path of the corpuscle;  $f(Xe\lambda)$  the ratio of the number of cases, in which a collision leads to ionisation, to the whole number of collisions;  $\gamma$  the ratio of the number of cases, in which collision leads to the recombination of the corpuscle, to the whole number of collisions. Since  $(nu/\lambda)f(Xe\lambda)$  is the number of fresh ions produced by the corpuscles in unit time, and as they move in this time through u cm.,  $f(Xe\lambda)/\lambda$  is the number of ions produced by a corpuscle in moving over 1 cm.: denoting this quantity by  $\alpha$ , we get

$$\frac{d}{dx}(nu) = nu\left(\alpha - \frac{\gamma}{\lambda}\right),$$

$$nu = Ce^{\left(\alpha - \frac{\gamma}{\lambda}\right)x},$$

òr

where C is the value of nu when x = 0.

If the field is strong enough to make the corpuscles reach the electrodes before they have time to recombine,  $\gamma = 0$ , and we have

 $nu = C\epsilon^{ax}$ ;

nu is the quantity of negative electricity passing in unit time through unit area of a plane at right angles to the axis of X at a distance x from the origin, and can be measured by placing a metal plate at this distance, connecting it with an electrometer, and measuring by means of this instrument the rate at which negative electricity is reaching the plate. A very valuable series of experiments on this effect have been made by Townsend\* and Townsend and Kirby† who have determined the values of  $\alpha$  for gases under different pressures and for electric fields of different intensities. The following are the values of  $\alpha$  found by Townsend for air:

<sup>\*</sup> Townsend, Phil. Mag. vi. 1, p. 198, 1901.

<sup>+</sup> Townsend and Kirby, ib. p. 630.

X volts per cm.	Pressure •17 mm. a	Pressure -38 mm. a	Pressure 1.10 mm.	Pressure 2·1 mm.	Pressure 4·1 mm.
20	•24			_	_
40	·65	•34	_	-	
80	1.35	1:3	.45	·13	_
120	1.8	2.0	1.1	•42	·13
160	2.1	2.8	2.0	.9	•28
200		3.4	2.8	1.6	•5
240	2.45	3.8	4.0	2.35	.99
320	2.7	4.5	5.2	4.0	2.1
400		5.0	6.8	6.0	3.6
480	3.15	5.4	8.0	7.8	5:3
560	_	5.8	9.3	9.4	7:1
640	3.25	6.2	10.6	10.8	8.9

Thus we see that for a given value of X,  $\alpha$  begins by increasing with the pressure, it attains a maximum at a particular pressure, and then diminishes as the pressure increases; we see too that the larger the value of X the higher the pressure at which  $\alpha$  is a maximum. The values given for  $\alpha$  at the two lowest pressures show that, as the force is increased,  $\alpha$  approaches a constant value.

These results follow at once from the value we have obtained for  $\alpha$ , viz.

$$\alpha = \frac{f(Xe\lambda)}{\lambda}$$
.

If X is constant, then at the pressure when  $\alpha$  is a maximum,

$$\frac{d\alpha}{d\lambda} = 0,$$

$$\frac{f'(Xe\lambda) Xe}{\lambda} - \frac{f(Xe\lambda)}{\lambda^2} = 0 \dots (1),$$

$$f'(Xe\lambda) = \frac{d \cdot f(Xe\lambda)}{d \cdot Xe\lambda} :$$

where

or

equation (1) may be written

$$Xe\lambda f'(Xe\lambda) = f(Xe\lambda) \dots (2).$$

This equation determines the value of  $\lambda$  when  $\alpha$  is a maximum; we see from the form of the equation that the solution of (2) is of the form

$$Xe\lambda = c$$

where c is independent of both X and  $\lambda$ ; thus the value of  $\lambda$ , when  $\alpha$  is a maximum, is inversely proportional to X, and since  $\lambda$  is inversely proportional to the pressure, it follows that the pressure at which  $\alpha$  has its maximum value is proportional to X.

When the electric field is so strong that the kinetic energy acquired by the corpuscle between two collisions is great enough to make the corpuscle ionise the molecule whenever it collides with it,  $f(Xe\lambda) = 1$  and  $\alpha = 1/\lambda$ ; hence  $\alpha$  becomes in strong fields equal to the reciprocal of the mean free path, i.e. to the number of collisions made by the corpuscle in moving over 1 cm. Thus, from the table, we may infer that a corpuscle makes about 3.25 collisions per cm. when moving through air at a pressure of '17 mm. of mercury. Townsend has shown that the number of collisions determined in this way agree well with the number deduced from the Kinetic Theory of Gases for the collisions between a body of negligible size and one of the size of a molecule of air. The number of collisions made by a corpuscle moving through air at a pressure of 1 mm. of mercury, as determined by the above method, is about 21. Townsend and Kirby have shown that the numbers of collisions made by a corpuscle moving through hydrogen or carbonic acid at this pressure are respectively 11.5 and 29: these, again, agree well with the values deduced from the Kinetic Theory.

When we are dealing with corpuscles moving with the velocity of those in the Lenard rays, i.e. with velocities between 10° and 10° cm./sec., the number of ions produced is much smaller than those produced by the comparatively slow corpuscles dealt with in the preceding experiment: thus, Durack\* has shown that a corpuscle moving with a velocity of 5 × 10° cm./sec. only produces about '4 ions when moving through 1 centimetre of air at the pressure of 1 mm. of mercury, and with the still more rapidly moving corpuscles shot out from radium the ionisation is still smaller. The effect of velocity on the ionisation may, I think, be explained by considerations of the following kind: let us suppose that the molecules of a gas consist of a large number of smaller particles, and that each of these repels the corpuscle; for the sake of taking a definite case, let us consider a molecule as analogous to a metallic cage enclosing a large number of nega-

<sup>\*</sup> J. J. E. Durack, Phil. Mag. vi. 4, p. 29, 1902.

tively electrified particles, the force due to these outside the cage being balanced by a positive charge on the cage itself, equal in magnitude to the sum of the negative charges on the particles inside the cage; then if a slowly moving corpuscle were to penetrate the cage, the repulsions exerted on it by the particles would at once drive it out before it had penetrated an appreciable distance inside the cage: thus, in this case, the number of collisions made by the corpuscle in its journey through the gas would be the same as the number it would make if the molecules of the gas were hard, impenetrable, elastic solids; we have seen that this hypothesis agrees well with the results of experiments on slowly moving corpuscles. If, however, the velocity of the corpuscle is very great, the repulsion of the particles inside the cage will not stop the corpuscle; the corpuscle will penetrate the cage, being deflected by every particle it passes. The conditions of the problem are now quite different from those when the corpuscle was moving so slowly that it could not penetrate the cage; we proceed briefly to consider the collisions in this The problem of the collision between bodies repelling each other with a force varying inversely as the nth power of the distance has been investigated by Maxwell\*, who solved the problem when the two bodies were moving with any velocities. We shall suppose that the velocity of the particles is so small with respect to that of the corpuscle that they may be supposed to be at rest. In this case, if T is the kinetic energy of a corpuscle,  $\delta T$  the change in T due to a collision, then Maxwell's result gives

$$\delta T = \frac{4M_1M_2}{(M_1 + M_2)^2} T \sin^2 \theta,$$

where  $M_1$ ,  $M_2$  are the masses of the corpuscle and the particle respectively, and  $\theta$  is given by the equation

$$\frac{\pi}{2} - \theta = \int_{0}^{x'} \frac{dx}{\sqrt{1 - x^2 - \frac{2}{n - 1} \left(\frac{x}{\alpha}\right)^{n - 1}}};$$

the force between the bodies is supposed to vary inversely as the  $n^{\rm th}$  power of the distance between them, and

$$\alpha = b \left\{ \frac{V^{2} M_{1} M_{2}}{K \left( M_{1} + M_{2} \right)} \right\}^{\frac{1}{n-1}},$$

<sup>\*</sup> Maxwell, Collected Papers, Vol. ii. p. 26.

where V is the velocity of the corpuscle before collision, b the length of the perpendicular let fall from the particle on the line of flight of the corpuscle before collision, and K the force at unit distance.

x' is the positive root of the equation

$$1 - x^{2} - \frac{2}{(n-1)} \left(\frac{x}{\alpha}\right)^{n-1} = 0.$$

Let us take the case when the force varies inversely as the square of the distance, i.e. n = 2, then we have

$$\frac{\pi}{2} - \theta = \int_{0}^{x'} \frac{dx}{\sqrt{1 - x^2 - \frac{2x}{\alpha}}}$$

$$= \frac{\pi}{2} - \sin^{-1} \frac{\frac{1}{\alpha}}{\sqrt{1 + \frac{1}{\alpha^2}}};$$
thus
$$\sin \theta = \frac{1}{\sqrt{1 + \alpha^2}} = \frac{1}{\left\{1 + \frac{b^2 V^4}{K^2} \left(\frac{M_1 M_2}{M_1 + M_2}\right)^2\right\}^{\frac{1}{2}}},$$
and hence  $\delta T = -\frac{4M_1 M_2}{(M_1 + M_2)} T \cdot \frac{1}{1 + \frac{b^2 V^4}{K^2} \left(\frac{M_1 M_2}{M_1 + M_2}\right)^2}.$ 

Since T varies as  $V^2$  we see that when V is small  $\delta T$  will increase with V and will be proportional to  $V^2$ , it will reach a maximum value when  $V^2 = \frac{K}{b} \frac{M_1 + M_2}{M_1 M_2}$ , while for larger values of V,  $\delta T$  will decrease as V increases and will ultimately vary as  $1/V^2$ .

Now  $-\delta T$  is the energy lost by the corpuscle and given up to the particle; thus  $\delta T$  will measure the energy available for dissociating the molecule, the ionising effect will therefore reach a maximum value and will then diminish as the velocity increases. When  $\alpha$  is large,  $\theta$  is proportional to  $1/\alpha$ , i.e. to  $1/V^2$ ; now  $2\theta$  is the angle through which the direction of motion is deflected, thus, for corpuscles moving with different speeds, the ionisation of the gas and the diffusion of the corpuscles will be proportional to each other.

## CHAPTER XIII.

#### SPARK DISCHARGE.

179. WE have hitherto mainly been discussing cases in which the ionisation was produced independently of the electric field acting upon the gas, we shall now proceed to the consideration of cases in which the ionisation is mainly due to the action of the electric field itself, and when the electric field before sending the electric current through the gas has first to make the gas a conductor. Cases when ionisation is produced by an electric field have already been considered on pp. 231 et seq., we shall now consider the most familiar case of this kind,—the electric spark. as simple a case of this as possible, let us suppose that we have two large metal plates parallel to one another and near together, let the plates be placed in connection with a large battery of cells or some other means of producing a difference of potential between them; then if we start with a very small difference of potential between the plates the only current which will pass from one plate to the other will be the very small one due to the spontaneous ionisation of the gas between the plates; this current is not luminous and is proportional to the distance between the plates, and so by pushing the plates near together may be made as small as we please. On measuring the potential difference, however, a stage is reached when a current accompanied by luminosity passes between the plates, and when this, the sparking stage, is reached the potential differences between the plates remain approximately constant, even when the number of cells in the circuit connecting the two plates is increased. The potential difference between the plates when the spark passes depends upon the distance between the plates, i.e. the length of the spark, and on the nature and pressure of the gas in which the plates are immersed; the investigation of the

connection between these quantities has occupied the attention of many observers. Before we consider their results, it will be useful to consider some properties of the spark which have an important effect on the accuracy of such observations.

180. We shall call the greatest potential difference, which can be applied to the electrodes for an indefinitely long time without causing the spark to pass, the spark potential difference. It must not be supposed, however, that whenever a potential difference just greater than this is applied to the plates a spark always passes; it frequently happens that if the potential difference is only applied for a short time the air between the plates can sustain a much greater difference of potential than the spark potential without a spark passing through it. Thus Faraday\* long ago observed that it takes a greater potential difference to start the first spark than is required to keep up the sparks when once they have been started, and that the effect of one spark in facilitating the passage of its successors does not die away until the gas has rested for several minutes. I found that if the gas is dried with extreme care it is possible to get it to stand without a spark passing a potential difference three or four times as large as that which is sufficient to produce a spark in less perfectly dried gas+. The dry gas seems, however, to be in an unstable state as far as its electrical properties are concerned, for when once a spark has been forced through it the potential difference between the plates falls to the value for a moist gas, and the gas is not again able to stand a greater potential difference until it has rested for several minutes; this result suggests that if we had a perfectly dry gas it might not be possible to start a spark through it. The gas would, however, be in an unstable state, and may be compared to a supersaturated solution into which a foreign body has to be introduced before crystallisation begins, though the process once started continues until the solution ceases to be supersaturated. Another analogy would be a gas supersaturated with aqueous vapour, when for condensation to take place we require the presence of nuclei round which the drops may condense. The tendency of the gas to get into this electrically unstable state is much diminished by the presence of moisture, or of gases from flames, sparks,

<sup>\*</sup> Faraday, Experimental Researches, § 1417.

<sup>+</sup> J. J. Thomson, Phil. Mag. v. 36, p. 313.

or arcs, by the illumination of the cathode by ultra-violet light, or by the exposure of the spark-gap to Röntgen or Becquerel rays, in short by any agent which introduces ions into the field. Warburg\* has made very extensive researches on the effect produced by several of these agents on the passage of sparks; the method he used consisted in measuring the interval between the application of a potential difference greater than the spark potential and the passage of the spark; this interval, which may be several minutes when the potential only just exceeds the spark potential, diminishes as the potential difference increases, we shall call it the 'lag' of the spark. The amount of the 'lag' has an important effect on many phenomena connected with sparks; thus for example if it is great and an induction coil or some other machine furnishing a very rapidly changing potential be used to produce the spark, the terminals may support for the short time during which the electric field lasts a potential difference which would produce a spark if the lag were short; in a case like this an agent might make the spark pass by diminishing the time of lag even though it had no effect on the spark potential. A notable instance of this is the effect produced by ultra-violet light on sparks passing between the terminals of an induction coil. Hertz+ showed that the exposure of the spark-gap to such light facilitated the passage of the spark; E. Wiedemann and Ebert; showed that if the negative electrode is screened off from the light, leaving the spark-gap and positive electrode illuminated, no effect is produced; we have seen (Chapter X.) that the illumination of a negatively electrified body leads to a discharge of negative ions, and that no ions are produced when the body is positively electrified. Swyngedauw§ found that if the positive electrode was large its illumination helped the spark: it is possible that with large electrodes sufficient light may be reflected from the positive to the negative electrode, or to some body in the neighbourhood of the positive electrode which is negatively electrified by induction, to cause the negatively electrified body to emit ions.

<sup>\*</sup> Warburg, Sitz. Akad. d. Wissensch., Berlin, xii. p. 223, 1896; Wied. Ann. lix. p. 1, 1896; lxii. p. 385, 1897.

<sup>+</sup> Hertz, Wied. Ann. xxxi. p. 983, 1887.

<sup>‡</sup> E. Wiedemann and Ebert, Wied. Ann. xxxiii. p. 241, 1888.

<sup>§</sup> Swyngedauw, Rapports presentés au Congrès International de Physique, Paris, iii. p. 164.

Wiedemann and Ebert (l.c.) showed that the nature of the gas had considerable influence upon the amount of the effect produced by ultra-violet light, the effect being especially large in carbonic acid gas (the currents due to photo-electric effects in this gas are much larger than in air). Warburg\* showed that the chief effect of the ultra-violet light was to diminish the 'lag' and that the effect on the spark potential was comparatively small. This is clearly shown by the figures given in the following table, taken from Warburg's paper: the potential difference was produced by a battery of storage cells, and a contact make and break was used, by means of which the potential difference was applied to the air-gap for a short interval, in this case '0012 sec. The fractions in the table have for their numerators the number of times a spark passed when the potential difference was applied for this time, and for their denominators the number of times the potential difference was applied; thus the fraction  $\frac{0}{10}$  indicates that the spark never passed, and the fraction  $\frac{10}{10}$  that it always did so. The gas used in these experiments was hydrogen at a pressure of 11 mm. of mercury, the spark potential was 960 volts in daylight, 1080 in the direct light from an arc lamp, and 1260 when this light had passed through glass. The electrodes were platinum spheres, 7 mm. in diameter, and the spark length was 4.5 cm.

Potential Difference in volts	096	1440	1500	1920	2040	2940	3000	3960	5040	0009	7020	7920	8940
In the dark  In daylight  In the arc light through glass  In the arc light	0 10	10	10	10	3 10	8 10	0 10	110	10	10	10	710	10

It will be seen from this table that while in the dark the spark does not always pass even when the potential difference is 9 times that required to produce a spark when the field is continuous, in the arc light a potential difference only a little greater than the minimum required to produce a spark, always produces a spark; the table shows too that daylight produces a very perceptible diminution of the 'lag.'

<sup>\*</sup> Warburg, Sitz. Akad. der Wissenschaften, Berlin, xii. p. 223, 1896.

Warburg \* showed that the 'lag' in a very dry gas was much longer than in one containing a small quantity of water vapour; the difficulty of starting the electric discharge in very carefully dried gas has already been alluded to (see p. 347).

The importance of the 'lag' in relation to the mechanism of the spark discharge seems first to have been realised by Jaumann+, who pointed out that while it lasted some process must be going on in the gas which converts it from an insulator to a conductor. During this process no light can be detected even in the darkest room, and both Jaumann and Warburg failed to find by direct experiments with electroscopes any indication of a current passing through the gas at this stage. Warburg+, however, at low pressures observed some effects which seem to indicate that during the lag there is a current passing through the gas although it is too small to be detected by an electroscope or to produce any luminosity. The evidence for this is based on the effect produced by a magnet on the discharge through a gas at low pressure; a discharge is hindered by the action of a transverse magnetic field owing to the deflection of the ions which carry the current; Warburg showed that the magnetic field not only hampered the luminous discharge, it also produced a great increase in the duration of the 'lag,' he concluded from this that during the lag there is a feeble current which is essential for the production of the spark, and that the magnetic field by hampering this current prolongs the time which has to elapse before the spark can pass. Walter by taking photographs of sparks on rapidly moving plates has shown that a bright spark is preceded by faintly luminous brush discharges. We shall see when we consider the theory of the spark discharge that the formation of a preliminary current is necessary for the production of the spark.

Effect of rapid variations in the potential of the terminals on the passage of a spark,

181. Jaumann  $\parallel$  has made some interesting experiments on the effect on the spark length of rapid changes in the electrical

<sup>\*</sup> Warburg, Wied. Ann. lxii. p. 385, 1897.

<sup>†</sup> Jaumann, Ib. lv. p. 656.

<sup>‡</sup> Warburg, Ib. lxii. p. 385.

<sup>§</sup> Walter, Ib. lxvi. p. 636, lxviii. p. 776.

<sup>||</sup> Jaumann, Wien. Sitz. xcvii. p. 765, 1888.

condition of the electrodes. The experiments are of the following The main current from an electrical machine charged the

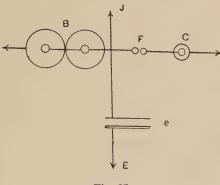


Fig. 87.

condenser B, while the condenser C could be charged through the air space F, C being a small condenser whose capacity was only 55 cm., while B was a battery of Leyden jars whose capacity was about 1000 times that of C; a wire was connected to the inside coating of B and terminated about 5 mm. above the plate E, which was connected with the earth. A glow discharge passed from the wire to the plate, and the difference of potential between the outside and inside coatings of the jars B was constant and equal to about 12 electrostatic units. When the knobs of the air break F were suddenly pushed together a spark about 5 mm. in length passed across the air break and in addition a bright spark 5 mm. long jumped across the air space at e where there was previously only a glow. The passage of the spark at F put the condenser Cin connection with B, and thus produced a rapid variation in the potential of the wire, and the spark at E was the result. From experiments of this kind Jaumann came to the conclusion that if V is the potential difference between the electrodes the condition

for sparking is that  $V\frac{dV}{dt}$  and not V should have a definite value,

so that if we could make the potential difference vary with great rapidity it might produce a spark even though its magnitude were much below the sparking value. I cannot see, however, that the experiments justify this conclusion; it must be remembered that when we add on the small condenser we start electrical vibrations,

and that while these are going on the maximum value of the potential in certain parts may greatly exceed the value when the vibrations have died away. Thus, to take a very simple case, suppose A is a very large Leyden jar, while B is a very small one, originally A is charged, B is not, the outsides of both are connected with the earth; if the insides of A and B are suddenly connected, then though the final potential of B will be smaller than the initial value of the potential of A, yet the maximum value during the oscillations will be nearly twice as large as the initial potential of A, and thus if B were suddenly connected with A a spark might pass across the plates of B although B might stand without sparking a potential difference equal to that originally existing between A: the passage of this spark would, however, be due to the oscillation producing a great increase in the maximum potential difference, and would not necessarily indicate that with a given potential difference the spark would pass more easily if this were changing than if it were steady. This question has been the subject of much controversy, it is often called the question of 'constant spark potential' and has been discussed by Jaumann\*, Swyngedauw<sup>†</sup>, and K. R. Johnson<sup>‡</sup>.

Variation of the spark potential difference with the spark length and pressure of the gas.

182. The first measurements of the potential difference required to produce a spark through air at atmospheric pressure were made by Lord Kelvin§ in 1860, since then the subject has attracted much attention and important investigations have been made by Baille||, Liebig¶, Paschen\*\*, Peace††, Orgler‡‡, Strutt§§, Bouty||||, Earhart¶¶ and Carr\*\*\*. The values of the spark potential differ-

- \* Jaumann, Wied. Ann. lv. p. 656, 1895; Wien. Sitz. xevii. p. 765, 1888.
- † Swyngedauw, Thèse : Contribution à l'Étude des Décharges, 1897.

‡ Johnson, Drude's Ann. iii. p. 460, 1900; v. p. 121, 1901.

- § Lord Kelvin, Collected Papers on Electrostatics and Magnetism, p. 247.
- || Baille, Annales de Chimie et de Physique [5], xxv. p. 486, 1882.
- ¶ Liebig, Phil. Mag. v. 24, p. 106, 1887.
- \*\* Paschen, Wied. Ann. xxxvii. p. 79, 1889. ++ Peace, Proc. Roy. Soc. lii. p. 99, 1892.
- ## Orgler, Drude's Ann. i. p. 159, 1900.
- §§ Strutt, Phil. Trans. 193, p. 377, 1900.
- Bouty, Comptes Rendus, 131, pp. 469, 503, 1900.
- ¶¶ Earhart, Phil. Mag. vi. 1, p. 147, 1901.
- \*\*\* Carr, Proc. Roy. Soc. lxxi. p. 374, 1903.

ence given by the earlier experimenters are as a rule somewhat larger than those found under similar circumstances by more recent observers, probably because latterly more attention has been paid to eliminating the effects due to 'lag'; whenever 'lag' is present the potential difference when the spark passes is higher than the minimum required to produce a spark. We shall first give a general account of the laws which have been brought to light by the experiments made on this subject, reserving until the end of the chapter the tables which embody the numerical results obtained by the above-mentioned physicists.

Let us first take the case where the electrodes are so large compared with the distance between them and placed in such a position that the lines of electric force are parallel to each other, this condition would be fulfilled if the electrodes were parallel planes placed at a distance from each other not greater than a small fraction of their diameter; it is approximately fulfilled in the arrangement most frequently used where the electrodes are portions of spheres of large radius placed close together.

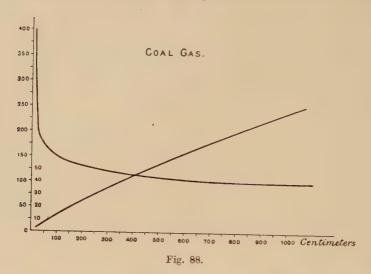
In the first place the potential difference required to produce a spark of given length does not depend upon the metal of which the electrodes are made (it is possible that aluminium and magnesium electrodes may be exceptions to this rule). Experiments on this point have been made by Righi\*, Peace, and Carr. Righi tried electrodes of carbon, bismuth, tin, lead, zinc, and copper and got the same potential difference with all these substances. Peace (l.c.) who made very careful experiments with electrodes of zinc and brass could not detect the slightest difference in the potential difference required to spark across them. Carr found the spark potential to be the same with electrodes of brass, iron, zinc, and aluminium. On the other hand, De la Rue and Hugo Müller+ came to the conclusion that sparks pass more easily between aluminium electrodes than between electrodes of any other metal, but that with this exception the nature of the electrodes has no influence upon the spark length. It is worthy of remark that the cathode fall of potential which is very closely connected with the spark potential is nearly the same for electrodes

<sup>\*</sup> Righi, Nuovo Cimento (2), xvi. p. 97, 1876.

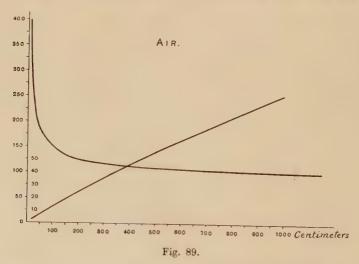
<sup>†</sup> De la Rue and Müller, Phil. Trans. 169, Pt. 1, p. 93, 1898.

of all the metals used by Righi; for aluminium and magnesium electrodes, however, it is decidedly smaller.

The connection between the spark potential and the spark



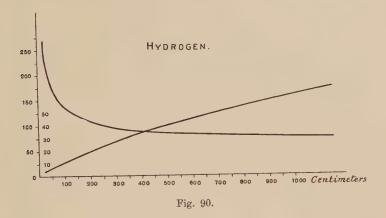
length is represented by the curves given in Figs. 88, 89, 90, and 91 for air, hydrogen, and carbonic acid and coal gas at



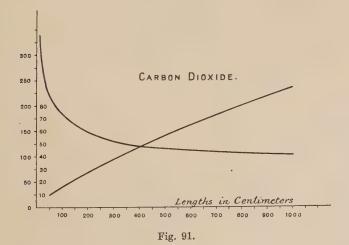
atmospheric pressure, the ordinates are proportional to the

potential difference required to produce a spark of a length represented by the abscissae.

The curves in Figs. 88—91 are due to Liebig (l.c.), who used spherical electrodes 19.5 cm. in diameter. The curves



running up to the vertical axes represent the connection between the average value of the electric intensity, *i.e.* V/d where V is the spark potential and d the spark length, and the spark length.



It will be seen that except for very short sparks the curves representing the relation between V and d are approximately

straight lines, so that for moderately long sparks the relation between V and d would be of the form

$$V = a + bd$$

where a and b are constants. Chrystal\* has shown that the simple relation

$$V = 4.997 + 99.593d$$

where V is measured in electrostatic units and d in centimetres agrees with Baille's very numerous experiments on the spark potential in air at atmospheric pressure quite as well if the spark length exceeds 2 mm. as the more complicated formula

$$V^2 = 10500 (d + 0.08) d$$

proposed by Baille himself. Carey Foster and Pryson† also found that the linear relation V=a+bd was the one which best represented the results of their experiments on the potential difference required to spark through gas at atmospheric pressure.

183. The curves we have given do not however give any indication of the relation between the spark potential and the spark length when the latter is exceedingly small. When the spark length falls below a certain value which is inversely proportional to the pressure, and which we shall call the critical spark length, the potential difference has a minimum value, and if the spark length is still further diminished the spark potential begins to increase and goes on increasing until the spark length gets down to about 10-4cm., when it very rapidly diminishes. The increase of the spark potential due to a diminution in the spark length was first observed by Peace; as the critical spark length at atmospheric pressure is exceedingly small, only about '01 mm., it is difficult to experiment with sparks short enough to show the effect, as however the critical spark length varies inversely as the pressure, we can by diminishing the pressure increase the critical spark length until its observation becomes comparatively easy. Perhaps the simplest way of showing the effect is to use slightly curved electrodes and to observe the position of the spark as these are brought closer together. When the electrodes are at some distance apart the spark passes along the shortest line between them; as the electrodes

<sup>\*</sup> Chrystal, Proc. Roy. Soc. Edin. xi. p. 487, 1882.

<sup>†</sup> Carey Foster and Pryson, Chemical News, xlix. p. 114, 1884.

are pushed together it will be found that a stage is reached when the spark no longer passes along the shortest line, but goes to one side, taking a longer path, showing that it is easier to produce a long spark than a short one; with this arrangement the potential difference required to produce the spark does not vary, as the electrodes are moved nearer together it remains constant and equal to the minimum potential difference required to produce a spark; the spark length too is constant and equal to the critical spark length; the position of the spark is determined by the condition that it passes at the place where the distance between the electrodes is equal to the critical spark length. In order to measure the increase of potential difference due to the diminution in spark length it is necessary to use perfectly flat and parallel electrodes, when these are pushed together the length of the spark is necessarily diminished. The electrodes used by Carr (l. c.) are represented in Fig. 92; they were plane brass plates embedded in ebonite and separated by ebonite rings of different

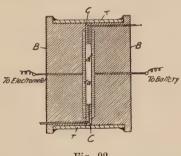


Fig. 92.

thicknesses. With this apparatus Carr obtained the results given in the following table:

Pressure 2.02 mm.: gas—air.

Spark length	Spark potential in volts
1 mm.	558
2 mm.	371
3 mm.	357
5 mm.	376
10 mm.	472

Pressure 1.05 mm.: gas-air.

Spark length	Spark potential in volts
1 mm.	1826
2  mm.	594
$3 \mathrm{\ mm}$ .	397
$5 \mathrm{\ mm}$ .	355
10 mm.	379

The effect is even more strongly marked in hydrogen, as the following table shows.

Pressure 2:6 mm.: gas-hydrogen.

Spark length	Spark potential in volts
1 mm.	1781
2 mm.	462
3 mm.	398
5  mm.	285
10 mm.	317

In each of these cases the spark potential for the shortest spark is greater than for the longest. When the spark length falls below about  $5 \times 10^{-4}$  cm. the spark potential, as Earhart has shown, falls off rapidly; we shall return to this point later on. The existence of a critical spark length is also proved by the remarkable changes which take place in the appearance of the discharge when the electrodes are brought very near together. Thus in the course of some experiments on the discharge between large parallel plates I observed\* that at very low pressures the discharge went from the under side of the lower plate, which was the positive electrode, and round to the top of the upper plate, the space between the plates was quite free from any luminous discharge: showing the discharge went more easily round the longer path than by the much shorter one between the plates. The same thing is shown in Figs. 93 and 94, which are drawings given by Lehmann+ of the appearance as seen through a microscope of the discharge

<sup>\*</sup> J. J. Thomson, Proc. Camb. Phil. Soc. v. p. 395, 1886.

<sup>+</sup> Lehmann, Molecülare Physik, ii. p. 295.

between electrodes of different shapes placed very near together. A very famous experiment due to Hittorf\*, represented in Fig. 95,

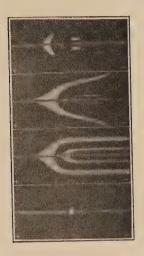


Fig. 93.



Fig. 94.

is another illustration of this. The two electrodes were only 1 mm. apart, the regions around them were connected together by a long

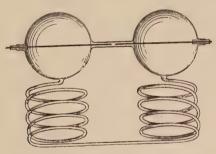


Fig. 95.

spiral tube 375 cm. long; in spite of the enormous difference between the lengths of the paths the discharge, when the pressure was very low, all went round through the spiral, the space between the electrodes remaining quite dark.

184. The curves in Figs. 88—91 show how rapidly the value of V/d (V being the spark potential and d the distance

<sup>\*</sup> Hittorf, Wied. Ann. xxi. p. 96, 1884.

between the plates) increases as d diminishes. This was observed by Lord Kelvin in 1860. If the electric field were uniform V/d would be the electric intensity between the plates; in general, however, when a current of electricity passes through a gas the field is not uniform but is greater at one or both of the electrodes than in the rest of the field, we are not justified therefore in assuming that V/d is the maximum electric intensity between the electrodes.

## Variation of the spark potential with the pressure.

185. If the spark length is constant and not too small then, starting with air at atmospheric pressure, as the pressure is diminished the spark potential decreases, the relation between the potential and pressure being at first a linear one; on further diminution of the pressure the spark potential reaches a minimum value, after this any further diminution in the pressure is accompanied by an increase in the spark potential. The relation between the spark potential and the pressure is represented by the curve in Fig. 96,

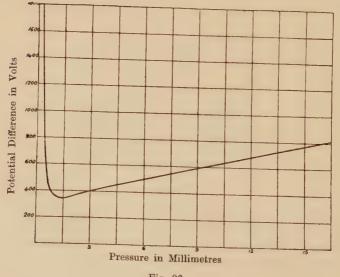
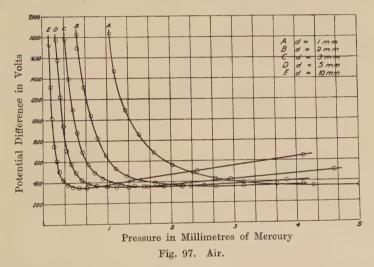


Fig. 96.

taken from a paper by Carr (l.c.); in this curve the ordinates represent the spark potential, the abscissae, the pressure; the

electrodes were parallel planes and the spark length 3 mm. The pressure at which the spark potential is a minimum is called the critical pressure. Peace (l.c.) showed that the critical pressure depended upon the spark length, the shorter the spark length the greater the critical pressure. He showed too that the minimum spark potential was constant, being independent of the spark length; in air it was equal to about 351 volts, so that unless the spark length is less than about  $5 \times 10^{-4}$  cm., a potential difference of less than 351 volts cannot produce a spark.

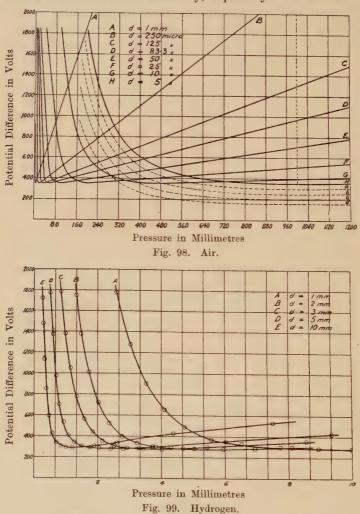
These points are well illustrated by the curves in Fig. 97, taken from Carr's paper; they represent the relation between the pressure and the spark potential, for sparks of 1, 2, 3, 5, and 10 mm.



The critical pressures for these spark lengths as given by Carr are as follows.

Spark length	Critical pressure	Product of spark length and critical pressure
1 mm.	4.98 mm.	4:98
2 mm.	2.71 mm.	5:42
3 mm.	1.89 mm.	5:67
5 mm.	1.34 mm.	6:7
10 mm.	679 mm.	6:79

It will be seen that the product of the critical pressure and the spark length is approximately constant: we must remember that owing to the flatness of the curves in the neighbourhood of the critical pressure the exact determination of the critical pressure is a matter of some difficulty, especially with the shorter



sparks: the differences in the product of the critical pressure and the spark length are not greater than could be accounted for by the errors in the determination of the critical pressure.

The same features are shown by sparks through hydrogen and

carbonic acid; the curves for these as given by Carr are shown in

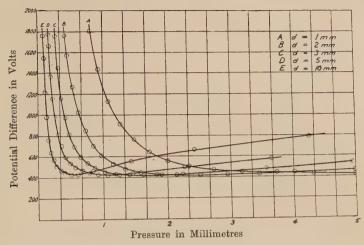


Fig. 100. Carbon Dioxide.

Figs. 99 and 100, and the connection between the critical pressure and the spark length shown in the following tables:

Hydrogen. Minimum potential 280 volts.

Spark length	Critical pressure	Product of spark length and critical pressure
1 mm.	10·3 mm.	10·3
2 mm.	5·93 mm.	11·8
3 mm.	4·02 mm.	12·06
5 mm.	2·8 mm.	14·0
10 mm.	1·46 mm.	14·6

Carbonic acid. Minimum potential 420 volts.

Spark length	Critical pressure	Product of spark length and critical pressure
1 mm.	5·02 mm.	5·02
2 mm.	2·52 mm.	5·04
3 mm.	1·63 mm.	4·89
5 mm.	1·07 mm.	5·35
10 mm.	·510 mm.	5·1

The constancy of the product of spark length and critical pressure in the case of carbonic acid is very marked.

Carr has also given curves for the connection between spark length and pressure for  $H_2S$ ,  $SO_2$ ,  $CO_2$ ,  $C_2H_2$ ,  $O_2$ ,  $N_2O$ ; these are shown in Fig. 101.

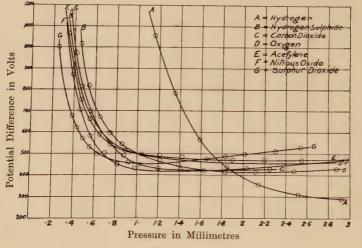


Fig. 101.

The spark length for these gases was 3 mm.

Very careful experiments on the relation between the pressure and the spark potential were made by Strutt\* for air, hydrogen, nitrogen, and helium; the experiments on nitrogen and helium are especially interesting, as the minimum spark potential in these gases was found by him to be greatly affected by minute traces of impurity. Thus the presence of a very minute quantity of oxygen in nitrogen increased the minimum spark potential from 251 volts to 388 volts. Thus nitrogen from which the oxygen had been removed by passing the gas over metallic copper gave a minimum spark potential of 388 volts, the value of this potential for a specimen of nitrogen prepared from air by the absorption of the oxygen by alkaline pyrogallol was 347 volts; when, however, the oxygen was more completely removed by bubbling the gas repeatedly through the liquid alloy of sodium and potassium the minimum spark potential fell to 251. The curves obtained by

<sup>\*</sup> Hon. R. J. Strutt, Phil. Trans. 193, p. 377, 1900.

Strutt for nitrogen are shown in Fig. 102. Curve No. 2 refers to the purest specimen, curve No. 1 to a specimen which had been

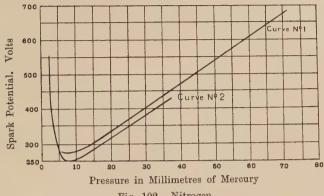
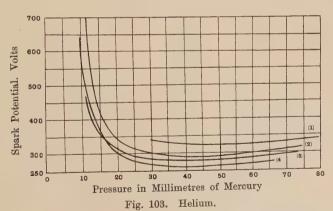


Fig. 102. Nitrogen.

passed several times through the sodium and potassium alloy, but not so often as that to which curve No. 2 relates: the minimum spark potential for this specimen was 276 volts. The curves after passing the critical pressure are parallel.

The discharge through helium, which was also studied by Strutt, presents many interesting features. Ramsay and Collie \* first drew attention to the ease with which the discharge passed through



helium. Strutt's experiments, the results of which are represented in Fig. 103, show that for a given length of spark the critical

<sup>\*</sup> Ramsay and Collie, Proc. Roy. Soc. lix. p. 257, 1896.

pressure is exceedingly high, being about 5 times that of air for the same spark length and more than twice that of hydrogen. The great effect of small impurities on the minimum spark potential is shown by the different curves in Fig. 103, which refer to samples purified in different ways: the smallest value of this potential obtained by Strutt was 261 volts.

186. We have seen that the product of the critical pressure and the spark length is constant and is also independent of the nature of the electrodes, it is thus a property of the gas; the following table contains the values of this product q, calculated from the measurements of Carr and Strutt, and also the mean free paths  $(\lambda)$  of the molecules of the gases at atmospheric pressure, these with the exception of helium are taken from the table in O. E. Meyer's Kinetische Theorie der Gase, p. 142, that of helium is deduced from Lord Rayleigh's\* experiments on the viscosity of helium: though these free paths are taken for a particular pressure, the ratio of the free paths of the molecules of different gases is independent of the pressure. The numbers in column (3) are the spark length in millimetres multiplied by the critical pressure:

Gas	Minimum spark potential	q	$\lambda \times 10^5  \mathrm{cm}$ .	$10^5  imes \lambda/q$
Air Nitrogen Oxygen Hydrogen Carbonic acid. Sulphur dioxide. Nitrous oxide. Sulphuretted hydrogen Acetylene Helium	418 C.	5·7 6·7 14·4 5·1 3·3 5 6	.95 .98 1.05 1.8 .68 .48 .68 .628	17 14 12 13 14 14 10

The letters S. and C. indicate that the measurements were made by Strutt or Carr: no very great accuracy can be claimed for the values of q, as the determination of the critical pressure is difficult; a small error in the determination of the spark potential near this pressure would lead to a large error in the value of the

<sup>\*</sup> Lord Rayleigh, Proc. Roy. Soc. lxix. p. 198, 1896.

critical pressure. Taking this into account, I think the differences shown in the preceding table for  $q/\lambda$  from the constant value 1.3 are not, except in the case of sulphuretted hydrogen and helium, greater than might be explained by errors of experiment. In the two exceptions sulphuretted hydrogen and helium there are special circumstances which make us hesitate to accept the results as final without further experiment. Sulphuretted hydrogen is decomposed by the spark, hydrogen being liberated; if such a decomposition had occurred in the experiments we have used for the determination of q the spark would have passed through a mixture of hydrogen and sulphuretted hydrogen, the hydrogen would increase the critical pressure and hence the value of q. Again as Strutt's experiments show, the numbers for helium are very greatly affected by the presence of small amounts of impurity, so that it would hardly be safe to draw conclusions from this gas unless the free path determination had been made with the same specimen of gas as the electrical determinations.

We may, I think, conclude that for a large number of gases the value of  $q/\lambda$  is approximately constant, *i.e.* that with a given spark length the critical pressure is proportional to the mean free path of the molecules of the gas.

## Paschen's Law.

187. As the result of a very numerous series of experiments on the relation between spark potential and pressure, Paschen\* came to the conclusion that the spark potential depended only upon the product of the pressure and the spark length: *i.e.* upon the mass of gas between unit area of the electrodes. Thus, if the spark length d and pressure p of the gas are both altered, but in such a way that their product does not change, the spark potential V will remain constant; or in other words V is a function of pd.

The following results taken from Paschen's paper show how nearly the law is obeyed over the range of pressures studied by him; all these pressures it ought to be noticed are considerably above the critical pressures. V is the spark potential measured in electrostatic units, p the pressure measured in cm. of mercury,

<sup>\*</sup> Paschen, Wied. Ann. xxxvii. p. 79, 1889.

and d the spark length in cm.: the electrodes in these experiments were spheres 1 cm. in radius.

Air: pd = 7.5

p	d	V
10	0.75	16.23
15	0.50	16.54
20	0.38	16.75
25	0.30	17.00
30	0.25	16.83
40	0.17	16.86
50	0.15	16.68
75	0.1	16.33
	Mean	16.65

Air: pd = 20

p	d	V
28.6	0.7	34:30
33.3	0.6	34.63
40.0	0.5	35.12
50.0	0.4	34.77
66.66	0.3	35.39
	Mean	34.64

Hydrogen: pd = 7.5

p	d	V
10	0.75	9.50
15	0.50	9.32
$\frac{20}{25}$	0.38	9·47 9·59
30	0.25	9.58
40	0.187	9.69
50	0.15	9.90
75	0.10	10.44
	Mean	9.68

Hydrogen: pd = 20

p	d	V
28·6	0·7	19·12
33·33	0·6	19·25
40·00	0·5	19·43
50·00	0·4	19·43
68·66	0·3	20·00

Carbonic acid: pd = 7.5

p	d	V	
12·5 15·0 20·0 25·0 30·0 40·0 50·0	0.6 0.5 0.38 0.30 0.25 0.187 0.15	16:45 16:48 17:02 17:92 17:79 18:33 17:77	
75.0	0·10 Mean	$\frac{17 \cdot 21}{17 \cdot 37}$	

Carbonic acid: pd = 20

p	d	V	
33.33	0.6	33.03	
40.00	0.8	32.86	
50.00	0.4	33.46	
66.66	0.3	34.11	
	Mean	33.6	

The relation between the spark potential and the product pd is shown in the curves for air, hydrogen, and carbonic acid in

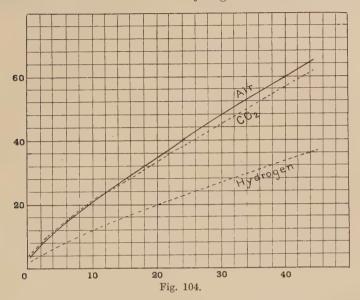
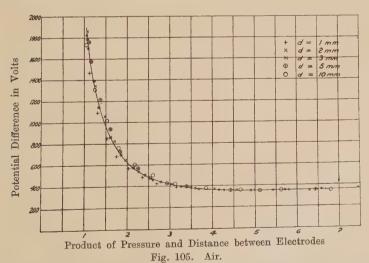


Fig. 104, the ordinates are the spark potentials in electrostatic measure, the abscissae the values of pd.



Paschen's experiments were all made at pressures considerably greater than the critical pressure; it has, however, quite recently

been shown by Carr (l.c.) that Paschen's law holds at all pressures. This is very clearly shown by the curves in Figs. 105, 106, which

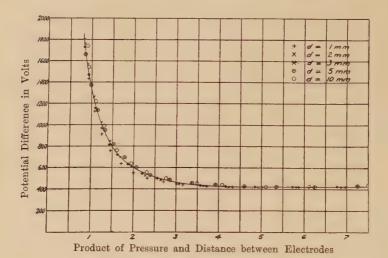


Fig. 106. Carbon Dioxide.

represent the relation between the spark potential V (in this case measured in volts) and the product pd (p was measured in millimetres of mercury and d in millimetres); five different values of d were used, ranging from 1 to 10 mm.; the results of these are represented on the curve by symbols attached to the points on the curve determined by the various experiments. It will be seen that the points for all the spark lengths all lie on the same curve, and in this case the range of pressures extended far below the critical pressure. The results of Paschen's law are very important; we see that to find the spark potential corresponding to any spark length and any pressure it is only necessary to possess the results of experiments made with a constant spark length over the whole range of pressures. We see, too, that it follows from this law that the critical pressure must vary inversely as the spark length, a result for which as we have seen there is direct experimental evidence. It follows too from this law that if we know the values of the spark potential required to produce a spark of constant length for all pressures we can deduce the value of the spark potential for a spark of any length at any pressure.

188. For pressures considerably greater than the critical pressure the relation between the spark potential and the spark length is a linear one; if V is the spark potential and x the spark length at atmospheric pressure, then

$$V = ax + b$$
,

where, if V is measured in electrostatic units and x in centimetres, the experiments by Baille, Liebig, Paschen, Orgler give the following values for the constants in hydrogen, air, and carbonic acid.

Gas	BAILLE		LIEBIG		Paschen		Orgler	
Gas	a 	<i>b</i>	a	<i>b</i>	a	<i>b</i>	a	<i>b</i>
Air Hydrogen Carbonic acid	99.6	5	87·4 55·8 91·8		92·5 43·0 91·1		93·6 46·3 85·6	

Wolf\*, who measured the spark potential required to produce a spark 1 mm. long at pressures varying from 1 to 5 atmospheres, found that (as we should expect from Paschen's law) the relation at these high pressures between spark potential and pressure is a linear one; if V is the spark potential in electrostatic measure and x the pressure in atmospheres, then Wolf found that V was given by the following expressions:

For hydrogen	V = 6.509 x	+6.5
For oxygen	V = 9.6x	+4.4
For air	V = 10.7 x	+3.9
For nitrogen	V = 12.08x	+ 5.0
For carbonic acid	V = 10.22x	+7.2.

If F is the average electric force between the electrodes in these experiments, then F = 10 V.

The order of the spark potential for different gases as will be seen from the preceding table depends upon the pressure; thus at the pressure of 1 atmosphere V for  $\mathrm{CO}_2$  is greater than V for air, while at high pressures it is less.

<sup>\*</sup> Wolf, Wied. Ann. xxxvii. p. 306, 1889.

189. Bouty\* has made a series of experiments on the electric field required to make a gas into a conductor, using a method which dispensed with the use of metallic electrodes. In this method the gas at a low pressure is contained in a glass vessel with parallel sides, and this vessel is placed in the space between two parallel plates parallel to the walls of the vessel, the difference of potential between these plates is increased until the gas in the glass vessel becomes luminous, indicating that a discharge is passing through it; the strength of the electric field, i.e. the electric force (not the potential difference), when this occurs is called by Bouty the cohésion diélectrique of the gas. A very considerable number of gases were examined by this method. Bouty found that the cohésion diélectrique F for gases up to 6 cm. pressure could be represented by the formula

F = a + bp,

where a and b are constants and p is the pressure. When F is measured in absolute electrostatic units and p in atmospheres, Bouty found that

For hydrogen F = 1.4 + 63.33 pFor air F = 1.593 + 119.09 pFor carbonic acid F = 1.703 + 144.4 p;

he compares these expressions with those given by Wolf and points out that while the coefficients of p are not so very different the constant terms are of quite a different order; he ascribes this difference to the electrodes in Wolf's experiments being metal, while in his experiments they were glass; it seems to me that the following explanation is more probable. If V is the potential difference required to produce a spark of length l through gas at a pressure p considerably greater than the critical pressure, then we have approximately, if A and B are constants,

$$V = A + Blp$$
;

since we know by Paschen's law that V is a function of lp; hence F, the average electric intensity when the spark passes, is given by the equation

 $F = \frac{A}{I} + Bp,$ 

hence the constant term varies inversely as the length of the spark
\* Bouty, C. R. 131, p. 469, 1900.

while the coefficient of p is independent of the spark length. In Wolf's experiments the spark length was only 1 mm., while the distance between the plates in Bouty's experiments was much greater so that the difference in the spark length would explain the difference in the constant term, and it is not necessary to ascribe it to the nature of the electrodes. Bouty\* has determined the constants a, b, in the expression F = a + bp for the cohésion diélectrique for a number of vapours, the results are given in the following table. Bouty's measurements were made at pressures ranging from 0055 cm. to 2 cm. of mercury. The constants apply when the pressure is measured in cm. of mercury and F in volts per cm.

Vapour of	a	<i>b</i>
Water	333	500
Methyl-alcohol	375	616
Ethyl-alcohol	364	800
Ether	360	1000
Methyl formate	364	1020
Ethyl propionate	312	1083
Acetone	355	1100
	360	1110
Ethyl formate	369	1250
Methyl acetate	330	1510
Carbon bisulphide	380	1610
Toluol	377	1670
Benzol	311	1070

It will be seen that the values of a vary very little in comparison with those of b. The values of b are in nearly every case in the same order as those of  $1/\lambda$ , where  $\lambda$  is the mean free path of the molecules of the gas, and are in many cases roughly proportional to this quantity. If the law which is suggested by these results actually holds and b is inversely proportional to  $1/\lambda$  the spark potential V required for a constant spark length must at pressures greater than the critical pressure be expressed by an equation of the form

 $V = a + \frac{b}{\lambda}$ ,

where  $\lambda$  is the mean free path of the molecules and a and b are constants which are the same for all gases.

<sup>\*</sup> Bouty, C. R. 131, p. 503, 1900.

190. v. Röntgen\* arrived at the conclusion that the spark potential for a constant spark length was inversely proportional to the mean free path of the molecules of the gas through which the spark passed; we have seen, however, that the ratio of the spark potential for different gases varies with the pressure and the spark length, so that this statement does not give complete expression to the laws of the spark-discharge. If we look at the question from the point of view of Paschen's law we see that from that law

$$V = f\left(\frac{x}{\lambda}\right)$$
,

where x is the spark length and  $\lambda$  the mean free path of the molecules of the gas; if the spark potential for different gases depended only upon the mean free path of the molecules of the gases the function f would be the same whatever were the nature of the gas; but, if this were the case the minimum potential required to produce a spark would be the same for all gases, a result which is inconsistent with the determinations made of this quantity. I have tried an equation of the form

$$V = A + F\left(\frac{x}{\lambda}\right)$$
,

where F is the same function for all gases and A a constant which may vary from one gas to another. Practically the only gases for which we possess sufficient materials to test this law adequately are air, hydrogen and carbonic acid. I have found that the observations in air and hydrogen are in fair agreement with this law, while those in carbonic acid are not: it is desirable, however, that the law should be tested over a far wider range of gases, as there are special circumstances connected with carbonic acid which make one hesitate to accept conclusions drawn from this gas alone; in the first place the experiments made by different observers differ more widely for this gas than for any of the others tested, it is one in which the 'lag' of the spark is exceedingly pronounced, and in other cases of discharge, such for example as that produced by ultra-violet light, it exhibits peculiarities not shown by air or hydrogen. Careful observations on the spark discharge in a gas which has a mean free path differing considerably from either hydrogen or air are much wanted.

<sup>\*</sup> Röntgen, Göttingen Nach. 1878, p. 390.

191. Natterer\* tested for a large number of gases the length of spark produced at constant pressure by a small induction coil; the measurements made by this method are of necessity exceedingly rough but they are for many gases the only measurements we possess relating to the passage of the spark. Part of Natterer's results are given in the following table, the temperature when not stated is to be taken as about 20° C., the spark lengths are in millimetres.

Gas	Spark length	Gas	Spark length
$\begin{array}{c} H_2 \\ N_2 \\ NO \\ O_2 \\ HCl \\ Cl_2 \\ HBr \\ HI \\ Br_2 (100^{\circ}C.) \\ I_2 (230^{\circ}C.) \\ H_2O (130^{\circ}C.) \\ H_2S \\ N_2O \\ SO_2 \\ HgCl_2 (271^{\circ}C.) \\ NH_3 \\ PH_3 \\ S_2Cl_2 (135^{\circ}C.) \\ PCl_3 (137.5^{\circ}C.) \\ AsCl_3 (181.5^{\circ}C.) \\ PBr_3 (271^{\circ}C.) \\ SiF_4 (101^{\circ}C.) \\ SiF_4 (101^{\circ}C.) \\ SiCl_4 (170^{\circ}C.) \\ SiCl_4 (170^{\circ}C.) \\ SnCl_4 (260^{\circ}C.) \\ CH_4 \\ C_2H_2 \\ \end{array}$	5-7 2-4 2-4 2-3·5 1·5-2 2-3 2·5-3 4-7 3-5 3-5 1·5-2 2-2·5 5-8 4-7 1·75-2 1·25-1·5 1·75-2 5-7 2·25-2·5 1·5-2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$\begin{array}{c} \text{HCN (80° C.)} \\ \text{CO} \\ \text{CO} \\ \text{C}_2\text{H}_4 \\ \text{C}_2\text{H}_6 \\ \text{CH}_3\text{OH (100° C.)} \\ \text{CO}_2 \\ \text{CH}_3\text{CHO (100° C.)} \\ \text{C}_2\text{H}_5\text{OH (110° C.)} \\ \text{C}_2\text{H}_5\text{OH (110° C.)} \\ \text{C}_2\text{H}_5\text{CO (100° C.)} \\ \text{C}_2\text{H}_6\text{CHO (100° C.)} \\ \text{C}_2\text{H}_5\text{CO (100° C.)} \\ \text{C}_2\text{H}_5\text{CO (100° C.)} \\ \text{C}_2\text{H}_5\text{CO (100° C.)} \\ \text{C}_3\text{H}_4\text{S (110° C.)} \\ \text{C}_4\text{H}_4\text{S (110° C.)} \\ \text{C}_4\text{H}_4\text{S (110° C.)} \\ \text{C}_2\text{H}_5\text{D (100° C.)} \\ \text{C}_4\text{H}_5\text{C (100° C.)} \\ \text{C}_4\text{H}_5\text{C (100° C.)} \\ \text{C}_4\text{H}_5\text{C (100° C.)} \\ \text{C}_4\text{C}_4\text{C}_5\text{C (100° C.)} \\ \text{C}_4\text{C}_4\text{C}_5\text{C (100° C.)} \\ \text{C}_4\text{C}_4\text{C (100° C.)} \\ \text{C}_4\text{H}_5\text{C (100° C.)} \\ \text{C}_4\text{C}_4\text{C (100° C.)} \\ \text{C}_5\text{C}_4\text{C (100° C.)} \\ \text{C}_5\text{C}_4\text{C (100° C.)} \\ \text{C}_5\text$	6—8 7—9 8—11 1·5—2 6—9 4—7 4—7 5—8 2—3 7—9 4—5 3—7 3—3·5 1·75—2 2—2·5 1·5—1·75—2 1·75—2 2—2·5

It will be noticed that the spark lengths are short in vapours of complicated chemical constitution in which the mean free paths are small; the halogen elements chlorine, bromine and iodine seem to exert a great influence in shortening the spark, these elements and their compounds have short free paths.

Natterer found that the spark length was exceptionally long

<sup>\*</sup> Natterer, Wied, Ann. xxxviii. p. 63, 1889.

in the monatomic vapours of mercury and cadmium, we have seen that it is also long in the monatomic gas helium.

## Theory of the Spark Discharge.

192. At this stage it may be useful to give an account of a theory which explains many of the peculiarities of the spark discharge. On this theory, which was given by the writer in a paper read before the Cambridge Philosophical Society, Feb. 1900, and published in the Philosophical Magazine, [5], 50, p. 278, 1900, the ionisation which is necessary to put the gas into the conducting state required for the passage of the spark is effected by means of ions which under the influence of the electric field producing the spark acquire so great a velocity that when they come into collision with the molecules of the gas through which they are moving they ionise the molecules. We have already had instances of the ionisation of a gas by rapidly moving ions in the cases of cathode and Lenard rays, and we have seen that the view (which was suggested by the consideration of the spark discharge) that ions in a strong electric field can acquire sufficient energy to enable them to act as ionising agents was of service in explaining some of the phenomena connected with the discharge of electricity produced by the action of ultra-violet light. Townsend (see p. 341) has shown that in the case of a gas ionised by means of Röntgen rays the negative corpuscles present in the gas can in a strong electric field produce fresh ions by their collision with the molecules of the gas; we have thus from several sources direct evidence that rapidly moving negative ions can by means of collision give rise to fresh ions.

Let us now consider the case of a gas between two parallel metal plates, between which there is an electric field, then if there were a few negative ions present these would be set in motion by the field, and if the strength of the field exceeded a certain value would acquire sufficient energy to ionise the molecules of the gas with which they came into collision, fresh ions would be produced and a current of electricity would flow through the gas. If, however, the conditions are such that only the negative ions in the field produce fresh ions, this current will only be transitory, in a short time all the negative ions will be driven up to the cathode and the current will stop. If, however, the positive ions in their

journey to the cathode can produce fresh ions, then negative ions are continually being produced, these under the action of the field will produce new ions and so the number of the ions and the conductivity of the gas will increase in geometrical progression; this increase will not, however, go on indefinitely, for with the increased conductivity of the gas the strength of the electric field between the plates will diminish until it falls to such a point that the number of ions produced in unit time by the field is equal to the number lost in the same time through the combination of the ions and through the motion of the ions up to the electrodes. To maintain the current it is not necessary for the positive ions to produce fresh ions at all parts of the field between the electrodes, it is sufficient for them to do so close to the cathode. The positive ions will strike against the cathode; we shall suppose that under this bombardment by the positive ions the cathode emits negative corpuscles—in fact cathode rays—so that the continuous supply of negative corpuscles comes on this view from the metal of the cathode stimulated by the positive ions striking against it. The action of the positive ions as ionising agents is thus confined to the effect produced by their impacts on the cathode, it is not necessary to suppose that they, like the negative corpuscles, ionise the molecules of a gas by striking against them. The expression for the potential difference is however the same whether we suppose that the positive ions cause the cathode to emit corpuscles by their impact with it, or whether we suppose that they ionise the gas close to the cathode, the positive ions in other parts of the field not possessing sufficient energy to ionise the gas.

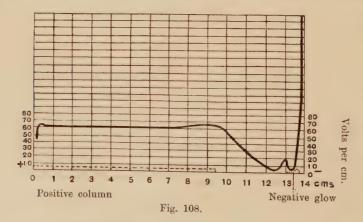
193. Before attempting to obtain by these principles the connection between spark potential, spark length and pressure it will be helpful to consider some facts as to the distribution of electric force along the spark, obtained by the study of the discharge at low pressures when the structure of the discharge is much more obvious than it is at atmospheric pressure. This structure as we shall see later shows many variations, but an example which may be taken as typical is that shown in Fig. 107. The distribution of electric intensity along the line of discharge is shown in Fig. 108. Next to the cathode there is a dark space called the Crookes dark space, the thickness of which does not depend upon the distance between the electrodes, then comes a luminous piece called the

negative glow, then comes a dark space called the Faraday dark space, and then a stretch of luminosity reaching to the anode,



Fig. 107.

called the positive column. From the curve giving the electric intensity we see that this is approximately uniform along



the positive column; but that in the Crookes dark space the electric intensity is very much greater. The potential difference

between the cathode and the negative glow, called the cathode potential fall, is as we shall see later independent of the pressure of the gas or the distance between anode and cathode, as long as this is greater than the thickness of the dark space. Recent measurements made by Strutt have proved that the cathode fall of potential is equal to the minimum spark potential. We see, too, that it is only in the Crookes dark space that the electric intensity is greater than in the uniform positive column, it is therefore only in this space that the positive ions would be likely to produce fresh ions by collisions with molecules of the gas. sum up we have a uniform electric intensity along the positive column and a variable but very much greater intensity inside the Crookes dark space. The thickness of the dark space does not depend upon the distance between the electrodes, so that the further these are apart the longer the region of uniform electric intensity along the positive column.

We shall now proceed to find the connection between the spark potential and the spark length. We found (p. 341) that if n is the number of corpuscles per unit volume at a distance x from the cathode, u the velocity of these corpuscles,  $\lambda$  their mean free path, e the charge on a corpuscle, then when the system is in a steady state

 $\frac{d}{dx}(nu) = \frac{nu}{\lambda}(f(Xe\lambda) - \gamma) \dots (1),$ 

where  $f(Xe\lambda)$  is the ratio between the number of collisions which produce fresh ions and the whole number of collisions, and  $\gamma$  the ratio of the number of collisions in which the corpuscles remain attached to the molecule to the whole number of collisions. If the electric field is very strong the corpuscles acquire so much energy that every collision produces ions, in this case  $f(Xe\lambda)=1$ , if  $Xe\lambda$  falls below a certain value then  $f(Xe\lambda)=0$ , we shall suppose that in the Crookes dark space the electric field is so strong that  $f(Xe\lambda)=1$ , and that in the rest of the field where the electric intensity is much less  $f(Xe\lambda)=\beta Xe\lambda-w$ , where  $\beta$  and w are constants.

From equation (1) we have

$$nu = n_0 u_0 e^{\int_0^x (f(Xe\lambda) - \gamma) \frac{dx}{\lambda}} \qquad \dots (2),$$

where  $n_0u_0$  is the value of nu when x=0, i.e. at the cathode; if we

put x=d in this expression we shall get the value of nu at the anode, this, if no positive ions come from the anode itself, is equal to i/e, where i is the current per unit area through the gas. Let us first take the case where d is greater than c, the thickness of the Crookes layer: then from x=0 to x=c,  $f(Xe\lambda)=1$ , and from x=c to d,  $f(Xe\lambda)=\beta Xe\lambda-w$ , hence in this case,

$$\int_{0}^{d} \left( f(Xe\lambda) - \gamma \right) \frac{dx}{\lambda} = \frac{c}{\lambda} + \beta e \left( V - V_{0} \right) - \frac{\gamma d}{\lambda} - \frac{w \left( d - c \right)}{\lambda},$$

where  $V_0$  is the fall of potential in crossing the Crookes dark space, *i.e.* the cathode fall of potential. Hence we have from (2) putting nu = i/e

$$i = n_0 u_0 e^{\frac{C(1+w)}{\lambda} + \beta e(V-V_0) - \frac{\gamma + wd}{\lambda}} \dots (3).$$

Now  $n_0 u_0$  is the number of corpuscles emitted in unit time by unit area of the cathode. We suppose that this emission is due to the bombardment of the cathode by the positive ions, and that the number of corpuscles emitted per second is proportional to the energy given to the cathode by the positive ions. The question now arises as to the energy possessed by the ions when they strike the cathode; before they reach the Crookes space they are moving in a weak part of the field, and their energy is proportional to  $Xe\lambda$ , where X is the electric intensity; when however they get into the dark space the field rapidly becomes more intense, and the energy of the positive ions rapidly increases, we shall therefore get a close approximation to the truth if we suppose that the energy of the positive ions is given to them in the dark space, and that the energy of each ion is equal to  $V_0e$ ,  $V_0$  being the cathode fall of potential. The number of positive ions which strike unit area of the cathode in unit time is  $(i - n_0 u_0 e)/e$ , and the energy given up by these to the cathode is therefore  $(i - n_0 u_0 e) V_0$ . We suppose that  $n_0 u_0$ the number of corpuscles emitted in unit time is proportional to the energy of bombardment, so that

$$n_0 u_0 = k (i - n_0 u_0 e) V_0$$

where k is a constant.

Substituting this value of  $n_0 u_0$  in equation (3) we get

$$i = \frac{k V_0 e i}{1 + k V_0 e} \epsilon^{\frac{c(1+w)}{\lambda} + \beta e (V-V_0) - (\gamma + w) \frac{d}{\lambda}};$$

hence we have

$$\beta e(V - V_0) = (\gamma + w) \frac{d}{\lambda} - \frac{c(1+w)}{\lambda} + \log \frac{(1+kV_0e)}{kV_0e} \dots (4),$$

or

$$V = V_{\text{o}} + \frac{1}{\beta e} \log \frac{(1 + k V_{\text{o}} e)}{k V_{\text{o}} e} - \frac{c (1 + w)}{\lambda} \frac{1}{\beta e} + \frac{(\gamma + w)}{\beta e} \frac{d}{\lambda}.$$

This gives us the relation between V the spark potential, d the spark length and  $\lambda$ , which is inversely proportional to the pressure. We see that the relation is a linear one, and since c is proportional to  $\lambda$  we see also that this equation satisfies Paschen's law that V is a function of  $d/\lambda$ .

We shall return to the discussion of this equation after we have considered the case when d the spark length is less than c, i.e. when the anode comes into the Crookes dark space. In this case  $f(Xe\lambda)$  is equal to unity throughout the field, and the energy with which the positive ions strike the cathode is now eV and not  $eV_0$ , where V is the potential difference between the plates. Hence we have

$$\int_0^d \left\{ f(Xe\lambda) - \gamma \right\} \frac{dx}{\lambda} = (1 - \gamma) \frac{d}{\lambda},$$

$$n_0 u_0 e = k (i - n_0 u_0 e) Ve.....(5).$$

and

Hence instead of equation (3) we have

$$i = n_0 u_0 e^{\frac{1}{\epsilon}(1-\gamma)\frac{d}{\lambda}},$$

from which we get

$$\frac{1 + kVe}{kVe} = \epsilon^{(1-\gamma)\frac{d}{\lambda}},$$

or

$$V = \frac{1}{ke} \frac{1}{e^{(1-\gamma)\frac{d}{\lambda}} - 1} \dots (6);$$

from this equation we see that V the spark potential increases very rapidly as  $d/\lambda$  diminishes; we see too that Paschen's law is again obeyed since V is a function of  $d/\lambda$ .

If we combine equations (4) and (6), and represent the result graphically by a curve whose ordinates are proportional to V and abscissae to  $d/\lambda$ , we get a curve similar to that shown in Fig. 109. A reference to the figures given on pages 360—5 will show that except just in the neighbourhood of the minimum spark potential the theoretical curve agrees well with those determined by experi-

ment; we could have anticipated the want of smoothness of the theoretical curve in this region, for here to simplify the calculation

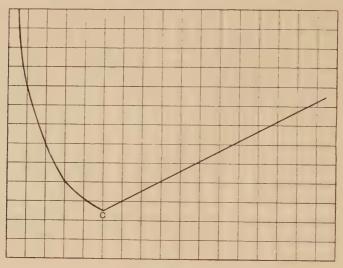


Fig. 109.

we assumed values for  $f(Xe\lambda)$  which were discontinuous at this point.

It is of interest to see what light the theory throws on the questions raised by the experiments. We saw that the measurements made on the spark potential suggest (we can hardly use a stronger term) that the spark potential could be expressed by an equation of the form  $V=k+f\left(\frac{d}{\lambda}\right)$ , where d is the spark length, and  $\lambda$  the mean free path, and f a function which is the same for all gases. Now for sparks whose length is greater than the critical spark length the theory gives  $V=\mathrm{constant}+\frac{(\gamma+w)\,d}{\beta e}\frac{1}{\lambda}$ ; if this is of the form under discussion  $(\gamma+w)/\beta e$  must be independent of the nature of the gas:  $\gamma$  measures the chance of a corpuscle sticking to a molecule against which it strikes, and  $\beta$  and w the chance of a molecule being ionised when struck by a corpuscle moving with a given velocity. We have not any independent measurements of these quantities; we should anticipate that they would depend to some, although probably not to any large extent,

on the nature of the molecule. We saw too (p. 366) that there is considerable evidence that for a given pressure the critical spark length in different gases is proportional to the mean free paths of the molecules: thus if c is the critical spark length when the free path is  $\lambda$ ,  $c/\lambda$  is the same for all gases.

Let us now consider the minimum potential  $V_0$  required to produce a spark; by equations (4) and (6) this is given by the equation

 $V_{\scriptscriptstyle 0} = \frac{1}{ke} (\epsilon^{(1-\gamma)\frac{c}{\lambda}} - 1).$ 

Thus neglecting variations in  $\gamma$  we see that the values of  $V_0$  in different gases are proportional to 1/ke. From equation (5) it follows that 1/ke is the potential difference through which a positive ion must fall in order to acquire such an amount of energy that when it strikes against the cathode it produces the emission of one corpuscle, either from the cathode itself or from a layer of gas next the cathode.

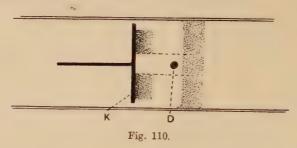
194. This view we have taken of the spark discharge accounts for the 'lag,' i.e. the interval between the application of the electric field and the passage of the spark which, as we have seen, is very noticeable under certain circumstances. For before the spark reaches a steady state there is a preliminary stage during which the number of ions is continually increasing. On the first application of the field the number of ions and the current through the gas is small, but in consequence of the collisions of these ions with the molecules of the gas, the number of ions and the current rapidly increase until finally a steady state is reached: this interval is what we have called the 'lag,' and we see that its duration will be diminished by any agent, such as ultra-violet light shining on the negative electrode, which increases the number of negative ions initially in the gas.

The view that the emission of negative corpuscles from the cathode is due to the impact against it of the positive ions is strongly supported by some experiments made by Schuster\* and Wehnelt† on the effect of placing solid obstacles in the Crookes dark space: these obstacles cast a shadow on the cathode, and

<sup>\*</sup> Schuster, Proc. Roy. Soc. xlvii. p. 557, 1890.

<sup>†</sup> Wehnelt, Wied. Ann. lxvii. p. 421, 1899.

from the region of this shadow there is no emission of cathode rays. This effect is illustrated in Fig. 110, taken from Wehnelt's paper; in this figure D is the obstacle and K the cathode.



Potential difference required to produce very short sparks.

195. Earhart\* has made a series of experiments on the difference of potential required to produce sparks whose length is comparable with the wave-length of sodium light; the electrodes used were steel spheres, and the connection between the spark potential and the distance between the spheres is shown in Fig. 111, in which the abscissae are the spark potential and the ordinates the shortest distance between the spheres. In consequence of the curvature of the electrodes, the least distance between the spheres is not necessarily equal to the spark length; thus when the distance is less than the critical spark length the spark will pass, not across the shortest distance, but across a place where the distance is equal to the critical spark length. Thus Earhart's curves do not show the increase in potential difference with diminishing distance between the electrodes as they would have done if they had been plane: the most interesting feature of the curves is the very rapid diminution in the spark potential when the distance between the electrodes falls to less than about  $3 \times 10^{-4}$  cm.; when the distance is less than this the spark potential falls off rapidly with the distance, and seems from Earhart's results to become directly proportional to the distance. The smallest potential difference actually measured was 32 volts when the distance between the electrodes was  $3 \times 10^{-5}$  cm.: this is only about one-tenth of the minimum spark potential. Earhart made some observations on the effect of pressure; diminution

<sup>\*</sup> Earhart, Phil. Mag. vi. 1, p. 147, 1901.

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of the pressure from three atmospheres to one atmosphere did not seem to affect the discharge potential when the electrodes were

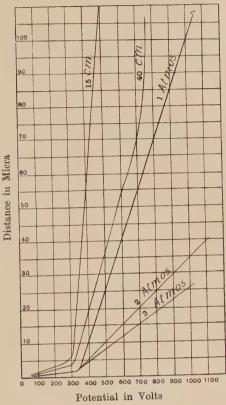


Fig. 111.

very close together; when the pressure was diminished below one atmosphere however the discharge potential also diminished. An inspection of the curves suggests that the character of the discharge changes when the electrodes are brought within a certain distance of each other, or what is equally consistent with the curves, when the average electric intensity, F, between the plates reaches a certain value (about a million volts per cm.): when F has once reached this value Earhart's experiments suggest that the discharge is determined by the condition that F, i.e. V/d, if V is the potential difference and d the distance between the electrodes, should have this value. These experiments raise many

important points, and it is to be hoped that they will be carried much further.

The following considerations seem to afford a possible explanation of the behaviour of the discharge when the electrodes are very close together. We have had occasion before to make use of the hypothesis that in a metal, even at ordinary temperature, free corpuscles are moving about in every direction; if these corpuscles could escape from the metal under ordinary conditions the metal would be unable to retain a charge of negative electricity. Now one of the reasons the corpuscles do not escape is that as soon as they leave the metal there is an electrostatic attraction between the corpuscle and the metal equal to  $e^2/4r^2$ , where e is the charge on the corpuscle and r the distance of the corpuscle from the surface of the metal; this attraction, unless the kinetic energy with which the corpuscle leaves the metal exceeds a certain very high limit, will drag the corpuscle back into the metal. Let us now suppose that an external electric force F acts on the corpuscle, tending to make it move away from the metal; then if Fe is comparable with  $e^2/4r^2$ , the external field will give appreciable assistance to the corpuscle in escaping from the metal, and will enable corpuscles to leave the metal, whose kinetic energy is too small to enable them to escape in the absence of an external field. If Fe is comparable with  $e^2/4r^2$ , F must be comparable with  $e/4r^2$ . Now in electrostatic measure  $e = 3.4 \times 10^{-10}$ , let us put  $r = 10^{-7}$ , then  $e/4r^2 = 8.5 \times 10^3$ . Now in Earhart's experiments F was about  $10^6$  volts per cm., or in electrostatic measure  $3.3 \times 10^3$ ; this is more than one-third of the value of  $e/4r^2$ , so that if, as is quite possible, r is somewhat greater than  $10^{-7}$ , the pull exerted by the external field would be able to drag the corpuscles away from the metal: as soon however as corpuscles can leave the electrode, that electrode will act like a cathode, and a discharge of negative electricity will pass from this to the opposite electrode. If this explanation is correct the discharge across these very small distances is entirely carried by the corpuscles and no part of it by positive ions; in the discharge we have previously considered, corpuscles and positive ions both take a share in carrying the discharge.

Discharge when the electric field is not uniform.

196. Baille\* and Paschen† have made some very interesting experiments on the potential difference required to spark between spheres small enough to make the variations in the strength of the electric field considerable. Baille's results are given in table A, Paschen's in table B:

A. POTENTIAL DIFFERENCES.

Pressure 760 mm., Temp. 15°—20° C.

Spark Length in cms.	Planes	Spheres 6 cm. diam.	Spheres 3 cm. diam.	Spheres 1 cm. diam.	Spheres '6 cm. diam.	Spheres •35 cm. diam.	Spheres ·1 cm. diam.
·05	8.94	8.96	9.18	9.18	9.26	9.30	9.63
·10	14.70	14.78	14.99	15.25	15.53	16.04	16.10
·15	20.20	20.31	20.47	21.28	21.24	21.87	19.58
•20	25.42	25.59	25.95	26.78	26.82	27.13	21.91
'25	30.38	30.99	31.33	32.10	32.33	31.96	23.11
.30	35.35	36.12	36.59	37.32	37.38	36.29	24.12
•35	40.45	41.45	41.47	42.48	42.16	39.39	25.34
•40	45.28	46.34	46.77	47.62	46.34	41.77	26.03
•45	50.48	51.46	51.60	51.56	50.44	43.76	26.62
•40	44.80	45.00	45.00	45.50	44.80	41.07	26.58
.45	49.63	50.33	49.63	52.04	48.42	43.29	28.49
.50	54.35	55.06	54.96	54.66	53.25	47.21	30.00
•60	63.82	65.23	65.23	65.23	59.69	53.75	31.51
•70	74.09	75.40	73.79	72.28	64.22	56.47	32.92
.80	84.83	87.98	84.76	77.61	67.75	58.79	33.82
.90	94.72	97.44	94.62	80.13	70.56	59.09	34.93
1.00	105.49	112.94	104.69	83.05	72.38	59.49	36.24

We see from the tables that with a given spark length between two equal spheres, one charged and insulated and the other put to earth, the potential difference varies with the diameter of the spheres; starting with planes the potential difference at first increases with the curvature and attains a maximum when the sphere has a certain diameter. This critical diameter depends upon the spark length, the shorter the spark the smaller the critical diameter.

<sup>\*</sup> Baille, Annales de Chimie et de Physique [5], xxv. p. 486, 1882.

<sup>+</sup> Paschen, Wied. Ann., xxxvii. p. 79, 1889.

B. SHORT SPARKS.

LONG SPARKS.

Spark Length in cms.	Spheres 1 cm. radius	Spheres •5 cm. radius	Spheres •25 cm. radius	Spark Length in cms.	Spheres 1 cm. radius	Spheres •5 cm. radius	Spheres •25 cm. radius
01 02 03 04 05 06 07 08 09 10 11 12	3·8 5·04 6·62 8·06 9·56 10·81 11·78 13·40 14·39 15·86 16·79 18·28 20·52	3·42 5·18 6·87 8·82 9·75 10·87 12·14 13·59 14·70 15·97 17·08 18·42 20·78	3·61 5·58 6·94 8·43 9·86 11·19 12·29 13·77 14·89 16·26 17·26 18·71 21·26	10 15 20 25 30 35 40 45 50 55 60 70 80 90 100 1.20 1.50	15.96 21.94 27.59 32.96 38.59 43.93 49.17 54.37 59.71 64.60 69.27 78.51 87.76	16 11 22 17 27 78 33 42 39 00 44 32 49 31 54 18 59 03 63 35 67 80 75 04 81 95	16·45 22·59 28·18 33·60 38·65 43·28 47·64 51·56 54·57 57·27 59·95 63·14 66·39 68·65 70·68 74·94 79·42

The results given in these tables show that when the spheres are very small the potential difference required to produce a spark

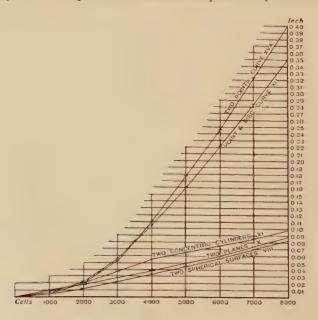


Fig. 112.

of given length is, if the spark is not too short, very much less than the potential required to produce the same length of spark between parallel planes, and that the spark potential difference with points as electrodes only increases slowly with the length of the spark. The effect of the shape of the electrode on the spark length is shown by the curves represented in Fig. 112, which is taken from a paper by De la Rue and Müller\*. The curves give the relation between spark potential and spark length for two planes, two spheres one 3 cm. in radius, the other 1.5 cm. in diameter, two coaxial cylinders, a plane and a point, and two points.

197. Schuster<sup>†</sup> has by the aid of Kirchhoff's solution of the problem of the distribution of electricity over two spheres, calculated from Baille's and Paschen's results the maximum electric intensity in the field before the spark passed: the results for Baille's experiments are given in the following table.

Spark Length in cms.	Planes	Spheres 6 cm. diam.	Spheres 3 cm. diam.	Spheres 1 cm. diam.	Spheres 6 cm. diam.	Spheres •35 cm. diam.	Spheres ·1 cm. diam.
·05 ·10 ·15 ·20 ·25 ·30 ·35 ·40 ·45	179 147 135 127 122 118 116 113	180 149 138 131 127 124 122 122 120	186 153 141 137 134 130 129 129 127	190 163 157 154 154 156 159 164 166	197 176 170 170 180 189 197 204 214	206 198 206 219 236 253 263 272 278	292 376 425 460 478 494 516 528 540
'40 '45 '50 '60 '70 '80 '90 1'00	112 110 109 106 106 106 105 106	118 119 117 116 117 123 120 128	124 122 125 125 126 130 132 133	157 167 166 181 188 192 191 194	197 206 218 233 234 250 255 258	268 275 296 327 339 349 349 349	539 578 608 639 667 685 708 733

It will be seen that the smaller the spheres, i.e. the more irregular the electric field, the greater the maximum electric

<sup>\*</sup> De la Rue and Müller, Phil. Trans. 1878, Pt. 1, p. 55.

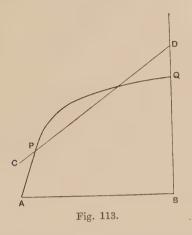
<sup>†</sup> Schuster, Phil. Mag., v. 29, p. 182, 1890.

intensity. We must be careful to distinguish between the electric field before the spark passes and the electric field during the discharge or even during the interval between the application of the potential difference and the passage of the discharge, for during this interval ions are moving about in the field and producing fresh ions; both of these effects will modify the distribution of the electric field. Thus to take an example, suppose we have a negatively electrified point near to a positively electrified plate; if there are no ions in the field the electric force would be a maximum at the point, and would steadily diminish as we approach the plate; if, however, there are ions present in the neighbourhood of the point the negative ions will be repelled from the point, while the positive ions will be pulled into it; this will have the effect of increasing the electric intensity at a distance from the point at the expense of that close to the point: if the negative ions congregate at the plate, so as to form a layer of negative electrification close to the plate, the electric intensity at the plate may rise to very high values. This is what actually occurs, for Mr Blyth has measured at the Cavendish Laboratory the distribution of electric intensity between a point and a plate when the discharge is passing, and has shown that it is large close to the point, is then comparatively small for some distance but becomes large again close to the plate.

The alteration of the electric field during the 'lag' will explain why a spark does not necessarily pass when one or both of the electrodes are small, even although the potential difference between one of the electrodes a and a point in the field P near to A (calculated on the assumption that there are no ions in the field) is greater than that required to produce a spark of length aP between plane electrodes, for during the 'lag' the movement of the ions in the field may have so reduced the potential difference between a and P that it is less than that required to produce a spark of length aP.

Although the processes going on during the lag may reduce the inequalities in the electric field between small electrodes they cannot be expected to remove them entirely, and when the field is far from uniform, as is the case with pointed electrodes, we can easily see that the potential difference required to produce a long spark is less than that required to produce a spark of the same

length between plane electrodes. For let the curve APQ (Fig. 113) represent the distribution of potential between small electrodes AB, and let CD be the curve which represents the potential



difference required to produce a spark in a uniform field (the ordinate of a point on CD represents the spark potential required to produce a spark whose length is equal to the abscissa of the point); then we see that although the potential difference BQ between the small electrodes may be less than BD, that required to produce a spark of length AB in a uniform field, the two curves may intersect; if they do so at P, then a spark will pass from A to P, the whole potential difference will be thrown on the region between P and B, so that the strength of this part of the field will increase and the spark will travel on to B.

198. When the electrodes are of different sizes Faraday\* found that the spark potential is different according as the smaller electrode is positive or negative; De la Rue and Müller† also observed the same effect; according to Wesendonck‡ this difference only occurs when a brush discharge accompanies the spark, when the conditions are such that the discharge passes entirely as a spark the spark potential is the same whichever way the spark passes.

<sup>\*</sup> Faraday, Experimental Researches, § 1480.

<sup>†</sup> De la Rue and Müller, Phil. Trans., 1878, Pt. 1. p. 55.

<sup>‡</sup> Wesendonck, Wied. Ann., xxviii. p. 222.

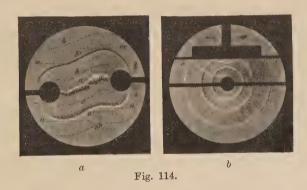
#### Pressure in the Spark.

199. The ions in the electric field acquire kinetic energy and as the pressure in a gas is proportional to the kinetic energy per unit volume the pressure along the path of the spark will be increased. This increase in pressure may be very large; for it is easy to show that the kinetic energy given to the ions, when a quantity of electricity equal to Q passes through the spark, is equal to VQ, where V is the spark potential. To take an example, let us suppose that we have a spark one cm. long through air at atmospheric pressure, and that we discharge by this spark the charge in a condenser of 1000 cm. capacity charged to the potential difference required to produce the spark, this potential difference is about 30000 volts, i.e. 100 in electrostatic units, hence in this case  $V = 10^2$  and  $Q = 10^2 \times 10^3$ , thus the energy given to the gas is 10' ergs. Now if this energy were distributed throughout 1 c.c. of gas it would increase the pressure by 6.6 atmospheres, it is however confined to the very much smaller volume traversed by the spark, the pressure in this region will be proportionately greater; to take  $\frac{1}{100}$  of a c.c. as the volume of gas traversed by the spark would probably be a very large over-estimate, and yet even if the volume were no less than this the initial pressure along the path of the spark would be 660 atmospheres. This high pressure would spread as a pulse from the region of the spark-gap, the pressure in the pulse, when this had got so far from the spark-gap that it might be regarded as spherical, varying inversely as the square of the distance from the sparkgap.

A well-known instance of the effects produced by this pressure is what is called the 'electrical bomb,' where a loosely-fitting plug in a closed vessel is blown out when a spark passes through the vessel. The effect can easily be observed if a pressure-gauge, in which the pressure is indicated by the motion of a small quantity of a light liquid, is attached to an ordinary discharge-tube, the pressure in the gas being most conveniently from 2 to 10 mm. of mercury. At the passage of each spark there is a quick movement of the liquid in the gauge as if it had been struck by a blow coming from the tube; immediately after the passage of the spark

the liquid in the gauge springs back within a short distance of its position of equilibrium and then slowly creeps back the rest of the way. This latter effect is probably due to the slow escape of the heat produced by the passage of the spark, the gauge behaves just as it would if a wave of high pressure rushed through the gas when the spark passed. The increased pressure due to the discharge has been described by Meissner\* and by De la Rue and Müller†.

The existence of a pulse spreading from the spark has been beautifully demonstrated by Töpler<sup>+</sup>, who studied by the method of instantaneous illumination the region round the spark immediately after it had passed. As the density of the air in the pulse differs from that of the surrounding gas, the pulse is optically different from the rest of the field and so can be made visible. Fig. 114 a, taken from Töpler's paper, represents the appearance



of the field looking so as to see the whole length of the spark, Fig. 114 b the appearance when the spark is looked at end-on.

Töpler noticed that the initial disturbance close to the spark gap showed periodic expansions and contractions, as if the regions of greatest disturbance were distributed at equal intervals along the length of the spark. There was an exceptionally large protuberance in the neighbourhood of the cathode.

<sup>\*</sup> Meissner, Abhand. der könig. Gesellschaft Göttingen, xvi. p. 98, 1871.

<sup>†</sup> De la Rue and Müller, Phil. Trans., 1880, p. 86.

<sup>‡</sup> Töpler, Pogg. Ann., exxxi. pp. 33, 180, 1867; exxxiv. p. 194, 1868.

In an experiment due to Hertz which also illustrates well the explosive effects due to the spark the explosion seemed to be more vigorous at the anode than at the cathode\*; in this experiment the anode was placed at the bottom of a glass tube with a narrow mouth, while the cathode was placed outside the tube and close to the open end. The tube and the electrodes were in a bell-jar filled with dry air at a pressure of 40—50 mm. of mercury. When the discharge from a Leyden jar charged by an induction coil passed through the tube, the glow accompanying the discharge was blown out of the tube and extended several centimetres from the open end; the effect was not so marked when the electrodes were reversed.

Haschek and Mache+ by measuring the pressure at the surface of a vessel through which sparks from a high tension transformer were passing have calculated the pressure in the spark; with brass electrodes and sparks 3 mm. long they estimated the pressure of the spark in air at a pressure of 704 mm. of mercury as 51.7 atmospheres, in carbonic acid at the same pressure 52.2 atmospheres, and in coal gas as 72.7 atmospheres; they found that the pressure in the spark was, as might be expected from the diminution in the spark potential, less when the pressure of the gas through which the spark passed was low than when it was high: thus in one of their experiments the pressure in the spark was estimated by them to be 27.2 atmospheres when the pressure of the air was 585 mm. of mercury, when the air pressure was reduced to 96 mm. of mercury the spark pressure fell to one atmosphere. They found too that the spark pressure depended upon the nature of the electrodes; thus under similar conditions they found that the spark pressures in air with electrodes of carbon, iron and brass were respectively 124, 79, 64 atmospheres. When as in these experiments sparks follow each other in rapid succession, the spark is carried to a considerable extent by the metallic vapour from the electrode.

Haschek and Exner<sup>\*</sup>, and Mohler<sup>§</sup> have published estimates of the spark pressure derived from observations of the displacement

<sup>\*</sup> Hertz, Wied. Ann., xix. p. 87, 1893.

<sup>+</sup> Haschek and Mache, Wied. Ann., lxviii. p. 740, 1899.

<sup>‡</sup> Haschek and Exner, Wien. Sitzungs., evi. p. 1127, 1897. § Mohler, Astrophysical Journal, iv. p. 175, 1896.

of the lines in the spectrum of the spark due to the electrode. Humphreys\* has shown that the effect of increased pressure in the vapour of a metal is to displace the lines towards the red end of the spectrum, and has measured the displacement for various pressures; hence if we assume that the displacement of the lines in the spark spectrum is due to the pressure of the spark, if we measure this displacement we can deduce the pressure in the spark.

The magnitude of the pressures in the spark explains the mechanical effects produced by sparks, such as the perforation of pieces of cardboard or thin plates of glass.

### Heating Effects produced by Sparks.

200. A large part of the energy given to the ions during the discharge will appear as heat and will raise the temperature of the gas and the vessel in which it is contained. Measurements of the heat produced by sparks have been made by Riess+, Paalzow+, G. Wiedemanns, Naccari and Bellati|, Poggendorff¶, Dewar\*\*, Rollmann††, Naccari‡, Villari§, Mugna||: measurements in absolute measure have been made by Heydwiller ¶¶ and Kauffmann \*\*\*. These experiments have mostly been made on the heat developed by the sparks produced by discharging Leyden jars; the most definite result obtained is that the heat produced in the spark gap is only a small fraction of the energy in the jar before it was discharged. The discharge of the jar is oscillatory, so that in this case we have a series of sparks following one another across the gap in quick succession; under these circumstances there is a great tendency for the spark to change into an arc, and in the arc the potential difference

- \* Humphreys, Astrophysical Journal, vi. p. 169, 1897.
- † Riess, Reibungselektricität.
- ‡ Paalzow, Pogg. Ann., exxvii. p. 126, 1866.
- § G. Wiedemann, Pogg. Ann., clviii. p. 35, 1876.
- || Naccari and Bellati, Beib., ii. p. 720, 1878.
- ¶ Poggendorff, Pogg. Ann., xeiv. p. 632, 1855.
- \*\* Dewar, Proc. Roy. Soc. Edin., vii. p. 699, 1872.
- † Rollmann, Pogg. Ann., exxxiv. p. 605, 1868.
- ‡‡ Naccari, Att. di Torino, xvii. p. 1, 1882.
- §§ Villari, Beib., iii. p. 713; iv. p. 404; v. p. 460; vi. p. 699; vii. p. 782.
- IIII Mugna, Beib., vi. p. 953.
- ¶¶ Heydwiller, Wied. Ann., xliii. p. 310, 1891; lxi. p. 541, 1897.
- \*\*\* Kauffmann, Wied. Ann., lx. p. 653, 1897.

between the electrodes, and therefore the heat produced by a given current, is very much less than for the spark. The relation between the electromotive force and the current in the case of the discharge through gases is in general so different from that for metals that it is somewhat misleading to speak of the resistance of the spark gap: it may, however, give some idea of the small amount of energy dissipated in the spark gap to say that the heating effect for sparks six millimetres long has been found in some cases investigated by Miss Brooks\* to be not greater than that which would have occurred if a wire about 2 ohms resistance occupied the position of the spark.

201. Schuster and Hemsalech† have made some very interesting researches on the constitution of sparks following rapidly one after another, such as are produced by the oscillatory discharge of a Leyden jar. The sparks were photographed on a rapidly moving film mounted on the rim of a wheel making about 30 revolutions per second, the motion of the film was at right angles to the length of the spark, so that the line traced on the film by a source of light moving with finite velocity along the spark length would be inclined to the direction of the spark, and its inclination would (if the velocity of the film were known) give the velocity of the source of light. By sending the light from the spark on its way to the film through a spectroscope the velocity corresponding to any line in the spectrum could be determined.

The conclusion arrived at by the authors from these experiments is that the first spark passes through air, but that if the sparks follow each other in rapid succession (as they do when produced by the oscillatory discharge of a Leyden jar) and are not too long the succeeding ones pass through the vapour of metal, the electrodes being vaporised by the heat produced by the first spark. This view is confirmed by a very interesting experiment made by the authors: they found that if self-induction was put into the spark circuit by which the jars were discharged the air lines almost disappeared from the spectrum of the spark while the metal lines were very bright: the self-induction increases the time the oscillations last and so enables the vapour of the metal to get well diffused

<sup>\*</sup> Miss Brooks, Phil. Mag., vi. 2, p. 92, 1901.

<sup>+</sup> Schuster and Hemsalech, Phil Trans. 1899, vol. exciii. p. 189.

through the spark gap, the discharge passing for by far the greater part of the time through the vapour so that most of the energy is spent in heating this and not the air.

The authors found that the velocity of the metallic vapours in the spark was greater for the metals of low atomic weight than for those of high; thus the velocity of aluminum vapour was 1890 metres per second, that of zinc and cadmium only about 545.

The very interesting result was obtained that the velocities of the vapours of some metals and especially of bismuth indicated by some of the lines in the spectrum were not the same as those indicated by other lines, thus in bismuth some of the lines indicated a velocity of 1420 metres per second, others a velocity of only about 550, while one line  $(\lambda = 3793)$  gave a still smaller velocity. This result raises some very interesting questions, as for instance whether bismuth is a mixture of different elements, some of the lines in the spectrum being due to one constituent, others to the other constituents; another possibility is that the molecules even of an element are not all of the same kind, and that the different lines in the spectrum are emitted by molecules of different kinds; we should also get a similar effect if the relative intensities of the lines varied greatly with the kinetic energy possessed by a molecule, if for example the intensity of a line α was very much greater than that of a line  $\beta$ , for a rapidly moving molecule, and very much less for a slowly moving one, then, if the molecules of the vapour were projected with different velocities, the line  $\alpha$  would indicate a higher velocity than  $\beta$ ; on these points Schuster and Hemsalech reserve their opinion until they have made further experiments.

# Effect of a Magnetic Field on the Spark.

202. We shall see later on that a magnetic field produces a very great effect on the discharge through gases when the pressure is low. At atmospheric pressure, however, the effects on the spark itself are very slight, although the halo of luminous gas which surrounds the course of the sparks when a number of sparks follow each other in rapid succession is drawn out into a broad band by the magnetic field. This halo, it may be observed, is deflected by a current of air though the spark itself is not affected.

Precht\* has observed a distinct effect of a magnet on a spark at atmospheric pressure when the sparks pass between a sharp point and a blunt wire; the spark is deflected by a transverse magnetic field in the same direction as a flexible wire conveying a current in the same direction as that passing through a spark would be deflected. He found, too, that the magnetic field affected the spark potential; thus when the distance between the electrodes was 8 mm. and the transverse magnetic force 7017 he found that when the pointed electrode was the anode, the rounded one the cathode, the magnetic field reduced the spark potential from 8670 volts to 7520 volts, while when the point was cathode, the rounded electrode anode the same magnetic field increased the potential from 6250 to 6450 volts.

#### Appearance of Long Sparks.

203. When sparks are of considerable length they exhibit a branched appearance, as shown in Fig. 115, the branches pointing

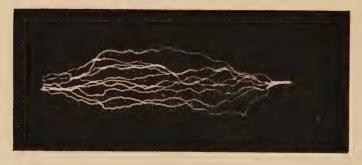


Fig. 115.

to the negative electrode; the electricity flowing along those branches which terminate abruptly must ultimately find its way to the electrodes by a dark discharge. The appearance of the spark is different at the positive and negative terminals, there is a single straight stem at the positive, while at the negative the discharge is divided into several threads. The spark along its course exhibits abrupt changes in direction as if it made its way by a series of jumps rather than as an uninterrupted stream.

<sup>\*</sup> Precht, Wied. Ann., lxvi. p. 676, 1896.

#### Discharge of Electricity from Points.

204. A very interesting case of electric discharge is that between a sharply pointed electrode, such as a needle, and a neighbouring metallic electrode of considerable area. In this case the luminosity is confined at atmospheric pressure to the neighbourhood of the electrode, the current through the rest of the gas is carried almost entirely by ions of the same sign as the charge on the point.

Chattock (see page 53) has shown that the velocity of these ions under unit electric force is the same as that of the ions produced by Röntgen or Becquerel rays, and Townsend (see page 29) has shown that the charge on the ions is also the same. If the point is placed at right angles to a large metal plane, then for electricity to stream from the point the potential of the point must exceed that of the plane by an amount called by v. Röntgen\* the minimum potential; this minimum potential depends upon the sharpness of the point, the pressure and nature of the gas and the sign of the electrification of the point, being less if the point is negatively than if it is positively electrified; according to Warburg+, the minimum potential does not depend upon the distance of the point from the plane. When the potential difference between the point and the plane exceeds the 'minimum potential' a current of electricity passes from the point to the plane; the magnitude of this current for a given potential difference between the point and the plane rapidly diminishes as the distance from the plane increases: Warburg (l.c.) has shown that if d is the shortest distance between the point and the plane, then for a given difference of potential the current is proportional to  $1/d^{3\cdot17}$ , this law holds whatever be the sharpness of the point.

## Value of the Minimum Potential.

205. As this depends upon the sharpness of the point we can only compare the values of this quantity for the same point under different circumstances. The following table gives the value for

<sup>\*</sup> v. Röntgen, Göttingen. Nach. p. 390, 1878.

<sup>+</sup> Warburg, Wied. Ann., lxvii. p. 69, 1899.

the minimum potential with the same point at different pressures as determined by Tamm\*:

Pressure in cm. of mercury	Point -	Point +					
76	2140 volts	3760 volts					
70	2135 ,,	3755 ,,					
60	2105 ,,	3705 ,,					
50	2035 ,,	3585 ,,					
40	1905 ,,	3350 ,,					
30	1690 ,,	2970 ,,					
20	1360 ,,	2390 ",					
10	910 ,,	1580 "					

Thus the change in the minimum potential with the pressure is very slow when the pressures are high but becomes much faster at lower pressures.

The ratio of the minimum potential for positive and negative points is approximately the same at all pressures. Observations of the minimum potential in different gases have been made by v. Röntgen† and by Precht‡; the results of their observations are given in the following table, the numbers in the first two columns are due to v. Röntgen, those in the third and fourth to Precht.

Gas	Minimum pote	ential, point +	Minimum poter	ntial, pressure
	Pressure 205 mm.	Pressure 110 mm.	Point +	Point -
$egin{array}{cccccccccccccccccccccccccccccccccccc$	1296 volts 2402 ,, 2634 ,, 2777 ,, 3188 ,, 3287 ,,	1174 volts 1975 ,, 2100 ,, 2317 ,, 2543 ,, 2655 ,,	2125 volts 2800 " 3475 " 2600 " 2750 "	1550 volts 2350 ,, 2100 ,, 2000 ,, 2050 ,,

<sup>\*</sup> Tamm, Drude's Ann., vi. p. 259, 1901.

<sup>+</sup> v. Röntgen, Göttingen. Nach., 1878, p. 390.

<sup>‡</sup> Precht, Wied. Ann., xlix. p. 150, 1893.

#### Connection between Potential Difference and Current.

**206.** Warburg (l.c.) found that using the same point and keeping it at the same distance from the plate the relation between the current i and the potential V can be expressed by the relation

$$i = aV(V - M),$$

where M is the minimum potential. Sieveking\* considered that the linear relation  $i = b \ (V - M)$  represented his experiments with sufficient accuracy: in a recent paper by Tamm† this question is discussed, and a formula of the type of Warburg shown to give better agreement: in place of the minimum potential M Tamm writes  $\frac{1}{2} \ (M_1 + M_2)$  where  $M_1$  is the potential at which the discharge begins when the potential is gradually increased,  $M_2$  that at which it leaves off when it is gradually lowered, the two are not identical the latter being the smaller: the application of the formula in this form is limited to potential differences considerably greater than M.

The current with the same potential difference increases as the pressure diminishes, this is shown by the following results due to Tamm (l. c.). (See Tables, p. 402.)

It will be noticed that the current with the point positive is always less than that with the point negative, the potential difference being the same in the two cases. The increase of the current as the pressure diminishes is more rapid at small pressures than at high pressures; the current seems to be roughly proportional to the reciprocal of the pressure, while at low pressures it varies as the square of this quantity.

Tamm gives as the relation between  $i_x$  the current at a pressure of x centimetres, and  $i_{76}$  the current at 76 cm. pressure, the potential difference being V in both cases, the empirical equation

$$i_x = i_{76} \left\{ \frac{76}{x} - \sqrt[3]{\frac{V}{10^5}} \log \frac{76}{x} \right\}^2.$$

<sup>\*</sup> Sieveking, *Drude's Ann.*, i. p. 299, 1900. † Tamm, *Drude's Ann.*, vi. p. 259, 1901.

~ .			
Current	2.77	macro-	amneres.
0.00, 10,00	0,0	,,,,,,,,,	omporto.

Potential difference Pressure	- 4000	- 6000	-8000	-10000
76	1·4	4·2	8·0	13·4
70	1·6	4·6	8·6	14·5
60	2·0	5·7	10·5	17·6
50	2·6	7·8	13·7	22·8
40	3·7	11·3	20·4	33·7
30	6·8	19·5	35·3	58·0
20	14·6	44·7	80·9	134·2

Potential difference Pressure in cm. of Hg.	+4000	+6000	+8000	+10000
76	0.7	2·1	4·8	9·3
70	0.8	2·3	5·1	10·1
60	1.0	2·8	6·3	12·3
50	1.3	3·8	8·2	16·0
40	1.9	5·6	12·3	23·5
30	3.3	9·7	21·1	40·4
20	7.3	22·4	48·0	93·0

207. Warburg\* has shown that the presence of minute traces of oxygen in gases such as hydrogen or nitrogen produces a great diminution in the current from a negative point while it has but little effect on that from a positive one; thus the removal of a trace of oxygen from nitrogen increased the current from a negative point in that gas fifty times; this may be taken as indicating that oxygen has a great tendency to collect round the carriers of the negative charge and either make them less efficient as ionisers or else make them move more slowly in the electric field.

**208.** Warburg<sup>†</sup> has investigated the proportion of current received at different portions of the plane opposite the electrified point; he finds that the amount received per unit area at a point Q on the plane is proportional to  $\cos^m \theta$  where  $\theta$  is the angle QPO, P being the electrified point and O the normal from P on the

<sup>\*</sup> Warburg, Drude's Ann., ii. p. 295, 1900.

<sup>+</sup> Warburg, Wied. Ann., lxvii. p. 69, 1899.

plane, the electrified conductor is supposed to be at right angles to the plane; he finds that m for a negatively electrified point is equal to 4.65, for a positively electrified point 4.82, and that it is independent of the sharpness of the point.

#### The Electrical Wind.

209. The current of electrified ions which constitutes the discharge from the point sets the air in the neighbourhood in motion. For when the ions have settled down into the state in which their velocity is proportional to the electric force acting upon them the mechanical force acting upon them is transferred to the air through which they are moving, this gives rise to currents of air directed from the point, and these air currents are what is known as the electrical wind. This motion of the air forwards is accompanied by a reaction on the point, tending to drive it backwards. This reaction has been measured by Arrhenius\*, who finds that when positive electricity is escaping from a point into air the reaction tending to drive the point backwards is, when the current is kept constant, proportional to the pressure of the gas, and for different gases at the same pressure (air, hydrogen, and carbonic acid) varies as the square root of the molecular weight of the gas. The reaction when an equal current of negative electricity is escaping from the point is much less, the proportion between the two depending on the pressure of the gas; thus in air at a pressure of 70 cm. the reaction on the positive point was 1.9 times that of the negative, at 40 cm. 2.6 times, at 20 cm. 3.2 times, at 10.3 cm. 7 times, and at 5.1 cm. 15 times the reaction of the negative point. The reaction on the discharging point is due to the repulsion between the electrified point and the ions carrying the discharge; we can easily calculate this force. Suppose that the needle from which the electricity is discharged points in the direction of the axis of z; let  $\rho$  be the density of the ions at any part of the field, Z the electric force at the same point, then F, the force parallel to z acting on the ions, is equal to

#### $\iiint Z \rho dx dy dz$ ;

but if w is the velocity of the ion parallel to z, w = kZ where k is

<sup>\*</sup> Arrhenius, Wied. Ann., lxiii. p. 305, 1897.

the velocity of the ion under unit electric force; substituting this value for Z we get

$$F = \iiint \frac{w}{k} \rho dx dy dz;$$

but if i is the current

$$i = \iint w \rho dx dy$$
,

hence if k is constant throughout the field

$$F = \frac{i}{k} \int dz \qquad (1).$$

The reaction on the point is equal to F, hence for a constant current F varies inversely as k; this conclusion agrees when the point is positively electrified with the results of Arrhenius's experiments. For let us first consider the effects of pressure, k varies inversely as the pressure; hence F should be directly proportional to the pressure, this is in agreement with Arrhenius's result; next consider the reaction of different gases, if we refer to the values given on page 56, we see that the velocities of the ions under unit electric force are roughly inversely proportional to the square roots of the densities of the gases, hence F should be approximately directly proportional to the square roots of these densities. Since the velocity of the negative ion is greater than that of the positive the reaction on the negative point should be less than that on the positive; the ratio of the reaction on the positive point to that on the negative is however much greater than the ratio of the velocity of the negative ion to that of the positive. We have seen however reasons for believing that a rapid condensation of the gas takes place around the newly-formed negative ions after they are produced at the point, so that the velocity of the negative ion will be greater at first than after it has been for some time in the gas, it is only however for these aged ions that we know the velocity, while in the case of the point discharge a large part of the reaction will be due to the more rapidly moving freshly-formed ions in the immediate neighbourhood of the point, so that the value of F will be less than that determined by equation (1) when we substitute for k the observed velocity of the negative ion.

Discharge from a point whose electrification is rapidly changing sign.

- 210. If a point is charged up to a high and rapidly alternating potential, such as can be produced by the electrical oscillations started when a Leyden-jar is discharged, then in hydrogen, nitrogen, ammonia, and carbonic acid gas, a conductor placed near the point gets a negative, while in air and oxygen it gets a positive charge\*. Himstedt+ has shown that the distribution of electrification in these gases differs only in degree; he finds that in air and oxygen, although the electrification is positive near the point, yet it changes sign as we recede from it and ultimately becomes negative; while in hydrogen and the other gases mentioned above we get positive electrification if we go close up to the point; the difference between the gases is that in air the place where the electrification changes sign is some distance from the point, while in hydrogen it is close up to it. This outer zone of negative electrification is what we should expect from the greater velocity of the negative ions, for under an alternating electric field the amplitude of the path of the faster ions would be greater than that of the slower, and thus at a distance from the point greater than the amplitude of the slower ions there would be nothing but negative electricity. The determination of the distance at which the electrification changes sign would be a very complicated investigation, as it would involve in addition to the relative velocities of the positive and negative ions the difference in the values of the current proceeding from the point according as it is positively or negatively electrified, as well as the difference in the minimum potential at which the discharge begins.
- 211. The condition of a point from which electricity is discharging seems to suffer some modification as the discharge goes on, and this gives rise to variations in the current: Precht‡ found that a point from which positive electricity had been discharged sometimes got hollowed out into a kind of crater, as if some of the metal had been torn away; he found that a negatively electrified point did not suffer any change of shape.

<sup>\*</sup> Harvey and Hird, Phil. Mag. [5], xxxvi. p. 45, 1893. Himstedt, Wied. Ann., lii. p. 473, 1894. J. J. Thomson, Phil. Mag. [5], xl. p. 511, 1895.

<sup>†</sup> Himstedt, Wied. Ann., lxviii. p. 294, 1899.

<sup>‡</sup> Precht, Wied. Ann., xlix. p. 50, 1893.

#### Theory of the discharge from fine points.

212. We may suppose that the escape of electricity from a sharp point occurs in the following way. When the electric field at the point reaches a certain intensity a short spark passes from the point to the air a little distance away, along the path of this spark ions are produced, positive as well as negative; if the point is positively electrified the positive ions are driven out from this region into the surrounding gas and under the influence of the electric field find their way to the metal plate to which the point is discharging; if the point is negatively electrified it is the negative ions which are driven to the plate, and which carry the electricity which is discharging from the point.

Let us apply these considerations to explain some of the features of the discharge. We shall first consider the strength of the field required to produce the small spark from the point.

The relation between the potential difference required to produce a spark and the spark length is (see page 360) represented by a curve similar to  $\alpha$ , Fig. 116, where the ordinates represent the

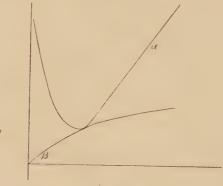


Fig. 116.

spark potential and the abscissae the spark length. Let us suppose that the point is equivalent in its electrical effect to a small sphere of radius a; thus if V is the potential of the sphere the potential difference between the sphere and a point at a distance x

from its surface is  $V \frac{x}{a+x}$ ; let the equation to the curve  $\beta$ 

(Fig. 116) be  $y = V \frac{x}{a+x}$ , then if the curve  $\beta$  intersects the curve  $\alpha$  a spark will pass from the point, if the curves do not intersect no spark will pass, the smallest value of V which will produce a spark is when the corresponding curve  $\beta$  just touches the curve  $\alpha$ . Now when  $\alpha$  is very small dy/dx for  $\beta$  is very small compared with y/x, but for the curve  $\alpha$  it is only in the neighbourhood of the minimum spark potential that this is the case, hence we conclude that when  $\beta$  touches  $\alpha$  it does so close to A, the point corresponding to critical spark  $x_0$  and to  $V_0$  the minimum potential difference required to produce a spark, hence we have approximately

$$V\frac{x_0}{a+x_0}=V_0,$$

$$V = \left(1 + \frac{a}{x_0}\right) V_0.$$

 $V_{\rm o}$  here is the value of the minimum potential required to produce a spark; we see that V diminishes as a diminishes, i.e. the sharper the point the smaller the discharge potential, it also diminishes as the critical spark length increases, and as the critical spark length is greater at low pressures than at high the minimum potential will diminish as the pressure diminishes. In consequence of the conductivity of the gas round the point, the radius of the sphere taken as equivalent in its electrical action to the point may be considerably larger than the actual radius of the point, and the proportions between these quantities may depend upon the pressure of the gas.

# Difference between the minimum potential for positive and negative points.

The minimum potential required for the discharge of positive electricity from a point is greater than that for negative: this is, I think, consistent with the preceding view, for the minimum potential difference  $V_0$  depends (1) upon the energy a corpuscle must possess to ionise a molecule against which it strikes, (2) upon the energy a positive ion must possess in order to make the cathode against which it strikes emit negative corpuscles; an increase in either of these quantities would be attended by an increase in the minimum spark potential. Now when the

discharging point is negatively electrified the conditions are the same as in the ordinary spark discharge, for there is a metallic cathode for the positive ions to strike against; when however the point is positively electrified, the cathode consists of the molecules of the gas, and it is very probable that a positive ion would require greater energy to detach a corpuscle from a molecule of a gas than from a piece of metal which we have reason to think is very easily ionised, this would have the effect of making  $V_0$  for the positive point greater than for the negative and thus making the minimum potential required for point discharge greater.

Relation between the current from a point and the potential difference between the point and the plane to which it discharges.

In order to simplify the mathematical analysis we shall take a case which, while presenting the same physical features as the point discharge from a needle, is yet from its symmetry more amenable to calculation, the case is that of the discharge from a very fine wire discharging to a coaxial cylinder. Almy\* has made a series of experiments on this kind of discharge. Let us take a point on the wire as the origin for polar coordinates and let r be the distance of a point in the gas from the wire, R the electric force at this point and  $\rho$  the density of the electrification, then we have

$$\frac{d}{dr}(Rr) = 4\pi\rho r \dots (1).$$

When we get beyond the region of the spark the discharge will be carried by ions of one sign, hence if  $\iota$  is the current per unit length of the wire, u the velocity of the ions, we have

$$\iota = 2\pi r u \rho$$
;

but u = kR, where k is the velocity of the ion under unit force, hence we have from equation (1)

$$\frac{d}{dr}(Rr) = \frac{2\iota}{kR} \; ;$$

integrating this equation, we get

$$(Rr)^2 = \frac{2\iota}{k} r^2 + C....(2),$$

where C is a constant. To determine C, let a be the smallest

<sup>\*</sup> Almy, American Journal of Science [4], xii. p. 175, 1902.

value of r, for which the ions are all of one sign (a will exceed the radius of the wire by a quantity of the order of the minimum spark length); when r=a, R will be comparable with the electric force required to produce a spark; thus R will at atmospheric pressure be greater than  $10^2$  in electrostatic units: in these units k for air at this pressure is 450, hence unless  $\iota$  were comparable with the value  $2\times 10^6$  in electrostatic measure, i.e. with  $\frac{2}{3}\times 10^{-3}$  ampères, which is much larger than the currents used by observers of the spark discharge,  $(2\iota/k)\,a^2$  will be small compared with  $(Ra)^2$ , i.e. C will be approximately independent of the current, and at the surface of the wire C will be large compared with  $\frac{2\iota}{k}\,r^2$ .

At the surface of the cylinder, on the other hand, in general,  $2\iota r^2/k$  will be large compared with C, for suppose the radius of the cylinder were  $10^3$  times that of the wire, then a current of a few microcoulombs per second (which is of the order of the currents made by Tamm in his experiments) would make  $2\iota r^2/k$  at the surface of the cylinder very large compared with  $(Ra)^2$  and therefore with C.

If V is the potential at the distance r from the wire, we have from (2)

 $\frac{dV}{dr} = \frac{1}{r} \left\{ \frac{2\iota}{\bar{k}} r^2 + C \right\}^{\frac{1}{2}};$ 

integrating this equation we find, if V' is the potential difference between the cylinder and the point near the wire where the current begins to be carried by ions of one sign, and b is the radius of the cylinder,

$$V' = \left\{ \frac{2\iota}{k} b^2 + C \right\}^{\frac{1}{2}} - \left\{ \frac{2\iota}{k} a^2 + C \right\}^{\frac{1}{2}} + \frac{1}{2} \sqrt{C} \log \frac{\left\{ \frac{2\iota}{k} b^2 + C \right\}^{\frac{1}{2}} - C^{\frac{1}{2}}}{\left\{ \frac{2\iota}{k} b^2 + C \right\}^{\frac{1}{2}} + C^{\frac{1}{2}}}$$
$$- \frac{1}{2} \sqrt{C} \log \frac{\left\{ \frac{2\iota}{k} a^2 + C \right\}^{\frac{1}{2}} - C^{\frac{1}{2}}}{\left\{ \frac{2\iota}{k} a^2 + C \right\}^{\frac{1}{2}} + C^{\frac{1}{2}}},$$

where  $\iota$  is so large that  $2\iota b^2/k$  is large compared with C, this becomes approximately,

$$V' = \left(\frac{2\iota}{k} b^2\right)^{\frac{1}{2}} + \frac{1}{2}\sqrt{C}\log\frac{2C}{\iota};$$

the second term on the right-hand side varies very slowly with  $\iota$ , treating it as a constant and writing  $\alpha$  for this term, we get

if V is the potential difference between the wire and the cylinder we have seen that  $V=V'+V_0$  where  $V_0$  is the least potential that can produce a spark (for air it is about 351 volts), thus we have from (1)

$$\iota = \frac{k}{2b^2} (V - V_0 - \alpha)^2 \dots (2),$$

so that for large values of V,  $\iota$  varies as  $V^2$ ; thus the current varies as the square of the potential difference. Almy\* found that the current was proportional to  $V(V-\beta)$ , thus for values of V large compared with  $\beta$  it is proportional to  $V^2$ ; according to Almy's experiments the current is more nearly proportional to the inverse cube of the radius of the cylinder than to the inverse square as indicated by equation (2); it is to be noted that any want of symmetry in the apparatus which would make the discharge tend to concentrate on a particular radius would make the current vary more rapidly with the radius than if the discharge were quite symmetrical. We see from equation (2) that the current varies as k, the velocity of the ion under unit force, thus since the negative ion moves faster than the positive, the discharge under given potential should be greater when the point is negative than when it is positive; from Tamm's observations the ratio of the negative current to the positive in air at atmospheric pressure is equal to 1.44, this is not far from the ratio of the velocities of the negative and positive ions for dry air.

Again, since  $\iota$  is proportional to k, and k is inversely proportional to the pressure, the current should vary inversely as the pressure when the potential difference is large; a reference to the table on page 402 will show that although this is approximately true at high pressures it ceases to be an approximation to the truth when the pressure is low, when the current varies more nearly as the inverse square of the pressure. At low pressures and with large currents the discharge is accompanied by luminosity right up to the plate; an example of this is shown in Fig. 117, taken

<sup>\*</sup> Almy, American Journal of Science [4] xii. p. 175, 1902.

from a paper by v. Obermayer\*: the appearance presented by the discharge suggests that ionisation is taking place at the plate as well as at the point, in which case ions of both signs would be present between the plate and the point, and our investigation

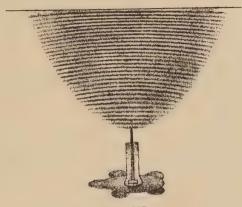


Fig. 117.

which is founded on the supposition that the current is carried entirely by ions of one sign would not apply. Even at atmospheric pressure there is evidence in some cases of the presence of ions of opposite sign to that of the electrification of the discharging point: thus C. T. R. Wilson + notices a case in which when a positive point was discharging into his expansion apparatus (see p. 136) an expansion which was sufficient to bring down negative but not positive ions produced a cloud, showing that negative ions were present.

We shall see that from a spark rays are given out (Entladungstrahlen) which can ionise a gas; some rays are thus given out from the small spark at the end of the discharging point, and these rays may in certain cases produce appreciable ionisation at a considerable distance from the point. The discharge from a point seems to possess very considerable actinic power ...

Earhart's experiments (p. 384) seem to indicate that when the electric force reaches a certain very high value the ions can come from the metal, it would be interesting to further test this view by seeing if a moderate potential was able to produce a discharge from an exceedingly fine point in a good vacuum.

<sup>\*</sup> v. Obermayer, Wien. Sitzungsberichte, c. p. 127, 1891.

<sup>†</sup> C. T. R. Wilson, Phil. Trans. A. vol. excii. p. 403, 1899.

<sup>‡</sup> Cook, Phil. Mag. [5], xlvii. p. 40, 1899. Leduc, Éclair. Électr. xxi. p. 144, 1899.

Table I. Air. (Carr.)

1786
1.02.

Table II. Air. (Carr.)

h=10 mm.	Spark Potential in Volts	831 645 504 504 420 372 348 351 353 377 425 504 605 1020 1315 1730
Spark Length=10 mm	Product of Pressure and Spark Length	70.9 41.2 23.9 13.9 9.82 9.82 9.62 2.53 2.53 1.58 1.25 1.05
th=5 mm.	Spark Potential in Volts	600 504 418 418 358 352 370 370 388 427 427 705 705 1223 1774
Spark Length=5 mm.	Product of Pressure and Spark Length	36.7 23.0 14.7 14.7 9.25 6.70 6.70 6.70 8.03 2.58 2.58 1.87 1.16 1.38 1.16
th=3 mm.	Spark Potential in Volts	1480 1275 1015 790 630 630 536 452 405 371 361 361 375 397 441 494 494 1395 1395 1786
Spark Length=3 mm.	Product of Pressure and Spark Length	153 1245 945 6442 6442 422 179 179 175 667 753 667 753 825 825 8218 8218 8218 1123 1123
h=2 mm.	Spark Potential in Volts	620 455 400 373 371 389 419 460 534 654 654 826 1042 11312 1695 1829
Spark Length = 2 mm.	Product of Pressure and Spark Length	40 26.4 11.0 8.22 6.32 5.42 4.64 4.04 4.04 3.50 3.04 3.04 1.71 1.50 1.28 1.09
h=1 mm.	Spark Potential in Volts	1510 1265 1025 784 634 634 477 477 417 357 352 352 352 352 354 352 352 352 352 352 368 368 368 368 368 368 368 368 368 368
Spark Length=1 mm.	Product of Pressure and Spark Length	150 120 90 90 61 40.8 21.6 19.4 12.4 7.77 7.77 7.77 7.77 7.77 7.77 7.77 7

Table III. Carbon Dioxide. (Cair.)

			-		_	_															
th=10 mm.	Spark Potential in Volts	993	2002	656	553	473	428	423	440	410	563	630	761	973	1919	1550	1790	1/90			
Spark Length=10 mm.	Product of Pressure and Spark Length	72.7	42.6	24:3	14.4	09.8	6.12	5.10	2.40	04.6	2.30	1.96	1.62	1.34	1.11	.946	608.	760			
th=5 mm.	Spark Potential in Volts	790	674	579	498	438	423	421	420	464	495	533	599	704	820	696	1159	1373	1663	1770	
Spark Length=5 mm.	Product of Pressure and Spark Length	45.5	28.8	18.2	11.6	7.25	6.25	0.50	000 cc	3.30	2.86	2.46	2.09	1.80	1.55	1.33	1.16	86:	.845	-820	
th=3 mm.	Spark Potential in Volts	674	563	477	127	420	419	430	449	487	542	599	669	815	971	1162	1445	1756			
Spark Length=3 mm.	Product of Pressure and Spark Length	26.2	16.7	9.01	0.10	0.70	4.03	3.60	3.06	2.62	2.57	1.95	1.67	1.44	1.26	1.08	.942	.855			
th=2 mm.	Spark Potential in Volts	802	645	918	404	403	450	419	420	427	443	473	525	605	20%	847	1026	1258	1574	1762	
Spark Length=2 mm.	Product of Pressure and Spark Length	42.6	27.0	10:0	8.01	60.09	5.90	5.04	4.30	3.68	3.16	89.7	7.37	96. T	60.1	1.45	1.25	1.07	-910	.842	
th=1 mm.	Spark Potential in Volts	516	460	195	191	419	420	427	443	475	503	666	550	703	310	112/	1432	1801			
Spark Length=1 mm.	Product of Pressure and Spark Length	19.8	0.41	6.83	5.86	5.03	4.31	3.73	3.18	25.13	2.34	00.7	7.77	14.1	1.00	1.00	.946	218.			

Table IV. Hydrogen. (Carl.)

= 10 mm.	Spark Potential in Volts	526	427	335	299	283	707	280	943	010	420	cac	850	1142	1477	1710			
Spark Length=10 mm.	Product of Pressure and Spark Length	75.3	43.7	25.5	17.7	14.6	12:2	1.0.1	04.00	20.7	67.6	4.70	3.90	3:30	2.76	2.64			
h=5 mm.	Spark Potential in Volts	469	415	350	300	287	281	282	285	293	305	345	410	539	904	975	1373	1775	
Spark Length = 5 mm.	Product of Pressure and Spark Length	89	46.7	30.1	19.0	16.4	14.0	12.0	10.2	08.8	29.4	6.30	5.45	4.64	4.04	3.50	3.00	2.58	
h=3 mm.	Spark Potential in Volts	415	356	301	286	278	282	292	310	356	440	564	780	1054	1382	1789			
Spark Length=3 mm.	Product of Pressure and Spark Length	40.8	25.6	16.2	13.9	12.0	10.3	8.79	7.56	6.45	5.55	4.77	4.05	3.48	00.8	9 64 20 70 80 80			
h=2 mm.	Spark Potential in Volts	435	360	323	299	285	279	284	293	305	333	399	523	797	0101	1380	1746	OX # T	
Spark Length=2 mm.	Product of Pressure and Spark Length	97	9.6%	0.23	1.91	13.9	11.8	10.0	09.8	7-44	6.46	5.54	4.73		3798	0.40 0.06	99.6	00 2	
h=1 mm,	Spark Potential in Volts	000	300	981	978	287	306	33 6	374	487	649	005	1975	1401	1011				
Spark Length=1 mm,	Product of Pressure and Spark Length	l i	21.7	201	10.0	8:04	7.7	6.50	75.5	4.73	4:11	4 II	9.04	5.04	7.60				

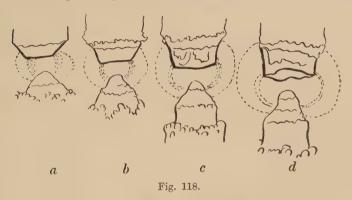
#### CHAPTER XIV.

#### THE ELECTRIC ARC.

213. In the electric spark and the discharge from a point the difference of potential between the electrodes is several hundred volts, while the current is only a fraction of a milliampère; in the case we now proceed to consider,—the electric arc,—where the electrodes are in a state of incandescence, the potential difference is very much smaller, while the current is enormously greater, often amounting to many ampères. We can produce the arc discharge if we take a battery of cells of small resistance, numerous enough to give a potential difference of 60 to 80 volts, and connect the electrodes with two carbon terminals which are at first pushed against each other, a current of electricity flows through the carbons and warms the junction; if while the current is still passing the carbons are drawn apart a bright discharge which may carry a current of many ampères passes from one carbon terminal to the other. This discharge, which is called the electric arc, is characterized by intense heat and light which make it of great practical importance. The main sources of the light are the extremities of the carbon rods which are in a state of vivid incandescence. The temperature of the extremity of the positive terminal is much higher than that of the negative; according to Violle\* the temperature of the former is about 3500° C., that of the latter about 2700° C., while the temperature of the arc itself he found to be higher than that of either terminal. The terminals if similar to begin with soon present marked differences in their appearance, the extremity of the positive terminal gets hollowed out into a crater-like shape, while the negative terminal if pointed to begin with remains so. Both terminals in general lose weight.

<sup>\*</sup> Violle, Comptes Rendus, cxv. p. 1273, 1892.

the positive, however, far more than the negative. The appearance of the terminals is shown in Fig. 118; these figures are due to Mrs Ayrton\*. a and b represent the appearance when the arc is quiet, d when it is giving out a hissing sound; in some cases a mushroom-shaped body forms at the end of the negative terminal.



The temperature of the crater of the positive terminal remains constant even when the current varies, an increase of current increases the area of the luminous crater, but the amount of light given out by each unit area remains unaltered; the temperature of the crater is probably the temperature at which carbon melts or volatilizes. E. W. Wilson† has shown that when the arc passes through gas at a very high pressure, say 20 atmospheres, the luminosity of the positive crater is sensibly less than at atmospheric pressure; in a later paper he gives reasons for thinking that this may be explained by the increased absorption of light by the gas surrounding the arc.

Connection between the difference of potential between the electrodes, the length of the arc, and the current.

**214.** If V is the potential difference between the terminals, l the length of the arc, Fröhlich; showed that the linear relation

$$V = m + nl$$
,

where m and n are constants, i.e. independent of l, exists between

<sup>\*</sup> Mrs Ayrton, Proc. Inst. Electrical Engineers, xxviii. p. 400, 1899.

<sup>†</sup> E. W. Wilson, Proc. Roy. Soc., lviii. p. 174, 1895; lx. p. 377, 1897.

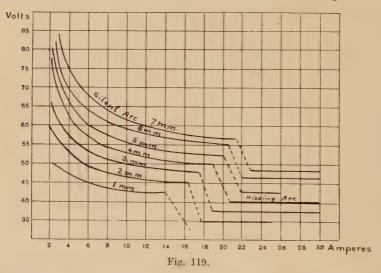
<sup>‡</sup> Fröhlich, Elektrotechnische Zeitschrift, iv. p. 150, 1883.

V and l. Mrs Ayrton\* has shown that both m and n are functions of the current i passing through the arc, and that

$$V = \alpha + \frac{\beta}{i} + \left(\gamma + \frac{\delta}{i}\right),\,$$

where  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$  are constants.

Ayrton<sup>+</sup> made a long series of experiments on the relation between the potential difference and the current through the arc, some of the curves representing the results of these experiments are given in Fig. 119, where the ordinates represent the potential



difference and the abscissae the current; it will be seen from these curves that for a quiet arc an increase in current is accompanied by a decrease in the potential difference, while in the hissing arc the potential difference is independent of the current.

The constants m and n in Fröhlich's formula have been measured by several experimenters, by Fröhlich himself, Edlund‡, Peukert  $\S$ , v. Lang  $\|$ , Gross and Shephard  $\P$ , Nebel \*\*, Arons  $\dagger \dagger$ ,

- \* Mrs Ayrton, The Electric Arc, chap. IV.
- + W. E. Ayrton. Mrs Ayrton, The Electric Arc.
- ‡ Edlund, *Pogg. Ann.*, 134, pp. 251, 337, 1868.
- § Peukert, Zeitschrift für Elektrotechnik, Wien, iii. p. 111, 1885.
- || v. Lang, Wied. Ann., xxvi, p. 145, 1885; xxxi. p. 384, 1887.
- ¶ Gross and Shephard, Proc. Amer. Acad. of Sciences, 1886, p. 2.
- \*\* Nebel, Centralblatt für Elektrotechnik, viii. pp. 517, 619, 1886.
- + Arons, Wied. Ann., lviii. p. 73, 1896.

Luggin\*; for carbon electrodes in air at atmospheric pressure m is about 39 volts, varying somewhat with the size and purity of the carbons; it is diminished by soaking these in salt solution; the value of n given by different experimeters varies considerably, this may be due to their having used currents of different intensities, as Mrs Ayrton has shown that it depends upon the current, diminishing as the current increases. When metallic instead of carbon terminals are used the value of m depends upon the metal being in general larger the higher the temperature at which the metal volatilizes; the values in volts found by v. Lang† for m for terminals of different substances are as follows: C = 35, Pt = 27.4, Fe = 25, Ni = 26.18, Cu = 23.86, Ag = 15.23, Zn = 19.86, Cd = 10.28. Lecher gives Pt = 28, Fe = 20, Ag = 8. Arons found for Hg the value 12.8, in this case the fall of potential along the arc itself was abnormally small. In interpreting these results it is important to notice that with some terminals the arc is intermittent. Lecher has shown that this is the case with iron or platinum terminals, and Arons that it is so with mercury terminals; no intermittence has been detected with carbon, silver or copper terminals. The potential differences given above are mean values, and if the arc is intermittent they may differ greatly from the actual potentials during the passage of the arc.

If the two terminals are of different materials the potential difference may depend upon the direction of the currents, this is especially the case when one of the electrodes is carbon and the other metal; the arc passes much more easily when the carbon is the negative terminal and the metal the positive one than it does in the opposite direction. So marked is this effect that if such a pair of terminals is connected up with an alternating electromotive force the arc may pass only in the direction in which the carbon is the negative terminal, the potential difference being insufficient to drive it the opposite way. For experiments on this point we may refer to papers by Blondel ||, by Duddell and Marchant ¶, and by Eichberg and Kallir\*\*.

<sup>\*</sup> Luggin, Wien. Ber., xeviii. p. 1192, 1889.

<sup>+</sup> v. Lang, Wied. Ann., xxxi. p. 384, 1887.

<sup>‡</sup> Lecher, Wied. Ann., xxxiii. p. 609, 1888.

<sup>§</sup> Arons, Wied. Ann. lviii. p. 73, 1896.

<sup>|</sup> Blondel, Comptes Rendus, 127, p. 1016, 1898; 128, p. 727, 1898.

<sup>¶</sup> Duddell and Marchant, Inst. Elect. Eng., xxviii. p. 1, 1899.

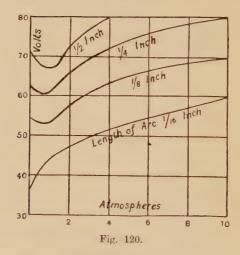
<sup>\*\*</sup> Eichberg and Kallir, Wien. Sitz. 107, p. 657, 1898.

#### Non-arcing Metals.

215. With some metals as terminals the arc has a great tendency to go out and is only maintained with difficulty; brass, cadmium, and bismuth are examples of such metals; in some cases this is a very useful property, it has been investigated by Wurtz\*: a great deal depends upon the size and shape of the electrodes, as well as of the material they are made; conditions which promote a rapid flow of heat from the hot extremities of the terminals are favourable to the extinction of the arc.

# Effect of pressure on the potential difference in the arc discharge.

216. The potential difference is not independent of the pressure of the gas through which the arc passes. Duncan, Rowland and Todd † have made an extensive series of experiments on this point; the results of some of their experiments are represented graphically in Fig. 120: it will be seen from the curves that for



short arcs the potential difference increases continuously with the pressure, while for longer arcs there is a critical pressure at which the potential difference is a minimum; this critical pressure seems to increase with the length of the arc.

<sup>\*</sup> Wurtz, Lum. El., xlv. p. 79, 1892.

<sup>+</sup> Duncan, Rowland and Todd, Electrician, xxxi. p. 60.

Effect of the nature of the gas on the potential difference.

217. The nature of the gas affects the arc, thus it is difficult to get good arcs in pure hydrogen; this may be due in part at least to the more rapid convection of heat from the terminals in this gas. Arons\* has measured the potential difference required to produce an arc 1.5 mm. long, carrying a current of 4.5 ampères between terminals of different metals in air and pure nitrogen; his results are given in the following table:

	Potential difference			Potential difference		
Terminal	Air	Nitrogen	Terminal	Air	Nitrogen	
Ag	21 23 25 27 29	? 21 21 30 20	Pt	36 39	30 27 18 22	

The case of silver is interesting as, though it gives good arcs in air, Arons could not obtain an arc in pure nitrogen; he ascribes this to the absence of any chemical combination between the silver and the nitrogen; he was able in the case of the other metals to get evidence of the formation of nitrides. With the exception of copper the potential differences in nitrogen are smaller than in air, the difference being very noticeable in the cases of iron and aluminium.

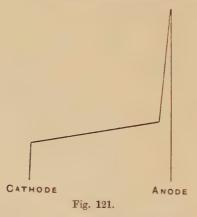
Arons also made a series of experiments in hydrogen, but found the greatest difficulty in producing the arc in this gas, and could only obtain it by using large currents and having the gas at a low pressure; cadmium, zinc, and magnesium gave the best arcs in hydrogen.

We must in the case of the arc remember that since the metal or the carbon volatilizes the arc goes through a mixture of the vapour of the metal and the air, nitrogen or hydrogen in which the terminals are immersed, so that the conditions of the experiment are very complicated; the presence of this vapour makes

<sup>\*</sup> Arons, Drude's Annalen, i. p. 700, 1900.

ambiguous the interpretation of the effect of changes of pressure in the gas around the terminals, as we do not know the pressure of this vapour.

218. The distribution of potential between the terminals generally shows the following characteristics: there is a considerable fall of potential close to the anode, a smaller one close to the cathode, and a very gentle potential gradient in the space between the terminals; the general nature of this distribution is shown by the curve in Fig. 121: the curve shows many of the characteristics



of the distribution of potential between two hot electrodes in flames; see p. 191.

Luggin\* found that with carbon terminals and a current of 15 ampères there was a fall of potential of 33.7 volts close to the anode, and one of 8.7 close to the cathode. The difference between the potential falls at the anode and cathode is not so large with iron or copper electrodes as it is with carbon. With mercury terminals Arons found that the cathode fall was 5.4 volts, the anode fall 7.4 volts. When the current is increased so much that the discharge passes from the quiet to the hissing arc there is a sudden fall of potential. Luggin† and Mrs Ayrton‡ have shown that this diminution in the potential occurs almost entirely at the anode, the potential gradients in the other parts of the discharge being but little affected.

<sup>\*</sup> Luggin, Centralblatt für Elektrotechnik, x. p. 567, 1888.

<sup>+</sup> Luggin, Wien. Sitz., xeviii. p. 1192, 1889.

<sup>#</sup> Mrs Ayrton, The Electric Arc.

219. Some experiments which are very suggestive as to the parts played by the two terminals in the arc discharge have been made by Fleming\*. In these experiments a third exploring carbon electrode was used which was either inserted in the arc, or what was often more convenient, placed outside the undisturbed path of the arc, and the arc directed on to it by means of a magnet. Fleming found that when the third terminal was connected with the negative terminal of the arc by a circuit which contained a battery of a few cells and a galvanometer to register the current, a current passed round the circuit under a very small electromotive force when the direction of the current was from the cold electrode placed in the arc through the arc to its negative terminal and then through the galvanometer, but that it would not pass in the other direction: another way of stating this result is to say that with one electrode hot and the other cold, a current can pass in the direction in which the negative electricity comes from the hot electrode into the gas, but not in the other direction. Thus although in ordinary arcs the positive terminal is the hotter, this experiment shows that a high temperature of the negative electrode is the essential condition for the arc discharge, and that if we can keep the temperature of the negative terminal up by independent means we can get a discharge, even although the temperature of the positive electrode is comparatively low. No arc, however, will pass if the negative terminal is cold.

Fleming found that if he connected the exploring electrode up to the positive electrode, without introducing any battery into the circuit, enough current passed through the exploring electrode to ring an electric bell or light an incandescent lamp placed between the electrode and the positive terminal: but that no appreciable current passed if the electrode were connected with the negative instead of the positive terminal; this result indicates that the potential of the spare electrode is brought nearly to an equality with that of the cathode. From these experiments Fleming concluded that the arc discharge consists of a torrent of negatively electrified particles of carbon shot off from the cathode, these carry the current and striking with great violence against the anode hollow it out, just as a body is hollowed out when struck by a sand blast.

<sup>\*</sup> Fleming, Proc. Roy. Soc., xlvii. p. 123, 1890.

The phenomena connected with the discharge of electricity from incandescent bodies (see Chap. VIII.) seem to me to indicate a somewhat different explanation of the arc discharge. We saw that an incandescent body such as a piece of carbon, even when at a temperature far below that of the terminals in the arc discharge, emits negatively electrified corpuscles at a rate corresponding to a current of the order of an ampère per square centimetre of incandescent surface, and that the rate of emission increases very rapidly with the temperature; thus at the temperature of the negative carbon in the arc the rate of emission probably corresponds to a current of a large number of ampères per square centimetre of hot surface. If then a piece of carbon were maintained by independent means at this high temperature and if this were used as the negative electrode a current could be sent through a gas to another electrode, whether this second electrode were cold or hot

Let us first suppose that the anode is cold, then the current would be carried entirely by negative ions, there would be free negative ions in the space between the electrodes, these would cause the electric force to increase as we pass from the cathode to the anode and would make the current increase rapidly with the potential difference. Now suppose that the anode becomes hot and that there is some gas in contact with it which can be ionised, yielding a supply of positive ions; this current will no longer be carried entirely by negative ions, though inasmuch as (p. 192) the velocity of the negative ion at these high temperatures is very much greater than that of the positive, by far the larger part of the current is carried by the negative ions. The presence of the positive ions, however, modifies very considerably the distribution of potential between the electrodes: the positive ions diffuse into the region of the discharge until they are sensibly equal in number to the negative ions; when this is the case the electric force is sensibly uniform between the terminals except close to the electrodes, and we have a distribution similar to that given in Fig. 49, p. 191, which is taken from a paper by H. A. Wilson on the conductivity through hot gases, and represents the distribution of potential between two hot electrodes: by comparison with Fig. 121 it will be seen that this bears a great resemblance to the distribution of potential between the terminals in the arc discharge.

The view we take of the arc discharge is that it is similar to the discharge between the incandescent terminals just considered, the only difference being that in the flame the temperature of the terminals is maintained by independent means, while in the arc it is maintained by the work done by the discharge itself; this requires that the potential difference between the electrodes also and the current passing between them should not sink below certain values. On the other hand when the temperature is maintained by external aid the smallest potential difference is able to send a current.

On this view the cathode is bombarded by the positive ions which maintains its temperature at such a high value that negative corpuscles come out of the cathode; these which carry by far the larger part of the arc discharge bombard the anode and keep it at incandescence, they ionise also either directly by collision or indirectly by heating the anode, the gas or vapour of the metal of which the anode is made producing in this way the supply of positive ions which keep the cathode hot. It will be seen that the essential feature in the discharge is the hot cathode, as this has to supply the carriers of the greater part of the current in the arc; the anode has in general to be hot, otherwise it could not supply the positive ions which keep the cathode hot; in such a case as that of a third electrode put in the arc and acting as one of the anodes we may regard the discharge as having two anodes, and as one is sufficient to keep the cathode hot we can get the arc to pass to the other anode even although it is cold.

220. The conditions that determine the current when a given electromotive force acts round the whole circuit of the arc are that the work supplied to the cathode and anode should be sufficient to maintain them at incandescence. Although we have not the data which would make a numerical calculation possible, yet an expression in an analytical form of these conditions may serve to make the preceding theory clearer and more definite.

We have seen that the number of corpuscles emitted in one second by unit area of a hot body increases very rapidly with the temperature, being represented with considerable accuracy by

a formula of the form  $A\theta^{\frac{1}{2}}e^{-\frac{w}{\theta}}$ , where  $\theta$  is the absolute temperature;

or

we shall call this function  $f(\theta)$ , then if  $\theta$  is the temperature and  $\omega_1$  the area of the luminous part of the cathode the number of corpuscles coming from the cathode in one second is equal to  $\omega_1 f(\theta)$ . If i is the current,  $R_1$ ,  $R_2$  the velocities of the positive and negative ions under unit electric force, the part of the current carried by the negative ions is  $R_2 i/(R_1 + R_2)$ , and this when divided by e, the charge on an ion, is equal to the number of negative ions passing a section of the arc per second; hence we have

$$\frac{R_2}{R_1 + R_2} \frac{i}{e} = \omega_1 f(\theta) \quad \dots (1).$$

Let us now consider the temperature equilibrium of the cathode. Let  $\omega_i \phi(\theta)$  be the rate at which it is losing heat by radiation and conduction, w the work expended when the cathode emits one corpuscle, then to maintain thermal equilibrium the rate at which energy must be given to the cathode is

$$\frac{w}{e}\frac{R_{2}}{R_{1}+R_{2}}i+\omega_{1}\phi\left(\theta\right);$$

this work has to be supplied by the positive ions coming up to the cathode in unit time; the number of such ions is

$$\frac{R_1}{R_1+R_2}\frac{i}{e};$$

we shall suppose that the energy they possess is got in passing through the fall of potential at the cathode; let this fall be denoted by  $E_0$ , then equating the rate at which energy is communicated to the cathode to the rate at which the cathode is losing energy we get

$$E_{0} \frac{R_{1}}{R_{1} + R_{2}} i = w \frac{R_{2}}{R_{1} + R_{2}} \frac{i}{e} + \omega_{1} \phi(\theta),$$

$$E_{0} = \frac{w}{e} \frac{R_{2}}{R_{1}} + \omega_{1} \frac{R_{1} + R_{2}}{R_{2}} \frac{\phi(\theta)}{i} \dots (2).$$

Let  $\theta_1$  be the temperature and  $\omega_2$  the area of the hot part of the anode,  $\omega_2\psi(\theta_1)$  the rate at which it is losing energy by radiation, conduction, and vaporisation, W the amount of work required to produce a positive ion.

The number of positive ions produced in unit time is

$$\frac{R_1}{R_1+R_2}\frac{i}{e}$$
;

thus the work absorbed per second at the cathode is

$$\omega_{2}\psi\left(\theta_{1}\right)+\frac{R_{1}}{R_{1}+R_{2}}\frac{Wi}{e}.$$

The number of negative ions striking against the anode in unit time is

$$\frac{R_{\scriptscriptstyle 2}}{R_{\scriptscriptstyle 1}+R_{\scriptscriptstyle 2}}\frac{i}{e}\,;$$

let us suppose that the energy with which they strike against the anode is that due to passing through the anode fall of potential  $E_1$ , equating the rate at which the anode is losing energy to that at which it is gaining it we have

thus

 $\theta_1$ , as we have seen, does not depend on the current but only on the material of which the anode is made.

If E is the external electromotive force acting on the circuit, R the resistance of the leads, then E-Ri is the potential difference between the arc terminals; when the arc is so short that we may neglect the changes in potential along the arc, apart from those at the anode and cathode, this difference of potential is equal to  $E_0 + E_1$ ; hence we have

$$E - Ri = E_0 + E_1 \dots (4)$$

thus we have four equations (1), (2), (3), and (4) to determine the four quantities  $\theta$ , i,  $E_0$ , and  $E_1$ .

Mrs Ayrton has shown that  $\omega_2$  the area of the crater is a linear function of the current and may be represented by an equation of the form  $\omega_2 = a + bi$ ; if  $\omega_1$  follows the same law then equations (2) and (3) suggest that  $E_0 + E_1$  will be of the form  $\alpha + \frac{\beta}{i}$ , where  $\alpha$  and  $\beta$  are independent of i, and this is in accordance with the results of the experiments made on the relation between the current through the arc and the potential difference between its terminals.

221. Taking the equation

$$E = Ri + \alpha + \frac{\beta}{i} \dots (5),$$

we see that the graph representing this relation is a hyperbola. E has a minimum value at the point A, this value is

$$2\sqrt{\beta R} + \alpha$$
.

The portion of the graph to the left of A corresponds to an unstable state, for suppose the current is changed from  $i_0$  to  $i_0 + x$  and

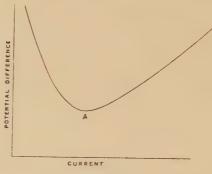


Fig. 122.

that there is self-induction L in the external circuit, let E' be the steady electromotive force due to batteries, &c., in this circuit, then from (5) we have

$$E' - L\frac{dx}{dt} = R(i_0 + x) + \alpha + \frac{\beta}{i_0 + x},$$

or when x is small

$$-L\frac{dx}{dt} = x\left(R - \frac{\beta}{i_0^2}\right),$$

$$x = Ce^{\frac{t}{L}\left(\frac{\beta}{i_0^2} - R\right)}$$

or

Now to the left of A,  $\frac{\beta}{i_0^2} - R$  is positive, hence x will increase indefinitely with t and the current will be unstable; to the right of A this quantity is negative and x will diminish to zero as the time increases, the current under these conditions will be stable. Thus for stability the current cannot be less than its value at A, i.e.  $(\beta/R)^{\frac{1}{2}}$ , hence if  $i_m$  is the minimum current,  $E_m$  the minimum external electromotive force, we have

$$i_m = (\beta/R)^{\frac{1}{2}},$$

$$E_m = 2(\beta R)^{\frac{1}{2}} + \alpha.$$

or if the external electromotive force is E the arc will go out if the resistance R in the external circuit is greater than

$$\frac{(E-lpha)^2}{4eta}$$
 .

Thus as one numerical example let us take the case of the arc 6 mm. in length for which the curve representing the relation between the current through the arc and the potential difference between the terminals is represented in Fig. 119, page 418; from the curve we find that  $\beta=3.4\times10^8$  in absolute measure; we may take  $\alpha$  as about 40 volts, or in absolute measure  $4\times10^9$  if E the electromotive force in the external circuit is 80 volts or  $8\times10^9$  absolute units; we find that the arc will go out if the resistance is greater than

$$\frac{16 \times 10^{18}}{4 \times 3.4 \times 10^{8}} = 1.2 \times 10^{10} = 12 \text{ ohms.}$$

222. Another way of treating the problem of the arc graphically is, instead of tracing the curve

$$E = Ri + F(i),$$

where F(i) is the potential difference between the terminals of the arc when it is carrying the current i, to trace the curve

$$y = F(i)$$

and the straight line

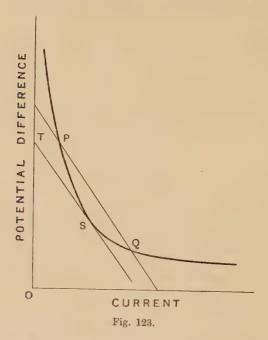
$$y = E - Ri;$$

if these intersect in two points P and Q (Fig. 123) we can show as before that the state corresponding to P is unstable, and that the current under the given external electromotive force and resistance is represented by the abscissa of the point Q; if the resistance is too great the line may not cut the curve at all, while if it is too small the point Q may be so far away that the corresponding value of the current may be too great for a silent arc and a hissing arc will necessarily be formed.

The minimum current for a given external resistance is got by finding the point S when the tangent to the curve is parallel to the line y = -Ri. The current at S is the minimum current, and the value of OT, T being the point where the tangent at S intercepts the axis i = 0, is the minimum external electromotive force.

To find the maximum value of R for which the arc can exist under a given external electromotive force  $E_1$  take  $ON = E_1$ , and from N draw a tangent to the curve; let this tangent cut the axis y = 0 in M, then ON/OM is the required resistance.

223. Hissing Arcs. When the current is increased beyond a certain value, the potential difference between the terminals falls in the case of carbon electrodes by about 8 or 10 volts and does not change when the current is increased; when in this state, the arc emits a hissing sound. Mrs Ayrton\*, who has made a study of the hissing arc, has shown that it occurs when the incandescence of the anode covers such a large area that it expands beyond the crater up the sides of the terminal: see Figs. 118, c and a, which represent the appearance of the arc in



the hissing and quiet stages. The hissing of the arc is closely connected with the oxidation of the terminal by the air; for when the incandescence extends up the sides of the carbon, the glowing carbon is no longer completely protected by the carbon vapour

<sup>\*</sup> Mrs Ayrton, The Electric Arc.

from oxidation. It is then that the arc hisses. Mrs Ayrton has shown that if the arc is formed in a closed vessel an increase of current ceases to make it hiss as soon as the oxygen in the vessel has been burnt up; whenever, however, fresh oxygen is introduced into the vessel the hissing recommences.

We can see why chemical combination should tend to diminish the potential difference between the terminals of the arc, for the heat evolved by the burning of the terminals would tend to maintain them at incandescence, so that the whole of the energy required for this purpose would no longer have to be supplied by the electric field.

Trotter\* has shown that parts of the arc are in rapid motion in the unstable state between the hissing and the quiet arc.

224. Effect of a magnetic field on the arc. The arc is deflected by a magnetic field in the same direction as a flexible conductor would be if it carried a current flowing in the same direction as that through the arc. The curved course corresponds to a longer path and the effect of the magnetic field on the potential difference is of the same character as an increase in the length of the arc, and just as it is possible to extinguish an arc by increasing its length, so the arc can be blown out by the application of a strong magnetic field.

<sup>\*</sup> Trotter, Proc. Roy. Soc. lvi. p. 262, 1894.

# CHAPTER XV.

# DISCHARGE THROUGH GASES AT LOW PRESSURES.

225. When the electric discharge passes through a gas at a low pressure differences in the appearance of the discharge at various points in its path become very clearly marked. The discharge (Fig. 124) presents the following features: starting from the cathode there is a thin layer of luminosity spread over its



Fig. 124.

surface, next to this there is a comparatively dark space, called the Crookes dark space, the width of which depends on the pressure of the gas, increasing as the pressure diminishes, it also as Schuster\* has shown depends to some extent on the intensity of the current, being greater for large currents than for small; the boundary of the dark space is approximately the surface traced out by normals of constant length drawn to the surface of the cathode; beyond the dark space there is a luminous region called the 'negative glow'; beyond this again is another comparatively dark region called by some writers the 'second negative dark space,' and by others the 'Faraday dark space,' its length is very variable even when the pressure is constant; beyond this again there is a luminous column reaching right up to the anode and called the 'positive column'; when the current and pressure are within certain limits this column exhibits remarkable alternations of dark and bright spaces, these are called striations and are shown in Fig. 125. The figure is taken from a paper by

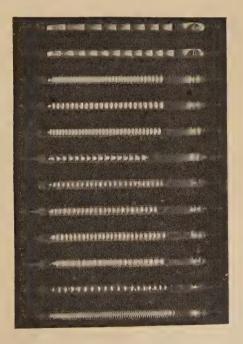


Fig. 125.

De la Rue and Müller, *Phil. Trans.*, 1878, pt. 1, p. 155. In long tubes the positive column constitutes by far the greater part of

<sup>\*</sup> Schuster, Proc. Roy. Soc. xlvii. p. 557, 1890.

the discharge, for the Crookes space, the negative glow, and the Faraday dark space do not depend markedly upon the length of the tube, so that when the length of the discharge is increased, the increase is practically only in the length of the positive column; thus for example in a tube used by the writer about 15 metres long the positive column occupied the whole of the tube with the exception of two or three centimetres close to the cathode.

# Distribution of the Electric Force along the discharge.

226. The electric force varies greatly along the discharge, it has been measured by Hittorf\*, Graham†, A. Herz‡, Skinner§, and H. A. Wilson||. The method employed by these observers was to measure the potential acquired by a metal wire placed in various positions along the line of discharge, if the potential of the wire is the same as that of the gas with which it is in contact we get from these observations the means of determining the distribution of electric force along the tube. As an example of how this method is carried out in practice we may take the apparatus used by H. A. Wilson and shown in Fig. 126. The discharge

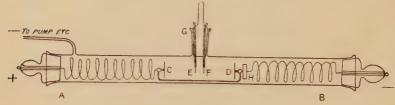


Fig. 126.

passed between two aluminium discs C and D supported by thin glass rods which kept them a constant distance apart. Flexible wire spirals connected these electrodes with wires sealed through the ends of the tube. A piece of iron H was fixed to the frame carrying the electrodes and enabled it to be moved along the tube by means of a magnet. Two electrodes E, F about 1 mm.

- \* Hittorf, Wied. Ann. xx. p. 705, 1883.
- † Graham, Wied. Ann. lxiv. p. 49, 1898.
- ‡ A. Herz, Wied. Ann. liv. p. 246, 1895.
- § Skinner, Wied. Ann. lxviii. p. 752, 1899.
- || H. A. Wilson, Phil. Mag. v. 49, p. 505, 1900.

apart were fused through the side tube G, these electrodes were connected with a quadrant electrometer whose deflection gave the difference of potential between E and F, and hence the electric force at this part of the tube. By moving the framework, EF could be brought into any part of the discharge between C and D, and thus the distribution of electric force between the electrodes mapped out. Another method which has been used is to keep the electrodes C and D fixed and move E, F by attaching them to a support floating on the top of a column of mercury the height of which could be altered.

For methods such as those just described to be successful the secondary electrodes must take up the potential of the gas with which they are in contact; to enable them to do this quickly there must be a plentiful supply of both positive and negative ions in the gas which by giving up their charges to the wire can raise or lower its potential to equality with the surrounding gas; the results obtained seem to justify the assumption that at moderate pressures the secondary electrodes do in most parts of the discharge acquire the potential of the gas, but the method is a dangerous one when the pressure is very low, or when the wire is placed in the Crookes space where the conductivity is very low.

Thus, to take an extreme case, suppose that a secondary electrode is placed in an enclosure in which there are torrents of negative ions but no positive ones, then the wire will go on receiving negative electricity until it gets so highly charged that it is able to repel the negative ions sufficiently to prevent any more striking it; when this stage is arrived at its potential may be lower than that at any point in the enclosure previous to its introduction.

227. I have suggested for discharge at low pressures the use of a method in which the deflection of the cathode rays is used to measure the strength of the electric field. The apparatus used to carry out this method is shown in Fig. 127. A and B are the electrodes kept at a constant distance apart and attached to springs, by means of which they can be moved along the tube. E and F are side tubes placed in line with each other, in E cathode rays are produced by a Wimshurst machine,

a pencil of these rays passes through a small hole in the disc G, traverses the electric discharge passing between A and B, then travels down the tube F producing a bright patch on a phos-

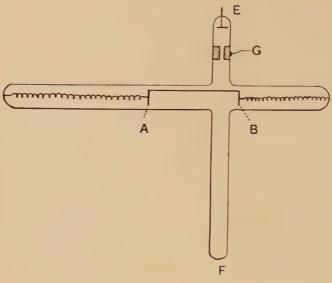
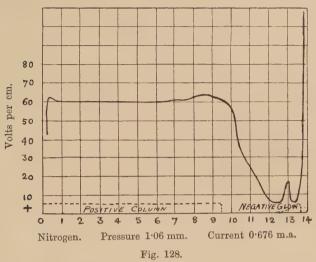


Fig. 127.

phorescent screen placed at the end of the tube. As the cathode rays are deflected by the electric force along the line of discharge the patch on the screen will be deflected from the position it occupies when the discharge is not passing; by measuring this deflection we can determine the electric force at the part of the discharge traversed by the rays; by moving the electrodes  $\boldsymbol{A}$  and  $\boldsymbol{B}$  along the tube we can map out the electric field at all parts of the discharge. Mr Strachan at the Cavendish Laboratory has in this way obtained the distribution of electric force in gases at low pressure.

228. The distribution of electric force in a discharge tube under various circumstances as to pressure and current is represented in the following figures in which the ordinates represent the value of the electric force at a point in the tube whose position is fixed by the abscissa. From these curves we infer that the electric force is very large indeed in the Crookes dark space, diminishes rapidly towards the negative glow, and in the negative

glow itself it is very small; it reaches a minimum either in the glow itself or in the portion of the Faraday dark space just



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outside the negative glow, after which it increases, towards the positive column; in the case of a uniformly luminous positive column (Fig. 128) the electric force is constant along it until we get quite

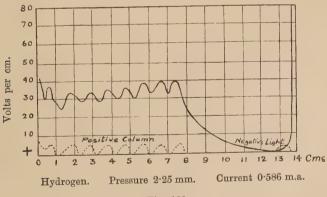
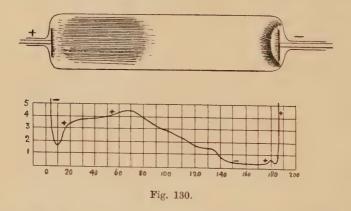


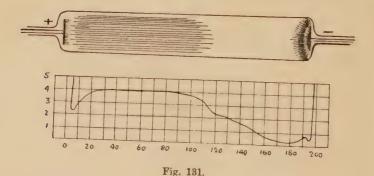
Fig. 129.

close to the positive electrode; a sudden jump in the potential called the anode fall of potential occurs quite close to the anode; in many of Wilson's experiments this drop was preceded by the

electric force falling to an exceedingly low value; in some cases indeed it was apparently reversed; it is not certain however that this apparent reversal may not have been due to disturbances produced by the introduction of the wires, &c., used to measure the potential. When the positive column was striated then, as we see from Fig. 129, the alternations of luminosity in the positive column are accompanied by alternations in the value of the electric force, maxima of the electric force occurring at the bright parts of the striæ, minima at the dark parts. Graham



showed that when the gas was impure there were considerable variations in the electric force even in the luminous positive column; this is shown in Fig. 130 and Fig. 131, which repre-



sent the distribution of electric force in an impure gas and in one which had been carefully purified. When there is no positive

column there is no region of constant intensity between the anode and the negative glow.

If X is the electric force, supposed parallel to x, and  $\rho$  the density of the electrification, then from the equation

$$\frac{dX}{dx} = 4\pi\rho$$

we see that the slope of the curves for x enables us to find the excess of the positive over the negative ions at each point of the discharge; an inspection of the curves shows that there is a very large excess of positive over negative in the Crookes dark space; in the negative glow the positive and negative ions are about equal in number; in the Faraday dark space there is an excess of negative ions; in the uniform positive column the two kinds of ions are about equal in number, while in a striated positive column there is a negative charge on the cathode side of the bright part of a striation and a positive charge on the anode side.

Distribution of electric force near the cathode. electric field in the neighbourhood of the cathode has been the subject of many researches. Hittorf\* showed that the potential difference between the cathode and a point in the negative glow was independent of the current, provided this was not great enough to cause the negative glow to enclose the whole of the cathode. When that stage was reached the potential between the cathode and the glow increased with the current. Thus if the cathode is a wire, then when the current is small the negative glow only surrounds the tip of the wire; as the current is increased the negative glow encloses more and more of the wire, but it is not until the glow reaches the end of the cathode that the difference of potential between the cathode and the glow begins to be affected by the current. This difference of potential is called the cathode fall of potential. Warburg + showed that it was independent of the pressure of the gas, and that the potential fall was practically the same whether platinum, zinc, copper, silver or iron electrodes were used; it was, however, considerably less when the electrodes were

<sup>\*</sup> Hittorf, Wied. Ann. xx. p. 705, 1883.

<sup>†</sup> Warburg, Wied. Ann. xxxi. p. 545, 1887; xl. p. 1, 1890.

made of aluminium or magnesium. Mey\* has recently shown that the cathode fall of potential depends more than had been thought on the nature of the cathode, and that it falls to comparatively low values for the strongly electro-positive alkali metals (see also Lyman, Proc. Camb. Phil. Soc. XII. p. 45, 1902). With zinc, copper and iron electrodes the cathode fall of potential is often abnormally small when the electrodes are new; it rises however to its normal value after the electrodes have been used for some time. Warburg ascribes this effect to the presence of a thin layer of oxide on the new electrode, which gets removed in course of time by the disintegration which occurs when the metal is used as a cathode. Hittorf + discovered that the cathode fall became exceedingly small when the cathode was raised to a red heat. Goldstein and Warburg (loc. cit.) found that the diminution in the cathode fall became much less when the heating was continued for a long time. It is worthy of remark in this connection that the emission of negative electricity from an incandescent wire often falls off very considerably after longcontinued heating. Warburg found that a trace of impurity in the gas produced surprisingly large effects on the cathode fall of potential. Thus he found that the cathode fall in nitrogen which contained traces of moisture and oxygen was with a platinum cathode 260 volts, while the same nitrogen, after being very carefully dried, gave a cathode fall of 343 volts; thus a mere trace of moisture had diminished the cathode fall by 25 per cent. As long as the total quantity of water vapour is small, the lowering of the cathode fall does not seem to depend much upon the amount of aqueous vapour present; when however there is much water vapour present the fall is greater than in pure nitrogen; thus in a mixture of aqueous vapour and nitrogen in which the pressure due to the aqueous vapour was 2.3 mm., that due to the nitrogen 3.9 mm., the cathode fall was 396 as against 343 in nitrogen with a trace of oxygen; the increase in the cathode fall was, however, not nearly so great as that in the potential differences along the positive column. In hydrogen Warburg found that a trace of aqueous vapour increased the cathode fall of potential.

<sup>\*</sup> Mey, Verhand. Deutschen Physikalischen Gesellschaft, v. p. 72, 1903.

<sup>+</sup> Hittorf, Wied. Ann. xxi. p. 133, 1884.

<sup>‡</sup> Goldstein, Wied. Ann. xxiv. p. 91, 1885.

Warburg \* also investigated the effect of removing from the gas all traces of oxygen. This was done by depositing on the inside of the tube a thin layer of sodium, which was produced by placing the tube in sodium amalgam, heating the glass and sending a current of electricity from the amalgam through the hot glass to an electrode inside the tube: the sodium thus deposited combined with any oxygen there might be in the tube. The removal of the oxygen produced a very great effect on the potential fall; thus in nitrogen with platinum electrodes the cathode fall was reduced by the removal of a trace of oxygen from 343 to 232 volts, while with magnesium electrodes the cathode fall when there was no oxygen was 207 volts. In hydrogen free from oxygen the cathode fall was 300 with platinum electrodes and 168 with magnesium electrodes; thus with platinum electrodes the cathode fall is greater in hydrogen than in nitrogen while with magnesium electrodes it is less.

The following table contains the results of the measurements of the cathode fall of potential in various gases by Warburg (*loc. cit.*), Capstick† and Strutt‡; it also contains the measurements by

Gas		ode fall in vo num electrod	Cathode fall with aluminium	Minimum po- tential differ- ence required to produce a	
	WARBURG	CAPSTICK	STRUTT	electrodes. Warburg	spark. STRUTT
$\begin{array}{c} \text{Air} \dots \\ \text{H}_2 \dots \\ \text{O}_2 \dots \\ \text{N}_2 \end{array}$ $\text{Hg vapour}$	340—350 about 300  230 if free from O 340	298 369 232	***	168  207	341 302—308  251
$Hg$ vapour $Helium \dots H_2O \dots NH_3 \dots$	940 •••	469 582	226	000	261—326

Strutt of the least potential difference able to produce a spark through the various gases. We see from the results that there is very considerable evidence in favour of the view that the minimum

<sup>\*</sup> Warburg, Wied. Ann. xl. p. 1, 1890.

<sup>+</sup> Capstick, Proc. Roy. Soc. lxiii. p. 356, 1898.

<sup>‡</sup> Strutt, Phil. Trans. exciii. p. 377, 1900.

potential difference required to produce a spark through a gas is equal to the cathode fall of potential in that gas.

The influence of the material of the electrode is shown by the results quoted in the following table which is due to Mey (l.c.).

#### CATHODE FALL.

Gas					F	Electro	de				
	Pt	Hg	Ag	Cu	Fe	Zn	Al	Mg	Na	Na-K	K
$egin{array}{c} O_2 & \dots \\ H_2 & \dots \\ N_2 & \dots \\ He & \dots \\ Arg \dots \end{array}$	369 300 232 226 167	226	295	280	230	213	190	168 207	185 178 80	169 125 78·5	172 170 69

Capstick found that if in dry gases a trace of oxygen was present the cathode fall was approximately the same as in pure oxygen. This is borne out by the results of the experiments of Warburg already quoted on the effect produced by a trace of oxygen in the presence of nitrogen. When water vapour is present it would appear from Warburg's experiments that this effect of the oxygen is to a large extent neutralised. We have already (p. 402) alluded to Warburg's experiments on the great diminution in the rate of escape of negative electricity from a point in nitrogen produced by the presence of a trace of oxygen; it seems probable that this effect is connected with that of a trace of oxygen on the cathode fall. The latter effect can hardly be due to any oxidation of the electrode, for Warburg has shown that the potential fall at slightly oxidised surfaces is less than that at bright ones.

230. For the compound gases  $H_2O$  and  $NH_3$ , the only ones hitherto observed, the cathode fall seems to obey the additive law, thus the cathode fall in  $H_2O$  = cathode fall in  $H_2+\frac{1}{2}$  cathode fall in  $O_2$ , while the cathode fall in  $O_3$ , while the cathode fall in  $O_3$  cathode fall in  $O_4$  cathode fall in  $O_4$  it would be very interesting to see if the connection between the cathode fall in a gas and its chemical composition suggested by the two results just quoted is confirmed by further observations on the cathode fall in other compound

gases. Carr came to the conclusion that the minimum spark potential also followed the additive law. The experimental difficulties are, however, very great, as it is exceedingly difficult to get a continuous discharge through a compound gas. If a circuit containing a telephone is placed in series with the discharge tube Capstick found that it is almost impossible to get the telephone silent when a compound gas is in the tube, while there is no difficulty whatever in doing so with an elementary gas. of the telephone indicates that the discharge is intermittent, and when this is the case the cathode fall cannot be measured.

231. Current density at the cathode. H. A. Wilson\* has measured the current density at a cylindrical wire cathode when the negative glow does not envelope the whole of the negative electrode. Under these circumstances the glow assumes the appearance shown in Fig. 132, its shape resembling a test tube with a well

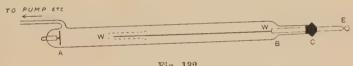


Fig. 132.

marked lip at the end furthest from the anode; as the current increases the glow reaches further along the electrode, the length of the glow being proportional to the current. Wehnelt+ has shown that the discharge from the cathode is confined to the area covered by the glow and that the current density is constant over this area; this shows that the current density at the cathode is independent of the total current flowing through the tube, provided that this is not so large as to make the glow envelope the whole of Wilson made a series of experiments in air at difthe cathode. ferent pressures, ranging from 6.7 mm. to .023 mm., and found that if C is the total current flowing through the tube in milliampères, l the length of wire covered by the glow in centimetres, d the diameter of the wire in centimetres, p the pressure of the gas in mm. of mercury, then  $C/l\pi(d+0.5)p$  was approximately constant and equal to 4; this result indicates that the current density at a point 25 mm. from the surface of the cathode is

<sup>\*</sup> H. A. Wilson, Phil. Mag. vi. 4, p. 608, 1902.

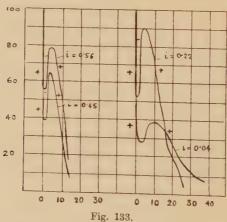
<sup>†</sup> Wehnelt, Drude's Ann. vii. p. 237, 1902.

constant when the pressure is constant whatever the diameter of the wire, and is proportional to the pressure when this alters. It is remarkable that the current density is the same for aluminium as for platinum electrodes, though the cathode fall is different. An inspection of Wilson's numbers shows that though C/p is approximately constant there is a tendency for it to slowly decrease to a minimum and then slightly increase again.

232. The distribution of electric force in the dark space and negative glow. The first determination of the electric force in the dark space was made by Schuster\*, who showed that if V is the difference of potential between the cathode and a point in the dark space or negative glow at a distance x from the cathode, then the relation

$$V = V_0 (1 - \epsilon^{-kx}),$$

where  $V_0$  is the cathode fall and k a constant (for constant pressure), represented very approximately the results of his experiments. This distribution of potential would, since  $\frac{d^2V}{dx^2} = -4\pi\rho$ , where  $\rho$  is the density of the free electricity, involve in the dark space the



existence of a positive charge of electricity, whose density decreases in geometrical progression as the distance from the cathode increases in arithmetical progression.

Graham+, who also measured the distribution of the electric

<sup>\*</sup> Schuster, Proc. Roy. Soc. xlvii. p. 526, 1890.

<sup>+</sup> Graham, Wied. Ann. lxiv. p. 49, 1898.

force in the dark space near the cathode in nitrogen, obtained for the distribution of potential results represented by the curves in Fig. 133. From these curves it would follow that although throughout the greater part of the dark space the electrical charge is positive, there is a layer of negative electricity just in front of the cathode. Wehnelt has repeated Graham's experiments without finding the nicks in the curve near the cathode; he ascribes them to the two exploring wires not being in the line of the current. Wehnelt gives the following figures as representing the distribu-

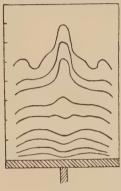


Fig. 134.

tion of the equipotential surfaces near the cathode; they probably are influenced to some extent by the walls of the tube. Both Schuster and Graham found that the electric force increased very rapidly close to the cathode; it was however very appreciable throughout the dark space. Skinner\*, in some recent experiments, came to the conclusion that the whole of the cathode fall takes place quite close to the cathode, and that the electric force in the rest of the dark space is exceedingly small. I think the latter result must be due to the exploring wire not having taken up the potential of the gas around it; for Strachan, using the method described on page 436, has found in agreement with Schuster and Graham that although the force increases exceedingly rapidly near the cathode, it is quite appreciable throughout the rest of the dark space.

233. The cathode fall of potential ceases to be constant when the negative glow covers the whole of the electrode, or when it

<sup>\*</sup> Skinner, Phil. Mag. vi. 2, p. 616, 1902.

reaches to the walls of the tube; its value under these circumstances is always greater than the normal fall and may rise to a very high value. Stark\* has given the following formula connecting the cathode fall of potential K with the intensity of the current when this is large enough to cover the whole of the cathode with negative glow

 $K = K_n + \frac{k}{pf^{\frac{1}{2}}}(C - xpf)^{\frac{1}{2}},$ 

where  $K_n$  is the normal cathode fall, p the pressure of the gas, f the area of the cathode, C the current through the tube, and k and k constants.

234. Thickness of the dark space. As the pressure diminishes the dark space gets broader and broader: the connection between the pressure of the gas and the width of the dark space has been investigated by Puluz†, Crookes‡, and more recently by Ebert§. According to Ebert the width of the dark space is not in general inversely proportional to the pressure of the gas, i.e. directly proportional to the mean free path of the molecules of the gas. The law found by Ebert when the cathode was so remote from the walls of the tube that the latter did not exert any restriction on the growth of the negative glow may be expressed as follows.

Let  $d_1$ ,  $d_2$  be the thicknesses of the dark space in the same gas at the pressures  $p_1$ ,  $p_2$  respectively, then

$$\frac{d_1}{d_2} = \left(\frac{p_2}{p_1}\right)^m,$$

where m is a positive quantity in general less than unity; he found that for the gases examined, air,  $O_2$ ,  $H_2$ ,  $N_2$ , CO, and  $CO_2$ , that there was a discontinuity in the relation between d and p when a certain pressure  $\Pi$ , different for the different gases, was reached, the value of m for pressures greater than  $\Pi$  differing from its value for lower pressures; thus to take oxygen as an example, Ebert found that for pressures greater than 7 mm. of Hg m had the value '459, while for lower pressures m was equal to '738. It is remarkable that the pressure '7 mm. is the pressure

<sup>\*</sup> Stark, Physikalische Zeitschrift, iii. p. 274, 1902.

<sup>+</sup> Puluz, Wien. Sitz. lxxxi. p. 874, 1880.

<sup>‡</sup> Crookes, Phil. Trans. clxx. p. 138, 1879. § Ebert, Wied. Ann. lxix. pp. 200, 372, 1899.

at which Bohr\*, Baly and Ramsay† found a discontinuity in the relation between the pressure and the volume of the gas to occur. Battelli‡ also obtained this result. Lord Rayleigh§ who made a very careful examination of the relation between the pressure and the volume of oxygen was unable to detect any such discontinuity. Newall $\parallel$  discovered that the electrodeless discharge through oxygen behaved very differently according as the pressure was greater or less than a certain critical pressure which was about 7 mm. Ebert¶ gives the following values for  $\Pi$ , the pressure at which the change in the law connecting p and d appears, and for d the thickness of the dark space at a pressure of 1 mm.

Gas	п	đ
$\begin{array}{c} H_2\\ CO\\ N_2\\ CO_2\\ Air\\ O_2\end{array}$	2·0 mm. 1·3 mm. 1·0 mm. 1·1 mm. 0·9 mm. 0·7 mm.	3·8 2·6 2·2 2·1 1·9 1·6

He states that  $\Pi$  is approximately proportional to the reciprocal of the linear dimensions of the cathode; if this is the case there seems no reason for connecting  $\Pi$  with the stage where there is a change in the relation between the pressure and volume of the gas.

235. The following results taken from Ebert's paper will give some idea of the thickness of the dark space d at different pressures p in different gases.

	Air	
$p \text{ in mm. of Hg} \mid 2.06 \mid d \text{ in mm.}  \mid 1.2 \mid$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	0.19
	Oxygen	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $

<sup>\*</sup> Bohr, Wied. Ann. xxvii. p. 459, 1886.

<sup>+</sup> Baly and Ramsay, Phil. Mag. v. 38, p. 307, 1894.

<sup>‡</sup> Battelli, Physikalische Zeitschrift, iii. p. 17, 1901.

<sup>§</sup> Rayleigh, *Phil. Trans.*, A. 196, p. 205, 1901.

Newall, Proc. Camb. Phil. Soc., ix. p. 295, 1897.

¶ Ebert, Verhand. Deutsch. Physik. Ges. ii. p. 99, 1900.

#### Hydrogen

p in mm. of Hg	3.05	2.04	1.37	0.95	0.72*	0.54	0.40	
d in mm	1.5	2.0	2.8	4.0	5.0	5.6	7.0	ı

## Nitrogen

p	*************	2.85	1.91	1.25	0.82	0.54*	0.35	0.26
d	***************************************	1.0	1.5	2.0	2.7	4.0	6.5	8.0

The results for hydrogen and nitrogen are plotted in Fig. 135, where the ordinates represent the thickness of the dark space and the abscissæ the reciprocals of the pressure. It will be seen that the points representing the experiments at the higher pressures lie very well on straight lines, while at lower pressures they no longer do so. The pressures when the curvature becomes marked are close to the pressures called by Ebert the 'critical pressure.' He found that as the pressure diminished the potential

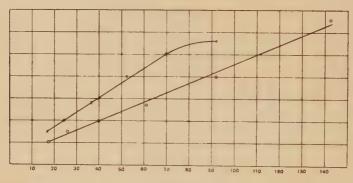


Fig. 135.

difference between the terminals at first diminished until this critical pressure was reached; when the pressure was still further reduced the potential difference increased as the pressure was diminished. The critical pressure was found to depend upon the size of the vessel, the larger the vessel the lower the critical pressure. The critical pressure marks the stage when the walls of the vessel begin to restrict the formation of the glow and to complicate the phenomena. In studying the laws governing the formation of the dark space it is better to confine ourselves to pressures higher than the critical pressure, when the walls of the tube do not exert any influence. Confining our attention to such pressures I am inclined to interpret Ebert's experiments somewhat differ-

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ently from Ebert himself. I think they show that d, the thickness of the dark space, may be expressed in the form

$$d = a + \frac{b}{p} \,,$$

where p is the pressure, and a and b are constants. If  $\lambda$  is the mean free path of a molecule of the gas,  $\lambda$  is proportional to 1/p, and the preceding equation may be written in the form

$$d = a + \beta \lambda \dots (1),$$

or the dark space measured from a distance a in front of the cathode is proportional to the mean free path of a molecule of the gas. If we plot the curve in which the ordinate is the thickness of the dark space and the abscissa the mean free path of a molecule of the gas, then taking  $\lambda$  for nitrogen at atmospheric pressure to be equal to  $9.86 \times 10^{-6}$  cm. and for hydrogen to  $1.85 \times 10^{-5}$  cm. (see Meyer, Kinetische Theorie der Gase), we find that the curves for hydrogen and nitrogen are almost identical; this indicates that in equation (1) the constants a and  $\beta$  are the same for the two gases, i.e. that if instead of measuring the dark space from the cathode itself we measure it from a constant distance from the cathode the thickness of the dark space bears to the mean free path of the molecules of the gas a ratio which is the same for all gases. The discharge in fact behaves as if the negative carriers came from a region a little in front of the cathode, and not from the cathode itself. H. A. Wilson's experiments on the current density at the surface of the cathode suggest the same view; the value of a, the constant in equation (1) as given by the curves in Fig. 135, is about 4 mm. The thickness of the layer at the surface, of which Wilson found the current density to be constant, is in air ·25 mm.: these two quantities are of the same order, and we. cannot claim for the value of a as determined by the curve in Fig. 135 any great accuracy, as a slight error in the observations might produce a large percentage error in a; for this reason I think it possible that the identity of the values of a found for hydrogen and nitrogen may be partly accidental, and more experiments are needed before it can be considered as established that a is the same for all gases. It would be interesting to see if the thickness of the velvety glow which covers the surface of the cathode is equal to a.

Connection between the thickness of the dark space and the free path of a corpuscle.

The mean free path of a hydrogen molecule at 0° C. and 760 mm. pressure is  $1.85 \times 10^{-5}$  cm. (Meyer, Kinetische Theorie der Gase). The mean free path of a corpuscle will be greater than this, first because the corpuscle is smaller than the molecule; if for the sake of definiteness we take the view that the collisions between two molecules and between a corpuscle and a molecule are analogous to those between two elastic spheres, then, neglecting the radius of a corpuscle in comparison with that of a molecule, the distance between the centres of a molecule and a corpuscle when in collision will be half the distance between the centres of two molecules when in collision. Now the free path is inversely proportional to the square of the distance between the centres when the spheres are in collision; thus the free path of the corpuscle will be four times that of the molecule. Again, under the electric field the corpuscles move with a velocity very great compared with the average velocity of translation of the molecules, so that the latter may be considered to be at rest. Maxwell\* has shown that the free path of a body moving through a collection of molecules at rest is  $\sqrt{2}$  times the free path if the molecules were moving with an average velocity of translation equal to that of the moving body; thus the mean free path of a corpuscle moving through hydrogen at 0° C. and 760 mm. pressure will be  $4\sqrt{2} \times 1.85 \times 10^{-5}$  cm.; the free path at a pressure of 1 mm. will therefore be  $4\sqrt{2} \times 1.85 \times 760 \times 10^{-5}$  cm., or about 8 of a milli-The thickness of the dark space in hydrogen at this pressure reckoned from a distance 4 mm. from the cathode is about 3.3 mm., or roughly 4 times the mean free path of the corpuscle, and we have seen that the proportion between the thickness of the dark space and the free path is probably the same at all pressures and in all gases. Thus the thickness of the dark space is a quantity of the same order of magnitude as the free part of a corpuscle calculated on the very special hypothesis used above.

Schuster<sup>†</sup> found that the thickness of the dark space depended to some extent on the current passing through the gas,

<sup>\*</sup> Maxwell, Collected Papers, vol. i. p. 386.

<sup>+</sup> Schuster, Proc. Roy. Soc. xlvii. p. 556, 1890.

increasing slightly with an increase in current. Wehnelt\* on the other hand found that the dark space contracted as the current increased; this seems to indicate that the dark space may have a stationary value for some particular current, increasing or decreasing with the current, according as the current is on one side or the other of this particular value.

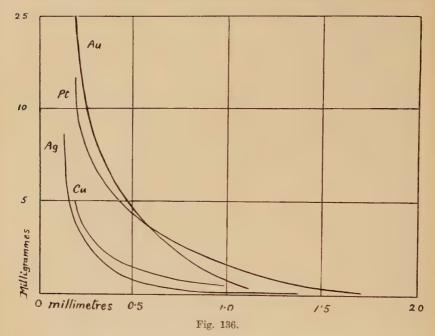
Disintegration of the cathode. When the discharge passes through the tube portions of metal shoot out normally from the cathode and form a thin metallic film on the walls of the tube or any body in the neighbourhood of the cathode; indeed thin metallic films for semi-transparent mirrors are now frequently made by placing a piece of glass in a vacuum tube near a cathode made of the metal it is wished to deposit and sending a current through the tube. The amount of metal shot off from the cathode depends on the pressure of the gas in the tube, it is much greater at low pressures than at high. It depends also on the nature of the gas; thus there is very little disintegration of aluminium electrodes in air, but a large amount in the monatomic gases, helium, argon and mercury vapour. It depends largely on the nature of the metal. According to Crookes+ the order of the metals in descending order of disintegration is Pd, Au, Ag, Pb, Sn, Pt, Cu, Cd, Ni, In, Fe. Granqvist to found that the order depended on the pressure of the gas. Thus at high pressures he found that Pt lost more than Au, at low pressures less. His results showing the connection between disintegration and pressure are represented by the curves in Fig. 136, where the ordinates are the loss of weight in milligrammes in an hour for electrodes 12 mm. long, 4.8 mm. broad, and 06 thick when a current of 2:46 milliampères passed through the tube, and the abscissæ the pressures. Granqvist found also that the loss in weight in a given time is proportional to the square of the current when the pressure is constant. Crookes found that if the cathode consisted of the alloy of gold and aluminium discovered by Roberts-Austen the gold was deposited while the aluminium was not; thus the composition of the cathode was changed by the discharge. The amount of metal volatilised from a cathode is very much greater than that from

<sup>\*</sup> Wehnelt, Physikalische Zeit. ii. p. 518, 1901.

<sup>+</sup> Crookes, Proc. Roy. Soc. l. p. 88, 1891.

<sup>‡</sup> Granqvist, Oefversigt. Kgl. Vetensk. Akad. Forh. Stockholm, 1898, p. 709.

the same wire when incandescent; thus Granqvist\* found that he got as much from a cathode in a few minutes as he got from the same wire when incandescent and without charge, or when used as



an anode, in twelve hours. The streams of metal from the cathode are deflected by a magnet, although not to anything like the same extent as the cathode rays.

238. The cause of this disintegration of the cathode has not been fully determined; it is possible that it is due to the same cause as the disintegration of incandescent wires, a very thin layer of cathode close to the surface being in a state analogous to that of a wire at a very high temperature; the surface of the cathode is bombarded by the positive ions which have fallen through a potential equal to the cathode drop; this might easily raise the surface layers to such a temperature that the energy would be radiated away and would not escape by conduction to heat the inside of the cathode. As a matter of fact the surface of the cathode is often to all appearance in a state of incandescence. It

<sup>\*</sup> Granqvist, Kgl. Akad. Stockholm, liv. p. 595, 1897.

would be interesting to test this view by seeing if the presence of even a trace of oxygen increased the disintegration of the cathode, as it produces a large increase in that of an incandescent wire. I am inclined to think, too, that gases absorbed in the metal have a considerable effect upon the disintegration and indeed upon the passage of the electricity from the cathode to the metal; in high vacua the potential difference between an anode and various cathodes in the same tube will often change capriciously, the order at one time being quite different from that a few minutes later. This would be readily explained if the amount of absorbed gas influenced the potential difference. If the disintegration does depend on absorbed gas, then we should expect the rate to fall off after long-continued use of a cathode in a high vacuum.

# The Faraday dark space and the Positive Column.

239. Measurements of the electric force in the Faraday dark space were first made by Hittorf\*. Graham† and H. A. Wilson‡ also made numerous determinations of the force in this as in other parts of the discharge, while Skinner§ has recently investigated the influence of pressure and of the magnitude of the current on the force in the dark space and on its length. The results of Skinner's experiments, which were made on carefully purified nitrogen,

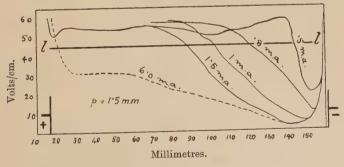


Fig. 137.

and with disc electrodes of considerable area, are represented in Fig. 137. An inspection of these curves shows that when

<sup>\*</sup> Hittorf, Wied. Ann. xx. p. 705, 1883.

<sup>+</sup> Graham, Wied. Ann. lxiv. p. 49, 1898.

<sup>#</sup> H. A. Wilson, Phil. Mag. [5], xlix. p. 505, 1900.

<sup>§</sup> Skinner, Phil. Mag. [5], l. p. 563, 1900.

the pressure is kept constant the width of the dark space increases as the current increases. (The boundaries of the dark space were found by Skinner to be at the points corresponding to the intersection of the straight line ll with the curves giving the electric force.) The current drives as it were the luminous positive column back on the anode, until with the largest current used the luminous positive column was reduced to a patch close to the anode. With the same current the width of the dark space is greater at low pressures than at high.

Skinner made an interesting experiment in which the gas in the tube was shielded from any disturbance travelling normally from the cathode. The cathode was a disc placed with its plane in the axis of the tube. This was surrounded by a piece of glass tubing, the axis of the tube being at right angles to the disc: thus any disturbance travelling from the cathode at right angles is prevented from reaching any but a small part of the gas between the electrodes. With this apparatus it was found that the luminous positive column occupied nearly the whole of the space up to the cathode: the dark space was very small, and increased but little with an increase in the current. Skinner observed that (with a tube of the normal type with the electrodes facing each other) when once by means of a large current the luminous positive column had been driven back on the anode, the gas took a considerable time before it recovered the power of transmitting a luminous discharge; the time required for the recovery depended upon the time the large current had been kept flowing through the tube. Skinner mentions times of one or two hours as having been required in some of his experiments.

The potential difference between the electrodes is represented by the area in Fig. 137, bounded by the axis of abscissæ, the two vertical ordinates through the electrodes, and the curve representing the electric force; we see from an inspection of the figure that this area diminishes as the current increases. Thus the curve representing the relation between the potential difference between the electrodes and the current through the tube slopes downwards. Hence to find the potential difference between the electrodes and the current through the tube when an external electromotive force  $E_0$  acts on a circuit including the tube, we pro-

ceed as in Art. 222 by drawing the line  $y = E_0 - Rx$ , where R is the external resistance in the circuit, and finding the points P, Q where this line cuts in the curve representing the relation between the potential difference and the current through the tube. For the reason given in Art. 222 the point P to the left corresponds to an unstable state, the other point Q to the stable one. in the case of the arc we see that with a given external electromotive force the current through the tube cannot sink below a certain finite value if the discharge is to be continuous\*.

Since with the exception of the cathode dark space the only dark part of the discharge is that where the curve representing the electric force is below the line ll (Fig. 137), it follows from Skinner's experiment that there is luminosity at all parts of the tube (with the exception of the cathode dark space), when the electric force exceeds a certain value depending on the pressure.

## The Positive Column.

The potential gradient along a uniform unstriated positive column is uniform; its value has been investigated by Hittorf+, A. Herz+, Graham, Wilson||, Skinner¶. The potential gradient in the positive column depends (1) upon the diameter of the discharge tube, (2) upon the pressure and nature of the gas through which the discharge is passing, and (3) the current passing through the gas.

The potential gradient diminishes as the diameter of the discharge tube increases, as the following table given by Herz (loc. cit.) shows. The influence of the size of the tube is not confined to tubes which are so narrow that their diameter is comparable with the mean free path of the molecules and corpuscles in the tube, but extends to the cases when the diameter of the tube is hundreds of times the mean free path. The results in the table relate to pure nitrogen; v is the potential gradient in volts per centimetre, 2R the diameter of the tube (the current

<sup>\*</sup> Kauffmann, Drude's Ann. ii. p. 158, 1900.

<sup>+</sup> Hittorf, Wied. Ann. xx. p. 726, 1883.

<sup>‡</sup> Herz, Wied. Ann. liv. p. 244, 1895.

<sup>§</sup> Graham, Wied. Ann. lxiv. p. 49, 1898.

<sup>||</sup> Wilson, Phil. Mag. [5], xlix. p. 505, 1900; Proc. Camb. Phil. Soc. xi. pp. 249, 391, 1902.

<sup>¶</sup> Skinner, Phil. Mag. [6], xi. p. 616, 1901.

passing through the tube was in all cases 1.2 milliampères), p is the pressure of the gas expressed in millimetres of mercury, and b the constant occurring in the equation

$$v - v_0 = -b (i - i_0),$$

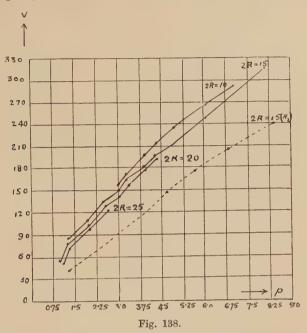
which Herz found expressed the relation between the gradients v and  $v_0$  corresponding to the currents i and  $i_0$ ; in this equation i and  $i_0$  are expressed in milliampères.

		v							
p	2R=10 mm.	2R=15 mm.	2R = 20 mm.	2R=25 mm					
8.0	***	156.8							
7.5		148.4	•••	•••					
7.0	144.4	140.1	***	***					
6.5	139.2	131.9	***	***					
6.0	132.6	123.8	***	• • •					
5.5	126.1	115.8	•••	•••					
5.0	118.2	107.8	***	***					
4.5	109.4	99.9	97.7	***					
4.0	99.7	$92 \cdot 2$	89.3	***					
3.5	89.2	84.5	80.5	***					
3.0	77.7	76.1	71.2	***					
2.5		66.2	61.5	00.0					
2.0		55.4	51.4	60.2					
1.5	•••	43.6	40.8	48.7					
1.0	0 + 0	100	29.8	37.5					
		***	29 6	26.9					
b	10.0	8.5	3.5	3.4					

The potential gradient in the positive column increases with the pressure, the results of Herz's experiments are represented by the curves in Fig. 138 in which the ordinates represent the potential gradient and the abscissæ the pressure, the dotted curve relates to experiments with hydrogen, the others to experiments with nitrogen in tubes of different dimensions, the curves seem very approximately linear. H. A. Wilson\* concluded from his experiments that the potential gradient in the positive column was proportional to the square root of the pressure; the linear relation v = a + bp, where v is the potential gradient, p the pressure

<sup>\*</sup> H. A. Wilson, Proc. Camb. Phil. Soc. xi. pp. 249, 391, 1902.

and a and b constants, represents the results of his experiments almost equally well.

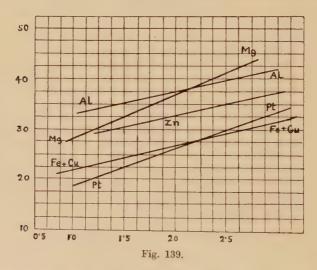


Herz showed that under similar conditions as to pressure and current the potential gradient in nitrogen was 1.4 times that in hydrogen. He found that a trace of aqueous vapour had no effect upon the gradient in the positive column, but that the presence of a small quantity of oxygen in the nitrogen increased the potential gradient.

- **241.** Relation between the potential gradient and the current. From the relation  $v v_0 = -b(i i_0)$  given by Herz it would follow that the potential gradient in the positive column continually increases as the current diminishes. H. A. Wilson has however shown recently that the potential gradient attains a maximum value for a certain value of the current and that when the current falls below this value the potential gradient rapidly diminishes.
- 242. When the positive column is striated the variations in the luminosity are accompanied by variations in the electric intensity,

the places of maximum luminosity are places of maximum potential gradient, this is clearly shown by the curve in Fig. 129, which is one given by Wilson for the striated discharge in hydrogen.

243. Anode drop in potential. Skinner\* has shown that there is a finite difference in potential between the anode itself and a point in the gas close to the anode. The magnitude of this drop in potential was investigated by him for the discharge through pure nitrogen; he found that it was independent of the current density, it increased slightly with the pressure, and depended upon the metal of which the anode was made, being greatest for aluminium and magnesium, for which the cathode fall of potential is least; the value of the anode drop at different pressures and for different metals is represented in the curves in Fig. 139. It will be observed that the anode drop is much smaller

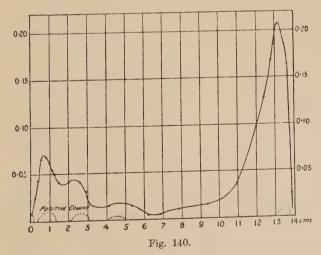


than the cathode one, it is also much more abrupt; there does not seem any region comparable in dimensions with the cathode dark space in which the drop of potential occurs; in none of the experiments hitherto made has it been found possible to get so close to the anode that the potential of the exploring wire differed by less than the anode fall of potential from the potential of the anode.

<sup>\*</sup> Skinner, Wied. Ann. lxviii. p. 752, 1899.

There is frequently a region in which the electric intensity is very small just in front of the anode; in some of the experiments made by H. A. Wilson, the electric intensity was apparently negative; we must remember that the introduction of the exploring wire disturbs the field, and that this reversal of the electric intensity may be due to this cause.

244. Number of ions at various points along the discharge. H. A. Wilson\* has made a series of investigations on this point; his method was to determine the current flowing between two small parallel platinum plates, the planes of the plates being parallel to the current flowing through the tube, a small potential difference (that due to one Clark's cell) was maintained between the plates, previous experiments having shown that with potential differences of this order the current was proportional to the potential difference, and therefore that the presence of a field of this intensity did not appreciably reduce the number of free ions. Under these circumstances if  $n_1$ ,  $n_2$  are the numbers of positive and negative ions respectively,  $k_1$ ,  $k_2$  the velocities of these ions under unit electric force, the current between the plates is proportional to  $k_1n_1 + k_2n_2$ . The results of Wilson's experiments



are represented in Fig. 140. It will be noticed that the current is very small in the cathode dark space, rises to its maximum value

<sup>\*</sup> H. A. Wilson, Phil. Mag. [5], xlix. p. 505, 1900.

in the negative glow, sinks again in the Faraday dark space and increases in the positive column, while in the striated discharge the current is a maximum in the luminous parts of a striation, a minimum in the dark ones.

**245.** It is interesting to compare the distribution of the electric intensity along the tube with these transverse currents. If X is the force along the tube, i the current through unit area, and if the velocity of the ions is proportional to the electric force at the point, then we have

$$X(k_1n_1 + k_2n_2) = i;$$

as i is constant along the tube,  $k_1n_1 + k_2n_2$  should be inversely proportional to X; as  $k_1n_1 + k_2n_2$  is proportional to the transverse current, we should expect the maxima for the transverse current to coincide with the minima for X. An inspection of the curves will show that this is not the case; thus the electric intensity in the Faraday dark space is less than in the positive column; the transverse current is also less, instead of being greater as indicated by the preceding reasoning. Again, both the electric intensity and the transverse current are greater at the bright parts of a striation than at the dark; in fact, luminosity seems to be accompanied by abnormally great transverse currents; it was this that led H. A. Wilson to suggest that the transverse current in the luminous parts was increased by secondary ionisation due to the illumination of the testing electrodes by the luminosity of the discharge. Skinner has suggested as another explanation for the discrepancy between the values of X and the transverse current that the velocity of the ions may not be proportional to the electric force; that, for example, though the electric force in the Faraday dark space is very small the ions there may be moving with high velocities which they acquired in moving through the strong electric field in the cathode dark space; thus the number of free ions necessary to carry the current may be very considerably less than that calculated from the assumption that the velocity was that due to the electric force in the Faraday dark space. If this were the explanation of the distribution of the transverse force, then the velocity of the ions in the Faraday dark space ought to be greater than in the uniform positive column. Now we can get information about the distribution of

the velocity of the ions at different parts of the tube by measuring the 'Hall effect.' H. A. Wilson\* has shown that when a magnetic force acts at right angles to the current passing through a vacuum tube, then a difference of potential proportional to the magnetic force is established between two electrodes, placed so that the line joining them is at right angles both to the current and to the magnetic force. The theory of this effect, called the 'Hall effect,' has been given in Art. 115; we showed that when equal quantities of positive and negative ions are present, then if Z be the difference of potential between two electrodes 1 cm. apart due to a magnetic force H, then

$$\frac{Z}{H} = \frac{1}{2} (u - v),$$

where u and v are respectively the velocities of the negative and positive ions. Thus a series of measurements of Z along the tube will enable us to deduce the distribution of velocities;

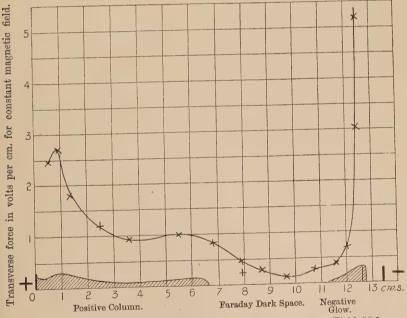


Fig. 141. Discharge in Air. Pressure 0.5 mm. Magnetic Field 22.1.

such measurements have been made by H. A. Wilson, and his results are represented in the curves given in Figs. 141 and 142.

<sup>\*</sup> H. A. Wilson, Proc. Camb. Phil. Soc. xi. pp. 249, 391, 1902.

It will be seen that the curves are similar in character to those giving the distribution of electric force; thus the value of Z in the Faraday dark space is less than in the positive column,

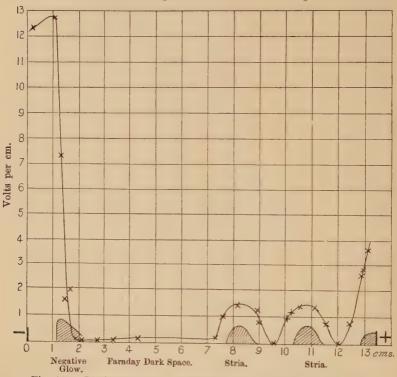


Fig. 142. Discharge in Air. Pressure 0.3 mm. Magnetic Field 29.4.

and in a striated discharge Z, like X, is a maximum at the bright parts of the striation, a minimum at the dark. These results seem to indicate that though a certain amount of lag between the values of X and the velocity of the ions is probable, especially at low pressures, it is not sufficiently large to explain the discrepancies between the curves for X and those for the transverse currents.

On Wilson's hypothesis that there is an additional ionisation due to the incidence of the light from the discharge on the metal of the electrodes, the current between electrodes made of wiregauze might be expected to be less than that between solid electrodes, as the area of metal exposed to the light is so much less in the first case than in the second.

246. The striated discharge. This form of discharge, examples of which are represented in Fig. 125, taken from papers by De la Rue and Müller\*, has from its very striking and beautiful character attracted a great deal of attention. It only occurs, or at any rate is only well developed, when the pressure of the gas and the current through the tube are within certain limits; it does not however depend upon the means used to produce the discharge; thus we get striations in discharges produced by induction coils, electric machines, or large batteries of storage or voltaic cells.

The striations are especially well developed in mixed gases, especially those which contain organic vapours, such as turpentine. Indeed some physicists consider they would not occur in perfectly pure gases+; it is however certain that they occur in gases which have been purified with the greatest care; according to Morren they do not occur in oxygen. Crookes to observed in a tube containing hydrogen three sets of striations, one set red, another blue, and the third grey; by spectroscopic examination he showed that the luminosity in the first set was due to hydrogen, that in the second to mercury vapour, and that in the third to hydro-It will be noticed from Fig. 125 that in some cases the striæ seem to occur in sets of two or three individual striæ situated quite close together. It will be seen that the luminous parts of the striæ are curved; the concavities being turned towards the positive electrode. When the tube is not of uniform width the striations are nearer together in the narrower than in the broad parts of the tube.

**247.** Investigations on the conditions determining the distance between successive striations have been made by Goldstein§, and by R. S. Willows||. Goldstein came to the conclusion that if d and  $d_0$  were the distances between the striations at the pressures p and  $p_0$ , then

 $\frac{d}{d_0} = \left(\frac{p_0}{p}\right)^m,$ 

<sup>\*</sup> De la Rue and Müller, Phil. Trans. 1878, pt. i. p. 155.

<sup>†</sup> E. C. Baly, Phil. Mag. xxxv. p. 200, 1893.

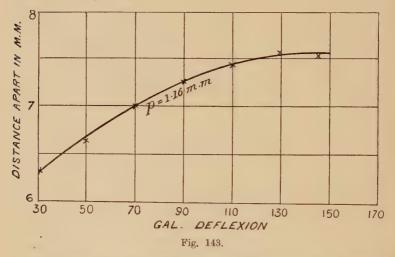
<sup>‡</sup> Sir W. Crookes, Proc. Roy. Soc. lxix. p. 399, 1902.

<sup>§</sup> Goldstein, Wied. Ann. xv. p. 277, 1882.

Willows, Proc. Camb. Phil. Soc. x. p. 302, 1900.

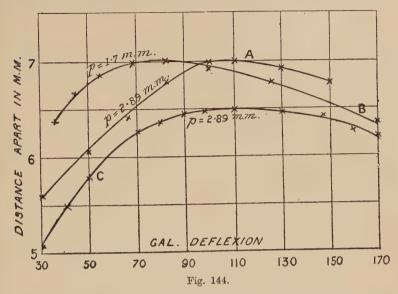
where m is a quantity less than unity (compare Art. 234). The distance between the striations increases as the pressure diminishes, but the percentage change in the distance is not so great as that in the pressure.

Willows found that in nitrogen the distance between the striæ increased with the current. Beginning with the smallest current capable of maintaining the discharge the distance at first increased very rapidly with the current. The rate of increase fell off however as the current increased; the connection between the current and the distance between the striæ in nitrogen is represented by the curve in Fig. 143.



In hydrogen the distance between the striæ at first increases with the current; it then attains a maximum, and then any further increase in the current produces a diminution in the distance between the striæ—the lower the pressure the smaller the current for which the distance between the striæ is a maximum. At very low pressures this current may be very little larger than the smallest current consistent with a continuous discharge, so that at these pressures the phase where an increase in current causes the striæ to separate may be almost effaced. The relation between the current and the distance between the striæ for hydrogen at two different pressures in a tube 12 mm. in diameter is shown in Fig. 144. The terminals for curves A and B were aluminium wires, for C they were aluminium discs.

By comparing these results with those for the thickness of the cathode dark space we see that under similar conditions as to



pressure and current the distance between the striæ is considerably greater than the thickness of the dark space.

248. Influence of the size of the discharge tube. The wider the tube the greater the distance between the striæ. According to Willows (l. c.) this distance is never greater than the diameter of the tube. When the striæ reach to the sides of the tube Goldstein showed that the ratio of the distances between the striæ for two given pressures is independent of the diameter of the tube. Another way of stating Goldstein's law is that the constant m which occurs in the equation

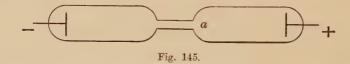
$$\frac{d_1}{d_0} = \left(\frac{p_0}{p_1}\right)^m$$

(see Art. 247) is independent of the size of the tube.

249. Influence of the nature of the gas. According to Willows the distances between the striæ in different gases under the same conditions as to pressure and current are not very different. At pressures between 1 mm. and 5 they are somewhat further apart in hydrogen than in air or nitrogen. The rate of alteration of the

distance with the pressure is however greater in the denser gases than in hydrogen. The range of pressure over which striations can be obtained is much greater in hydrogen than in air.

- 250. The striæ are most readily developed at the negative end of the positive column. Thus if the pressure be gradually reduced to that at which striation occurs, the first appearance of striation is the formation of a single stria at the end of the positive column. Successive striations are then formed until the whole of the positive column is striated. The stria at the negative end of the positive column always retains some individuality; thus its distance from its next neighbour is greater than the average distance; it is also often brighter than the other striæ.
- 251. Effect of a sudden contraction in the discharge tube. Goldstein\* found that in a tube with a constriction, such as that in Fig. 145, the end of the constriction next the anode behaved



like a cathode, i.e. that there was a dark space, negative glow, and Faraday dark space close to a; and that these were affected by a magnetic field in just the same way as if they had been produced by a metallic cathode. Lehmann† made a series of experiments with perforated diaphragms stretching across the discharge tube. He found on the side of the diaphragm next the anode the



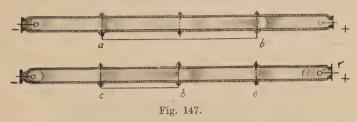
Fig. 146.

negative glow and the Faraday dark space; the cathode dark space was however absent. In the experiment represented in Fig. 146 the diaphragm was a porcelain sieve. He made other experiments with tubes having several perforated metallic diaphragms

<sup>\*</sup> Goldstein, Wied. Ann. xi. p. 832, 1880.

<sup>†</sup> Lehmann, Drude's Ann. vii. p. 1, 1902.

stretching across them. These diaphragms were connected with wires fused through the tube so that they could be connected up in various ways. If the diaphragms were all insulated the appearance of the discharge was as represented in Fig. 146. On the



anode side of each diaphragm there was the negative glow and the Faraday dark space, but no cathode dark space. If however two of the diaphragms were connected together by a metallic wire outside the tube, as Fig. 147, there was negative light but no dark space on the right of the diaphragms a and c; there was however a well defined dark space on the right of b. In this case some of the current instead of passing through the tube might pass through the wire outside, and at b would have, as at the cathode k, to pass from the metal to the gas. At the other diaphragms we may suppose the current went through the holes in the diaphragm.

252. Alternations in the luminosity of the discharge, similar

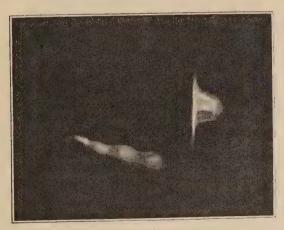


Fig. 148.

in appearance to those observed in the striated positive column at 30—2

low pressures, occur in certain cases in the discharge through gas at atmospheric pressure. Thus Töpler\* found that if several large Leyden jars were discharged across a spark gap, a plate of semi-insulating material such as basalt being inserted between the terminals, the portion of the discharge between the negative electrode and the plate showed distinct striations. Fig. 148 is copied from a figure given by Töpler. The discharge of an induction coil through the flame of a candle gives a bright discharge traversed by dark spaces as in Fig. 149.

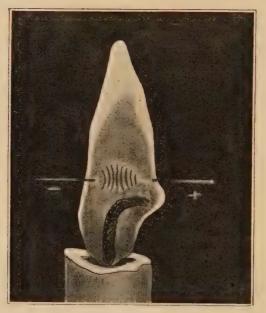


Fig. 149.

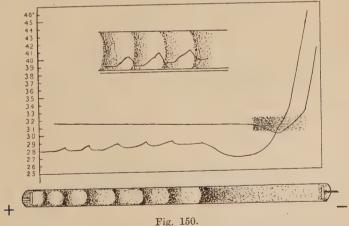
253. Distribution of temperature along the line of discharge. The average temperature of the gas in a discharge tube through which a luminous discharge is passing is often less than 100° C. Thus E. Wiedemann† proved that the average temperature of air at a pressure of 3 mm. in a tube conveying a luminous discharge was less than 100° C. Hittorf‡ measured the temperature in a discharge tube at three places, (1) in the positive column,

<sup>\*</sup> Töpler, Wied. Ann. lxiii. p. 109, 1897.

<sup>†</sup> E. Wiedemann, Wied. Ann. vi. p. 298, 1879.

<sup>#</sup> Hittorf, Wied. Ann. xxi. p. 128, 1884.

(2) in the negative glow and (3) in the Crookes dark space, and found that it was highest in (3) and lowest in (1). E. Wiedemann\* showed that the distribution of temperature along the tube depended materially upon the pressure, and that while at low pressures the temperature of the cathode was higher than that of the anode, the reverse was true at pressures greater than 26 mm. Wood+ made a very complete survey of the temperature in a discharge tube by means of a bolometer, which, floating on a barometer column of mercury, could be placed in any position in the tube. He found that in the unstriated discharge the temperature is constant in the positive column, diminishes in the Faraday dark space until it reaches a minimum just on the anode side of the negative glow, and then rapidly increases in the dark space next the cathode. In the striated discharge the temperature is greater in the luminous parts than in the dark. In no case did the bolometer indicate a temperature of more than 100° C. The bolometer temperature is of course the average temperature of all the molecules in a considerable space, and the fact that the average temperature is low does not preclude a few of the molecules possessing an amount of kinetic energy very much greater than that corresponding to the



temperature indicated by the bolometer. The distribution of temperature along the tube in a striated and an unstriated discharge is indicated by the curves in Fig. 150. It will be seen on com-

<sup>\*</sup> E. Wiedemann, Wied. Ann. x. p. 202, 1880.

<sup>+</sup> Wood, Wied. Ann. lix. p. 238, 1896.

paring these with the curves given for the distribution of electric force along the tube that the two curves are very similar. As the rate of work done by the current at any point of its path is proportional to the product of the current and the electric force, or since the current is constant, to the electric force, if all the work were converted into heat the curves for temperature would be similar to those for electric force. As this is very approximately the case we conclude that in tubes of moderate pressure the greater part of the electrical work appears as heat in the gas at places not very distant from where the work is done.

254. Action of a magnetic field on the discharge. It is convenient to consider separately the action of the magnetic force on the various parts of the discharge. We shall begin with the negative glow. Plücker\* showed that under a magnetic field the glow distributed itself in just the same way as a collection of iron filings, having perfect freedom of motion; thus the bright boundary of the negative glow coincides with the lines of magnetic force passing through the end of the negative electrode. This effect is illustrated in Figs. 151 and 152, which are taken from Plücker's

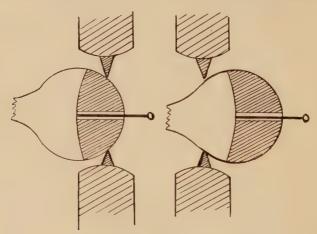


Fig. 151.

paper. In Fig. 151 the lines of magnetic force are transverse to the current, while in Fig. 152 they are more or less along it. The negative glow in fact behaves as if its luminosity were

<sup>\*</sup> Plücker, Pogg. Ann. ciii. p. 88, 1858.

produced by something moving along the lines of magnetic force. If the direction of the magnetic force is along the line

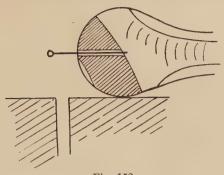


Fig. 152.

of discharge the negative glow spreads further down the tube

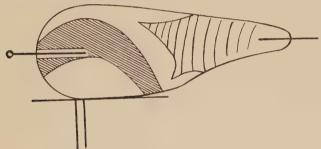
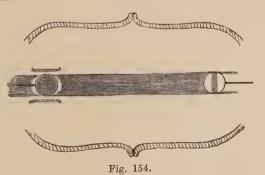


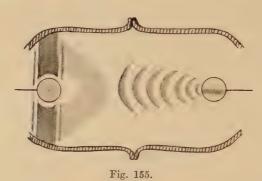
Fig. 153.

and the positive column is driven back; if the magnetic force



is at right angles to the tube, the negative glow follows the lines of force across the tube and does not extend so far down as when

there is no magnetic field; the positive column now comes further down the tube towards the cathode, and if it is striated new striations appear. These effects are illustrated by Figs. 154 and 155,



which are due to Lehmann\*. Fig. 154 represents the case when the magnetic force is along, Fig. 155 when it is across the tube.

255. Magnetic force affects the disposition of the glow over the surface of the cathode as well as its course through the gas. Thus Hittorf † found that when the negative electrode is a flat vertical disc and the discharge tube is placed so that the disc lies axially between the poles of a strong electromagnet, the disc is cleared of glow except on the highest point on the side most remote from the anode or the lowest point on the side nearest to it, according to the direction of the magnetic force. In another experiment Hittorf, using as cathode a metal tube about 1 cm. in diameter, found that when the axis of the cathode was at right angles to the line joining the poles of an electromagnet the cathode was cleared of glow in the neighbourhood of the places where the normals are at right angles to the lines of magnetic force. Both these results are what we should expect if the glow were due to charged particles projected normally from the cathode. The effect of a magnetic field on the disposition of the glow over the cathode has also been investigated by Schuster ...

256. The positive column is also affected by the magnetic field, the general effect being that the column is bent into a curve

<sup>\*</sup> Lehmann, Drude's Ann. vii. p. 1, 1902.

<sup>†</sup> Hittorf, Pogg. Ann. exxxvi. p. 221, 1869. Schuster, Proc. Roy. Soc. xxxvii. p. 317, 1884.

resembling the path of a positive particle under the action of the magnetic field and the electric force in the tube (see Art. 40). When the negative glow is deflected the positive column bends towards the place where the negative glow reaches the walls of the tube; this effect is shown in Fig. 156, which is due to Lehmann. There is often a dark space separating the ends of the negative glow and the positive column, as if the area of contact of the former with the glass acted like a secondary cathode.

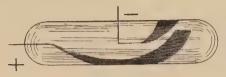


Fig. 156.

Effect of magnetic force on the striations. The influence of the magnetic field on the striations has been carefully studied by Spottiswoode and Moulton\*, and by Goldstein+; the conclusion they arrived at was that the bright parts of the striations, like the negative glow, set themselves along the lines of magnetic force, each bright part setting along the line of magnetic force passing through it and being separated by a dark space from its neighbour. As very important deductions have been made from this behaviour of the striæ, we quote the description of this effect given by Spottiswoode and Moulton and by Goldstein. former say: "If a magnet be applied to a striated column it will be found that the column is not simply thrown up or down as a whole, as would be the case if the discharge passed in direct lines from terminal to terminal threading the striæ in its passage. On the contrary, each stria is subjected to a rotation or deformation of exactly the same character as would be caused if the stria marked the termination of flexible currents, radiating from the bright head of the stria behind it and terminating in the hazy inner surface of the stria in question. An examination of several cases has led the authors of this paper to conclude that the currents do thus radiate from the bright head of a stria to the inner surface of the next, and that there is no direct passage from one terminal of the

<sup>\*</sup> Spottiswoode and Moulton, Phil. Trans. Part 1. p. 205, 1879.

<sup>†</sup> Goldstein, Wied. Ann. xi. p. 850, 1880.

tube to the other." Goldstein gives the following description of the behaviour of the striated column under magnetic force: "The appearance is very characteristic when in the unmagnetized condition, the negative glow penetrates beyond the first striation into the positive column. The end of the negative glow is then further from the cathode than the first striation or even, if the rarefaction is suitable, than the second or third. Nevertheless the end of the negative glow rolls itself under the magnetic action up to the cathode in the negative curve which passes through the cathode. Then separated from this by a dark space follows on the side of the anode a curve in which all the rays of the first striation are rolled up, then a similar curve for the second striation, and so on." We shall have occasion to refer to this point again when we consider the theory of the discharge.

258. Paalzow and Neesen\*, who investigated the effect of a magnetic field in helping or retarding the discharge, found that when the lines of force are parallel to the line of discharge, the nature of the effect depends upon pressure; if  $p_0$  is the pressure at which the discharge first begins,  $p_m$  the pressure when the current through the tube is a maximum, and  $p_n$  the lowest pressure at which the discharge passes, then for pressures between  $p_0$  and  $p_m$  the magnetic force retards the discharge, while if the pressure is between  $p_m$  and  $p_n$  it helps it; thus the magnetic field produces in this case the same effect as an increase in pressure. The same results are true if the anode alone is exposed to the magnetic force; if only the cathode is exposed to this force the preceding results hold if the field is weak; if the field is very strong, however, the effects produced are just the opposite, the magnetic field producing the same effect as a diminution in pressure.

When the lines of magnetic force are at right angles to the discharge the magnetic field at all pressures retards the discharge. They found that the effect of the magnetic field was not instantaneous, often taking several seconds before producing its normal effect. This lag is a very frequent phenomenon in the discharge tube; it generally can be explained by the effects produced by previous sparks; thus as it is easier for one discharge to follow

<sup>\*</sup> Paalzow and Neesen, Wied. Ann. lxiii. p. 209, 1897.

another than to be the first to pass through the tube, the magnetic field might not be able at once to stop the discharge if a strong discharge had just previously passed through the tube, though it might be able to prevent a discharge starting in the tube.

The author showed many years ago that the passage of the electrodeless discharge was hampered by a transverse magnetic field and facilitated by a longitudinal one.

Willows\*, who also investigated the effect of a transverse magnetic field on the potential difference between the terminals of a discharge tube containing gas at a low pressure, found that when the magnetic force is confined to the neighbourhood of the cathode the potential difference is diminished by the magnetic field when the pressure is low and increased when it is high. The effect is represented in the curves in Fig. 157, the scale of

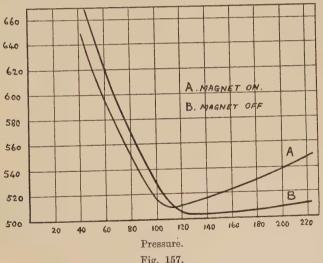
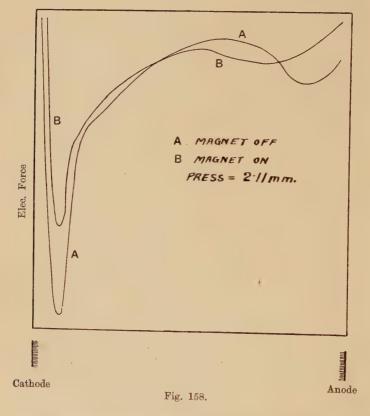


Fig. 157.

pressures is such that a pressure of 1 mm. of mercury is represented by 223. The pressure at which the curve for the magnet on intersects that for the magnet off, increases as the magnetic force increases and decreases when the current through the tube decreases. When the magnetic force is concentrated at any part of the tube except the cathode it always increases the potential difference.

<sup>\*</sup> Willows, Phil. Mag. vi. 1, p. 250, 1901.

Willows also investigated the effect of a uniform transverse magnetic field on the distribution of electric force between the terminals, the results of his experiments are represented by the curves in Fig. 158; the magnetic field diminishes to a considerable extent the great drop in the electric force which occurs in the negative glow.



260. Birkeland\* has shown that in a tube containing gas at a very low pressure a strong magnetic force parallel to the line of discharge produces an enormous diminution in the potential difference required to spark through the tube; the potential difference when the magnetic force at the cathode reaches a critical value falling to less than one-tenth of its previous value. Almy† has shown

<sup>\*</sup> Birkeland, Comptes Rendus, exxvi. p. 586, 1898.

<sup>+</sup> Almy, Proc. Camb. Phil. Soc. xi. p. 183, 1901.

that this effect can be produced by a transverse magnetic force as well as by a longitudinal one, and that the sudden diminution in potential is accompanied by a change in the appearance of the discharge, the magnet causing the discharge to change from a form in which it passes from the whole of the cathode to one where it is concentrated in one or more bright streams. This change in the appearance of the discharge, and also the diminution in the potential difference between the terminals, can be produced without the aid of the magnet by covering the outside of the tube in the neighbourhood of the cathode with tinfoil connected with the cathode. Almy showed that the effect of the magnet did not arise from the charges of statical electricity which accumulate on the glass of the tube, by showing that it took place when the cathode was placed inside a metal cylinder which was used as the anode.

261. We have already (see p. 358) described the appearance presented by the discharge when the terminals are placed very near together, an interesting modification of such an experiment is shown in Fig. 159, which represents an experiment made by

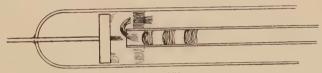


Fig. 159.

E. Wiedemann\* in which the anode was enclosed in a narrow glass tube which dipped into the cathode dark space; it will be noticed that the positive light turns round after leaving the tube and joins the negative glow.

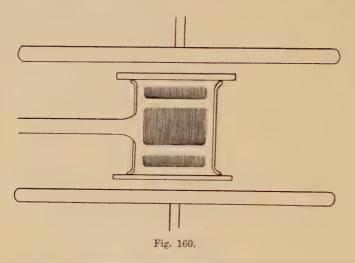
262. Discharge produced by very rapidly alternating electromotive forces. E. Wiedemann and Ebert<sup>†</sup> and Himstedt<sup>‡</sup> have made some very interesting experiments when the discharge was sent through the tube by the very rapidly alternating forces produced by discharging a condenser; in Wiedemann and Ebert's experiments the terminals were connected with the terminals in a Lecher's bridge arrangement producing electrical oscillations

<sup>\*</sup> E. Wiedemann, Wied. Ann. lxiii. p. 242, 1897.

<sup>†</sup> E. Wiedemann and Ebert, Wied. Ann. 1. pp. 1, 221, 1893.

<sup>#</sup> Himstedt, Wied. Ann. lii. p. 473, 1894.

whose time of swing was only about  $10^{-8}$  seconds. In Himstedt's experiments the alternating forces were produced by a Tesla transformer. The appearance presented by the tube is shown in Fig. 160; it will be seen that both electrodes show only the phenomena associated with a cathode, *i.e.* we have the dark space, the negative glow, and the Faraday dark space, but no



positive light; the latter is represented by the luminosity, in the middle of the tube; this disappears at very low pressures. The thickness of the dark space next the electrode diminishes as the rapidity of the oscillations increases.

## CHAPTER XVI.

THEORY OF THE DISCHARGE THROUGH VACUUM TUBES.

WE shall now proceed to apply the theory given on p. 376 of the spark discharge to explain some of the phenomena observed when the discharge passes through a vacuum tube containing gas at a low pressure. We have regarded the spark discharge as originating in the ionisation of the gas by moving ions, the small negative ions—the corpuscles—being more efficient ionisers than the positive ones, which have a greater mass. If, however, the ionisation in an electric field not exposed to external ionising agents, such as Röntgen rays, were solely due to the collisions of corpuscles with the molecules of the gas we could not have a continuous current through the gas. For suppose, to begin with, there were a few corpuscles between the electrodes, then if the negative electrode is on the right the electric field will set the corpuscles moving to the left, and if it were strong enough ionisation would occur between the positive electrode and the place from which the original corpuscles started. The new corpuscles produced by the collisions of the original ones with the molecules of the gas would themselves produce new ions, but all these would be formed to the left of the birth-place of the ions which produced them, there would thus be a gradual exodus of corpuscles towards the positive electrode while the gas round the negative electrode would in time be deprived of corpuscles and would cease to conduct, and by hypothesis it could no longer be ionised as all the negative ions would have been driven to the positive electrode.

We have seen that in every gas 'spontaneous' ionisation is continually taking place, and it might be urged that this process would furnish a supply of negative ions which would rapidly multiply by collisions with the molecules of the gas, and so furnish a supply of carriers sufficient for the current through the tube. If this were the case however the potential difference between the electrodes would vary rapidly with the current, in reality however the variation is very slight.

Again, the current under a given difference of potential would depend upon the amount of the spontaneous ionisation, *i.e.* the ionisation independent of the electric field; we can however increase the latter a hundredfold by exposing the gas in the discharge tube to the action of Röntgen rays without producing any appreciable increase in the current passing through the gas. To account for the phenomena of the discharge we must have ionisation produced by the electric field itself close to the cathode; we shall suppose that this ionisation is produced by the positive ions, and although these require a much greater amount of energy before they can act as ionisers than do the corpuscles, yet the very intense electric field which exists close to the cathode is sufficient to give them, when under its influence they have come up to the cathode, all the energy they require.

There are several ways in which these rapidly moving positive ions might produce fresh negative ions; the two that most naturally suggest themselves are, (1) that the positive ions by collision ionise the molecules of the gas near the cathode, (2) that the positive ions by striking against the surface of the cathode communicate so much energy to the corpuscles contained in the layer of metal close to the surface of the cathode that they are able to escape from the metal, just as they are able to escape from a metal when it is raised to incandescence.

The consequences will be very much the same whichever of these views we take; for the strength of the electric field increases so quickly near the surface of the cathode that the kinetic energy possessed by the positive ions, when they arrive quite close to the surface, will be enormously greater than when they are just a little further off, so that any ionisation produced by the collision of these positive ions with the molecules of the gas will be practically confined to the layer of gas close to the surface of the

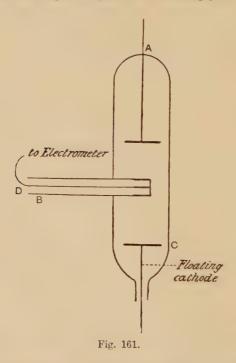
cathode. It is possible that the luminous glow which spreads over the cathode marks the seat of this ionisation. Thus whether we suppose the positive ions to act according to the method (1) or (2) we have negative ions starting from close to the surface of the cathode; these are driven from it by the electric field and soon acquire such velocities that they ionise the gas through which they pass, producing a supply of positive ions which are attracted by the electric field up to the cathode, there to produce a fresh supply of negative ions.

Thus the positive and negative ions in the space close to the cathode are on this view mutually dependent; if the supply of either is stopped, that of the other at once fails. This is very well illustrated by the experiment represented in Fig. 110, p. 384, in which an obstacle placed in the dark space throws a shadow as it were backwards and forwards; the obstacle stops the supply of positive ions to a portion of the cathode (the portion in shadow); this portion is no longer able to send out negative ions, in fact it ceases to act as an electrode.

## Origin of the dark space.

264. Let us now consider in more detail the ionisation produced by the negative ions coming from the cathode. The primary ones which start from or near the surface will in consequence of the very intense electric field which exists close to the cathode be shot out with very great velocity, they will therefore be cathode rays of a very penetrating kind; such rays in a given length of path do not produce so much ionisation as those moving with a smaller velocity. Let us now consider the case of a corpuscle produced by the collision of one of the primary ones with a molecule some little distance in front of the cathode; this 'secondary' corpuscle will start from a field much less intense than that from which the primary corpuscle started, it will therefore not acquire nearly so great a velocity; it will correspond to a much more easily absorbed kind of cathode ray, and will therefore in a given length of path produce many more ions. Again, the corpuscles produced by the 'secondary' corpuscles or by the primary ones at a greater distance from the cathode will in consequence of their smaller velocity be still more easily absorbed, and therefore produce still more ions per unit of path. Thus the amount of ionisation will be small in the strong parts of the field near the cathode, but will increase with great rapidity when we get to the weaker parts. Thus if ionisation were accompanied by luminosity the places close to the cathode where the electric field is strong would be dark, while the luminosity would increase with very great rapidity in the places more remote from the cathode where the electric field is weaker; the increase would be so rapid that the contrast and line of demarcation between the light and dark places would be sharply marked.

265. The scarcity of the negative ions in the strong field close to the cathode and their rapid increase in the weaker parts of the field towards the negative glow are strikingly shown in some



experiments made by the writer\*. In these a discharge tube was used similar to that shown in Fig. 161, C is a floating cathode which can be raised or lowered in the tube, A is the anode, and B

<sup>\*</sup> J. J. Thomson, Phil. Mag. vi. 1, p. 361, 1901.

a closed metal vessel provided with a window covered with very thin aluminium foil. The impact of negative ions on this window was found to generate rays which penetrated the tinfoil and ionised the gas in the closed vessel. This gas therefore conducted electricity, and if the electrode D was charged and connected with an electrometer, the charge leaked from it, the rate of leaking indicating the amount of ionisation in the gas, care being taken to charge up the electrode to a sufficiently high potential to produce the saturation current through the gas. The rays are very easily absorbed, this is clearly shown by diminishing the pressure of the gas in the closed vessel B and observing the rate of leak at different pressures. As long as the rays are entirely absorbed in passing through the gas in the vessel, the number of ions in the vessel, and therefore the saturation current, will be independent of the pressure of the gas; as soon however as the pressure gets so low that the rays pass through the gas without much absorption, the saturation current becomes proportional to . the pressure. The following table, which gives the variation of the saturation current with the pressure, shows that it is not until the pressure gets low that the saturation current is affected by the pressure, hence we conclude that the radiation produced by the impact of the negative ions against the window can only penetrate through a few millimetres of air at atmospheric pressure:

Pressure in vessel $D$ (thickness of vessel 1 cm.)	Saturation current
770 mm. 270 ,, 100 ,, 45 ,, 10 ,, 5 ,,	87 90 64 37 11 3

The intensity of the rays produced by these negative ions depends very much upon the distance of the window from the cathode. This is clearly shown by the following table, the results of which are represented by the curve in Fig. 162, in which the ordinates represent the amount of ionisation in the vessel and the abscissæ the distance from the cathode.

Pressure in discharge tube 6 m. Width of dark space 6 mm.

Distance of window from surface of cathode	Ionisation in vessel D (arbitrary units)
3	21
4	54
5	105
6	195
8	150 ?
10	180
20	66
30	40
40	25

It will be seen that the effect of the rays produced by the impact is small close to the cathode, increases very rapidly as we approach the negative glow, attains a maximum in the glow, and then

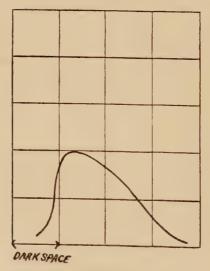


Fig. 162.

quickly drops down to a very small value; in fact the effect produced by the collision of the negative ions against the window varies in the way that we have described for the amount of ionisation produced by the collision of the corpuscles with the molecules of the gas.

**266**. The fact that the ionisation inside the vessel *D* increases and decreases with the luminosity in the discharge might lead to the suspicion that the ionisation inside D was not due to rays generated by the impact of negative ions against the window, but to the light coming from the gas; that it is in reality due to the former and not to the latter cause is shown by the following experiment. The tube was placed in a field of magnetic force, the lines of magnetic force being parallel to the window in the box D; the magnetic field concentrates the negative glow and increases its luminosity, so that if the ionisation in the box were due to the luminosity and not to the impact it should be increased by the magnetic field; on the other hand, since the negative ions move parallel to the lines of magnetic force, and therefore parallel to the window, the impact of the ions against the window is stopped, so that if this is the cause of the ionisation inside the box it should be very much diminished by the field; on trying the experiment it was found that the magnetic field almost entirely stopped the ionisation.

267. On the theory we are discussing the negative glow is due to the ionisation brought about by collisions between molecules of the gas and corpuscles which have started some distance from the cathode, such corpuscles being the descendants, so to speak, of the corpuscles which started from close to the cathode and which move with very much greater velocity than the glow-producing corpuscles which have started in a much weaker electric field. The thickness of the dark space will evidently be greater than the mean free path of a corpuscle, for this would be the approximate magnitude of the dark space if the negative glow were produced by collisions with the corpuscles from the cathode; the greater the mean free path the further will the negative glow be from the cathode, and we should expect from the preceding theory a linear relation between the thickness of the dark space and the mean free path.

The corpuscles which start from close to the cathode being but little absorbed may sometimes pass right through the negative glow, as in the case of the discharge studied by E. Wiedemann and represented in Fig. 124, p. 432. These corpuscles are the cathode rays which we shall discuss in the next chapter.

268. When ionisation takes place in the region round the cathode the positive ions move towards the cathode, while the negative ones move away from it; this produces an excess of positive electricity in the gas near the cathode. In consequence of this positive charge the electric force diminishes as we recede from the cathode. When the electric field sinks below a certain value it can no longer communicate to the corpuscles sufficient energy to make them act as ionisers, so that after the field has sunk to this value the ionisation will cease; it would be more accurate to say that the ionisation will cease soon after the field has reached this value, for the corpuscles may retain for some little distance the energy they acquired in stronger parts of the field and so continue to act as ionisers for a short distance in the weak field. The limit of the negative glow, furthest from the cathode, marks on our view the place where ionisation ceases.

269. Let us now consider what would happen in the gas between the anode and the negative glow g. Let us suppose for a moment that there is no ionisation taking place between g and the anode. Then as the current will be carried by ions dragged by the electric field from the region of ionisation between g and the cathode, all the ions between g and the anode will be negative ions, so that there will be a negative charge in the gas to the left of g; but a negative charge involves an increase in the electric force as we go from g towards the anode, and if the anode is far enough away the electric field may increase to such an extent that it is again able to give to the negative corpuscles sufficient kinetic energy to make them ionisers. When this happens the gas again becomes luminous, and we have in fact a repetition of the process occurring in the negative glow. The increased ionisation in the luminous part of the discharge will diminish the strength of the electric field until this gets so weak that no further ionisation takes place, the luminosity again ceases and the current will again, as in the Faraday dark space, be carried by ions produced elsewhere; there will also, as in that space, be an excess of negative ions, this will cause the electric force again to increase, ionisation accompanied by luminosity will recur, and the process will be repeated right up to the anode; we thus get bright and dark patches as in the striated positive column. On this view the luminous portions of the striations correspond to the negative

glow, the intervening dark spaces to the Faraday dark space, the process taking place along the positive column being a repetition of that taking place near the cathode. The similarity between the striated positive column and the phenomena at the cathode has been insisted on by several observers, notably by Spottiswoode and Moulton\*, Goldstein†, and Lehmann‡. Goldstein's statement is very clear and explicit, he says, "Jede einzelne Schicht des positiven Lichtes ist ein dem früher sogenannten negativen oder Kathodenlichte entsprechendes Gebilde, und das geschichtete positive Licht besteht eigentlich aus einer Aufeinanderfolge von Komplexen negativen Lichtes§." Several observers have regarded the behaviour of the positive column as necessarily implying a discontinuity in the discharge. Thus Spottiswoode and Moulton from the behaviour of the striated column liken the transmission of electricity along the positive column "to an action consisting of an independent discharge from one stria to the next, and the idea of this action can perhaps be best illustrated by that of a line of boys crossing a brook on stepping stones, each boy stepping on to the stone the boy in front of him has left." On the view we have indicated above a striated discharge need not necessarily be discontinuous.

270. We saw in Art. 35 that when the velocity of the ions is proportional to the electric force the curve representing the relation between the electric force at a point and the distance of that point from one of the electrodes is convex to the axis when the ionisation in the gas is greater than the recombination of the ions, and concave when it is less. The curve representing the distribution of electric force along the striated positive column is however (see Fig. 129) concave at the bright parts of the striæ where we have supposed the ionisation to be greatest, and convex at the dark parts where the ionisation is least. In a case, however, like that of a striated discharge where the pressure of the gas is low, and the free path of a corpuscle therefore considerable, the velocity of a corpuscle at a point will depend not only upon the magnitude of the electric force at that point, but also upon the forces which acted upon it before it reached the point: thus

<sup>\*</sup> Spottiswoode and Moulton, Phil. Trans. Part 1. p. 205, 1879.

<sup>†</sup> Goldstein, Wied. Ann. xi. p. 831, 1880; xii. pp. 90, 249, 1881.

<sup>‡</sup> Lehmann, Die Elektrischen Entladungen.

<sup>§</sup> Goldstein, Berlin. Monatsber. May 4, 1876.

the conditions upon which the investigation in Art. 35 is based need not apply in this case.

- 271. Case when the discharge is not striated and the positive column is of uniform intensity. The corpuscles are continually recombining, so that unless there is fresh ionisation their number is continually diminishing: if the rate of ionisation is equal to that of recombination the number of corpuscles will remain constant. Thus if, when the ionisation begins at the anode end of the Faraday dark space, the strength of the field is such that the number of ions produced by it in unit time is just equal to the number which recombine in that time, the number of ions, the strength of the field, the amount of ionisation, and therefore the luminosity will be constant all along the line of discharge, and we shall have the case of the uniform positive column.
- Anode fall of potential. Let us consider a point P close to the anode A, then the current at P is carried by negative corpuscles produced further from the anode than P and by positive ions either coming out of the anode or produced from the gas between P and A. That a considerable supply of positive ions is produced within a short distance of the anode is proved by the fact that in the uniform positive column the electric force is constant within a short distance of the anode, and when this is the case there are as many positive as negative ions per unit volume of the gas. Thus if the ions are produced in the gas the ionisation in the gas near the anode must be so intense that in an exceedingly thin layer of gas there are sufficient positive ions produced to neutralise the electrostatic effect of the negative ones moving up to the anode. Now under these conditions, if i is the current,  $R_1$ ,  $R_2$  the velocities of the positive and negative ions respectively, the number of positive ions which cross unit area of the uniform positive column in unit time is  $R_1i/(R_1+R_2)e$ , where e is the charge on an ion. Suppose w is the work required to ionise a molecule of the gas, then in the thin layer referred to an amount of work equal to  $wR_1i/(R_1+R_2)e$  must be done by the electrical field in unit time; but if V is the difference of potential between the two sides of this layer (one of these sides is the anode), the electrical work done in unit time is  $VR_2i/(R_1 + R_2)$ , since the quantity of negative electricity entering this layer in unit time

is  $R_2i/(R_1+R_2)$ ; hence supposing all the electrical work is spent in ionising the gas, we have

$$\begin{split} \frac{VR_{_{2}}i}{(R_{_{1}}+R_{_{2}})} = & \frac{R_{_{1}}wi}{(R_{_{1}}+R_{_{2}}) \ e}, \\ Ve = & \frac{R_{_{1}}}{R_{_{2}}}w; \end{split}$$

or

this is an inferior limit to V, since it is obtained on the assumption that all the work is spent in ionising the gas: we have thus a finite drop in the potential at the anode. If we proceed on the other supposition, that the positive ions come from the anode, just as we have seen positive ions do come out of metal or out of the gases absorbed by metal when the temperature is above a dull red heat, the preceding investigation will still apply, if w stands for the energy required to eject an ion from the metal, so that in this case again there is a finite drop of potential at the anode.

273. Action of magnetic force upon the discharge. We have seen (see Art. 40) that when a charged particle moving through a gas is acted upon by both electric and magnetic forces, it will follow the lines of magnetic and not of electric force, provided RH is a large quantity; here H is the magnetic force, and R the velocity acquired by an ion under unit electric force. Another way of expressing the same result is to say that a charged particle, moving with the velocity v, will follow the lines of magnetic force if mv/eH, the radius of the circle into which the path of a free particle is bent when moving at right angles to the magnetic force, is small compared with the mean free path of the particle. The result when put in this form is obvious, since (see p. 82) the free paths of the particles are spirals round the lines of magnetic force, and as the radii of these spirals are small compared with the length of the mean free path the only direction in which the particles make any appreciable progress is that of the magnetic force. The negative particles will be much more likely than the positive to follow the lines of magnetic force; for in the first place, the mean free path of the negative particles is greater than that of the positive, and secondly, the value of m/e is much less for the negative than for the positive particles. Thus we may expect the negative particles to follow the lines of magnetic force, even when the motion of the positive ones is but little affected by the magnetic field. The tendency of the negative particles to follow the lines of magnetic force is strikingly shown by the behaviour of the negative glow in a strong magnetic field, when, as Plücker has shown (see p. 470), the boundary of the glow coincides with a line of magnetic force.

Since the negative particles are much more affected than the positive by a magnetic field, if the proportion of the current carried by the negative ions varies at different points in its course the current will be much more deflected by the magnetic field in some places than in others. This is exactly what happens in the striated discharge; for suppose A and B are the bright parts of two consecutive striæ, then since by hypothesis there is ionisation in A, many more negative particles will leave A from the anode side than enter it from the cathode side; thus the proportion of the current carried by the negative ions will be much greater on the anode side of the bright patches than on the cathode side; the portion of the current on the anode side of a bright patch will therefore be much more affected by the magnetic field than that on the cathode side: the general effect of this will be much the same as if the current were discontinuous, and this, as we have seen (see p. 473), corresponds to the behaviour of the striated column in the magnetic field.

275. Effect of a constriction in the tube. Goldstein (see p. 466) has shown that on the anode side of a constriction we get negative glow; this is what we should expect on the preceding theory, for the electric force in the constriction will be greater than in the wider parts of the tube: there are several lines of reasoning by which we may show that this must be the case; in the first place the current density in the constriction is greater than in the rest of the tube; thus if there are in the constricted part the same number of ions per cubic centimetre as elsewhere, the velocity of the ions must be greater; for this to be the case the electric force must be greater also; or again, if the density of the ions is greater in the constriction than in the wide parts of the tube, then since the ions are produced by the electric field the larger number of ions will involve a more intense electric field. Thus, as the force in the constriction is greater than in the rest of the tube the

corpuscles which emerge from the constriction on the anode side will in the constriction have acquired a large amount of kinetic energy, and will therefore, like the corpuscles in the negative glow, produce great ionisation with its attendant luminosity.

Effect of pressure upon the electric force. We shall consider the case of a continuous positive column: in this case the reasoning given in Art. 193 applies, where it is shown that if  $\lambda$  is the mean free path of a corpuscle and X the electric force, then  $X\lambda$  is constant; in an unlimited gas  $\lambda$  is inversely proportional to the pressure; hence in this case we should have X proportional to the pressure. In the case of a gas contained in a tube the mean free path will be somewhat diminished by the restraint imposed by the tube; this diminution will be specially marked when the pressure of the gas is low and the tube narrow. If  $\lambda'$  is the mean free path of the corpuscle in the tube and  $\lambda$  the free path in an unlimited gas at the same pressure, then since  $\lambda'$  is less than \(\lambda, X\), the electric force in the tube, will be greater than that in the free gas. This agrees with experience, as we find the potential gradient greater in small tubes than in large ones. Without calculating the expression for the mean free path by a rigorous method we can easily in a general way see how the tube will affect the potential gradient. For if d is the diameter of the tube, then when d is large compared with  $\lambda$ ,  $\lambda'$  is very approximately equal to  $\lambda$ ; while when d is small compared with  $\lambda$ ,  $\lambda'$  is comparable with d; this condition will be satisfied if

$$\frac{1}{\lambda_1} = \frac{a}{d} + \frac{1}{\lambda},$$

where a is a constant. Since  $X\lambda'$  is constant, we have X proportional to  $\frac{1}{\lambda_1}$ , or since  $1/\lambda$  is proportional to p the pressure, we have X = A + Bp, where A and B are constants.

277. We have hitherto supposed that the ionisation in the discharge tube was entirely due to the collisions of the ions with the molecules of the gas: there is, however, another source of ionisation. E. Wiedemann\* discovered that an electric spark emits something which is propagated in straight lines, is stopped

<sup>\*</sup> E. Wiedemann, Zeitschr. f. Electrochemie, p. 159, 1895.

by all solids and liquids, and which possesses the power of exciting thermoluminescence (see p. 496) in suitable bodies; he called this radiation from the spark 'Entladungstrahlen.' Hoffmann\*, who subsequently investigated this question, showed that 'Entladungstrahlen' are emitted by discharges through vacuum tubes as well as by sparks, and that this radiation is not deflected by a magnet; he found that the radiation is absorbed by carbonic acid gas to a much greater extent than by oxygen. The writer+ showed that these 'Entladungstrahlen' possess the power of ionising the gas through which they pass, so that a part, though often only a small part, of the ionisation in the tube is due to these rays. The rays are given out by the luminous parts of the discharge, i.e. by the luminous positive column and especially by the luminous parts of the discharge near the cathode; they are not, however, given out by the Faraday dark space. As these rays help to ionise the gas the whole of the ionisation has not to be done by the collisions; so that the strength of the field required to produce discharge will be a little less than that calculated on the collision hypothesis; the difference will increase with the strength of the current, so that the Entladungstrahlen would tend to make the potential gradients in the tube diminish as the strength of the current through the tube increases.

278. We shall see that when the motion of a charged ion is accelerated the ion emits radiation analogous to Röntgen rays, the energy emitted per unit time being  $e^2f^2/3V$ , where e is the charge on the ion, f its acceleration, and V the velocity of light. As the ions carrying the current in the discharge tube are continually being accelerated by the electric force, and frequently, in addition, have their velocities suddenly altered by the collisions they make with the molecules of the gas, during which time their accelerations are very great, they will emit radiation, which will be most intense where the electric force is greatest; this radiation is, I think, Wiedemann's Entladungstrahlen.

<sup>\*</sup> Hoffmann, Wied. Ann. lx. p. 269, 1897.

<sup>+</sup> J. J. Thomson, Proc. Camb. Phil. Soc. x. p. 74, 1899.

## CHAPTER XVII.

## CATHODE RAYS.

279. So many observations have been made on these rays, and such important conclusions drawn from them, that it is convenient to devote a separate chapter to their consideration.

The cathode rays were discovered by Plücker\* in 1859; he observed on the glass of a highly exhausted tube in the neighbourhood of the cathode a bright phosphorescence of a greenish-yellow colour. He found that these patches of phosphorescence changed their position when a magnet was brought near to them, but that their deflection was not of the same nature as that of the rest of the discharge which we have seen he had carefully studied. Plücker ascribed the phosphorescence to currents of electricity which went from the cathode to the walls of the tube and then retraced, for some reason or another, their steps.

The subject was next taken up by Plücker's pupil Hittorf<sup>†</sup>, to whom we owe the discovery that a solid body placed between a pointed cathode and the walls of the tube casts a well-defined shadow, and the shape of the shadow only depending upon that of the body, and not upon whether the latter be opaque or transparent, an insulator or a conductor. This observation was confirmed and extended by Goldstein<sup>‡</sup>, who found that a well-marked, though not a very sharply defined shadow was cast by a small body near the cathode, whose area was much greater than that of the body: this was a very important observation, for it showed that the rays producing the phosphorescence came in a definite direction from the cathode. If the cathode were replaced by a

<sup>\*</sup> Plücker, Pogg. Ann. 107, p. 77, 1859; 116, p. 45, 1862.

<sup>+</sup> Hittorf, Pogg. Ann. 136, p. 8, 1869.

<sup>#</sup> Goldstein, Berl. Monat. p. 284, 1876.

luminous disc of the same size no shadow would be cast by a small object placed near it, for though the object might intercept the rays which came normally from the disc, yet enough light would be given out sideways by other parts of the disc to prevent the shadow being well marked. Goldstein, who introduced the term 'Kathodenstrahlen' for these rays, regarded them as waves in the ether, a view which received much support in Germany. A very different opinion as to the origin of the rays was expressed by Varley\*, and later by Crookes+, who advanced many and weighty arguments in support of the view that the cathode rays were electrified particles shot out from the cathode at right angles to its surface with great velocity, causing phosphorescence and heat by their impact with the walls of the tube, and suffering a deflection when exposed to a magnetic field by virtue of the charge they carried. The particles in this theory were supposed to be of the dimensions of ordinary molecules; the discovery made by Hertz+ that the cathode rays could penetrate thin goldleaf or aluminium was difficult to reconcile with this view of the cathode rays; although it was possible that the metal when exposed to a torrent of negatively electrified particles acted itself like a cathode and produced phosphorescence on the glass behind. The measurements described in Chapter V. of the mass of the particles carrying the charge show that though the cathode rays do consist of negatively electrified particles, the particles are not of the dimensions of even the smallest molecules, having a mass only about one-thousandth part of that of a molecule of hydrogen. We shall now proceed to describe the properties of the cathode rays in detail, beginning with that which led to their discovery, viz. the phosphorescence they produce when they fall on solids.

280. The colour of the phosphorescent light they produce when they fall on glass depends upon the nature of the glass; thus with soda glass the light is yellowish-green, with lead glass it is blue. A very large number of bodies become phosphorescent when exposed to these rays; indeed, this phosphorescence often affords a convenient means for detecting the rays: as phosphorescence is very easily excited in potassium platino-cyanide a

<sup>\*</sup> Varley, Proc. Roy. Soc. xix. p. 236, 1871.

<sup>+</sup> Crookes, Phil. Trans. Pt. 1. 1879, p. 135; Pt. 11. 1879, p. 641.

<sup>‡</sup> Hertz, Wied. Ann. xlv. p. 28, 1892.

screen of this substance is often used to detect the rays. The spectrum of the light given out by bodies when phosphorescing under bombardment by these rays is generally a continuous one. Sir William Crookes\* has shown that when the cathode rays fall on some of the rare earths, such as yttrium, the substance gives out a spectrum with bright bands; he has founded on this observation a spectroscopic method which is of the greatest importance in the study of the rare earths †. These earths are luminous when raised to a high temperature as in the mantles of Welsbach burners; there is, however, a marked difference between the incandescence produced in this way and that produced by cathode rays; thus in the Welsbach burner the addition of 1 per cent. of ceria to thoria increases the luminosity elevenfold as compared with that of pure thoria. Campbell Swinton; has shown, however, that it produces no appreciable change in the luminosity under cathode rays: again, in the flame pure ceria gives about as much light as pure thoria, while under cathode rays pure thoria gives a brilliant light, and pure ceria practically no light at all.

281. The impact of the cathode rays produces in some cases very definite chemical changes; thus Goldstein § has shown that the haloid salts of the alkali metals change colour when exposed to the rays; thus for example, crystals of rock-salt acquire under the rays a beautiful violet tint; this tint is not permanent, though under certain circumstances the rate of decay is exceedingly slow: thus there are at the Cavendish Laboratory some of these crystals, which, corked up in a test-tube but not kept in the dark, have retained a strong coloration for more than five years: exposure to moisture causes the colour to fade away rapidly. Lithium chloride is especially easily coloured; if a beam of cathode rays is slowly moved over the salt by a magnet the path of the beam traces out a coloured band over the surface of the salt. Similar changes in colour can be produced by chemical means; thus if sodium chloride is heated up with sodium vapour it gets coloured in much the same way as if it were exposed to cathode rays; the coloured salt is also produced at the cathode in the

<sup>\*</sup> Crookes, Phil. Trans. Pt. 11. 1879, p. 661.

<sup>+</sup> Ibid. Pt. III. 1883; Pt. II. 1885.

<sup>#</sup> Campbell Swinton, Proc. Roy. Soc. lxv. p. 115, 1900.

<sup>§</sup> Goldstein, Wied. Ann. liv. p. 371, 1898.

electrolysis of haloid salts. The coloured salt also occurs native. According to E. Wiedemann and Schmidt\* the coloration is due to the formation of a sub-chloride. Elster and Geitel† discovered that these coloured salts are very photo-electric, discharging negative electricity when exposed to light; behaving, in fact, as if they contained traces of the free metal. The glass of a vacuum tube also acquires a violet tint after long use.

- 282. The power of the glass to phosphoresce is deadened by long exposure to cathode rays: this is very beautifully shown in an experiment made by Crookes; the shadow of a mica cross was thrown upon the walls of the tube; after the discharge had been running for some time the cross was shaken down or a new cathode in a different part of the tube was used; the pattern of the cross could still be traced on the glass, but it was now brighter than the rest of the glass instead of darker as before. The portions outside the original pattern got tired by the bombardment, and so in the second part of the experiment phosphoresced less brightly than the portions inside the original shadow which were now bombarded for the first time. Crookes found that this change in the phosphorescence of the glass persisted even after the glass had been fused and again allowed to cool.
- 283. Villard§ found that cathode rays exert a reducing action; thus if they fall upon an oxidised copper plate, the part exposed to the rays becomes bright. In considering the chemical effects produced by the rays we ought not to forget that the incidence of the rays is often accompanied by a great increase in temperature, and that some of the chemical changes may be secondary effects due to the heat produced by the rays. Platinum after long exposure to the rays gets covered with platinum black.
- 284. Thermoluminescence. In some cases, even when no visible coloration is produced, the behaviour of the body after exposure to the rays shows that it has been changed. A very striking instance is the case called by E. Wiedemann 'Thermoluminescence.' Some bodies, after exposure to cathode rays,

<sup>\*</sup> Wiedemann and Schmidt, Wied. Ann. liv. p. 262, 1895; lxiv. p. 78, 1898.

<sup>+</sup> Elster and Geitel, Wied. Ann. lix. p. 487, 1896.

<sup>‡</sup> Crookes, Phil. Trans. Pt. 11. p. 645, 1879.

<sup>§</sup> Villard, Journal de Physique, 3me Série, t. viii. p. 140, 1899.

E. Wiedemann and Schmidt, Wied. Ann. liv. p. 604, 1895.

are found to possess for some time the power of becoming luminous when their temperature is raised to a point far below that at which they become luminous when in their normal state; they retain this property for weeks, and even months, after exposure to the rays. The substances in which this property is most highly developed belong to the class of bodies called by Van 't Hoff\* solid solutions; these are formed by precipitating simultaneously from a solution two salts, one greatly in excess of the other. The influence of a slight trace of a second substance

Cathode phosphorescence	After-glow	Thermo- luminescence	
faint yellowish	none	none	
intense green	strong green	intense green	
none	•••	***	
bright red	perceptible	perceptible	
faint dark violet	•••	0 0 4	
dark blue	faint	very faint	
red	perceptible	feeble	
intense dark red	persistent	intense red	
bright, white	persistent	white	
intense red	very persistent	very strong red	
bluish	faint	bright	
intense brown-	strong	bright yellow	
ish yellow yellow	persistent	bright yellow	
intense yellow	very persistent	intense yellow	
0	very faint	faint	
intense green	persistent	intense green	
	faint yellowish red intense green none bright red faint dark violet dark blue red intense dark red bright, white intense red bluish intense brownish yellow yellow intense yellow faint bluish	faint yellowish red intense green strong green  bright red perceptible faint dark violet dark blue faint red perceptible intense dark red bright, white intense red bluish intense brownish yellow yellow yellow faint bluish faint very persistent very faint	

on the phosphorescence produced while the rays are playing on the substance; the after-glow, which lingers for a time after the rays are stopped; and the thermoluminescence is shown by the

<sup>\*</sup> Van 't Hoff, Zeitschr. f. physik. Chem. v. p. 322, 1890.

preceding table, due to E. Wiedemann and Schmidt\*. By the symbol  $CaSO_4 + xMnSO_4$  is meant a 'solid solution' of a trace of  $MnSO_4$  in a matrix of  $CaSO_4$ .

The 'Entladungstrahlen' (see p. 491) also give rise to thermoluminescence, as Wiedemann found that any of the preceding substances showed thermoluminosity if sparks were produced close to them.

285. We may compare the after-glow observed with these solids with that which is observed when the electric discharge passes through certain gases which are found to remain luminous for a considerable time after the discharge has passed through them. It is not necessary that the discharge should consist of cathode rays; most kinds of discharges will produce this afterglow if the pressure is suitable; it is exceptionally conspicuous in electrodeless discharges and is especially well developed in oxygen and cyanogen, gases which polymerise with great ease. I think there are strong reasons for believing that the after-glow is very closely connected with the power some gases possess of polymerising and forming complex molecules; and that the gradual return of the gas from its polymerised to its normal form is accompanied by the emission of light.

286. Like the thermoluminescence of solids, the after-glow in gases seems to be increased by the presence of small quantities of impurities; thus it is brighter in oxygen with a little nitrogen than in pure oxygen. Newall† discovered a very remarkable effect connected with the after-glow in oxygen; he found that with the electrodeless discharge the after-glow was only developed when the pressure was between the limits 6 mm. and 01 mm. If the discharge is sent through the gas at a pressure not between these limits, there is no glow, but if after the discharge has ceased the pressure is altered so as to come within the limits the gas at once begins to glow, suggesting that the polymerised form is stable, i.e. does not go back into the normal form except between the limits 6 mm. and 01 mm. It may be mentioned that this is the region of pressure in which some observers, though not all, have observed large departures from Boyle's law.

† Newall, Proc. Camb. Phil. Soc. ix. p. 295, 1897.

<sup>\*</sup> Wiedemann and Schmidt, Wied. Ann. lvi. p. 201, 1895.

In the case of phosphorescent solids and liquids we may regard the phosphorescence as arising in the following way. The cathode rays or Entladungstrahlen will ionise the substance, causing complex substances to be formed which phosphoresce as they break up into their original constituents; some of these complex molecules are unstable at the temperature of the room and at once begin to decompose, giving rise to the after phosphorescence of the glass, etc.; others are stable at ordinary temperatures, but are unstable and decompose at high temperatures; these produce thermoluminescence.

- 287. M°Clennan\* has shown that some salts, especially the sulphates of potassium, barium, strontium and calcium, after exposure to cathode rays, or to the radiation from a spark, possess the power of discharging a positively electrified body placed near them in a gas at low pressure, behaving in fact as if they were photo-electric bodies exposed to the action of ultraviolet light, i.e. they emit slowly moving negatively electrified corpuscles. McClennan made experiments to show that there was no emission of ultra-violet light from the heated salts. There does not seem to be any connection between the powers of salts to produce the effect discovered by McClennan and their power of producing thermoluminescence: as McClennan found that many salts which glowed strongly when heated did not give his effect, which was given by some salts which hardly showed any thermoluminescence.
- Thermal effects produced by the rays. The cathode rays heat bodies on which they fall, and if the rays are concentrated by using a portion of a hollow cylinder or spherical shell as a cathode, platinum may be raised to incandescence, thin pieces of glass fused, and the surface of a diamond charred.

Measurements of the amount of heat developed by the rays have been made by E. Wiedemann and Ebert<sup>†</sup>, E. Wiedemann<sup>‡</sup>, and Ewers  $\S$ . A simple example will give some idea of the amount of energy carried by the rays. If n is the number

<sup>\*</sup> McClennan, Phil. Mag. vi. 3, p. 195, 1902.

<sup>+</sup> Wiedemann and Ebert, Sitz. der phys. med. Soc. Erlangen, Dec. 1891.

<sup>‡</sup> E. Wiedemann, Wied. Ann. lxvi. p. 61, 1898.

<sup>§</sup> Ewers, Wied. Ann. lxix. p. 167, 1899.

of corpuscles striking a body in unit time, m the mass of a corpuscle, and v its velocity, then E the energy possessed by the corpuscles striking the body in unit time is  $\frac{1}{2}nmv^2$ ; if all the corpuscles coming from the cathode are caught by the body and e is the charge on a corpuscle, then ne = I, the current carried by the corpuscles; thus  $E = \frac{1}{2}I\frac{m}{e}v^2$ : now  $10^{-5}$  ampères is not an exceptionally high value for I, and if  $v = 5 \times 10^9$  cm./sec. we get, since  $m/e = 10^{-7}$ ,  $E = 12.5 \times 10^5$ ; thus the energy possessed by the corpuscles striking the body per minute would be nearly 2 calories.

289. The impact of the corpuscles does more than heat the body, it makes it phosphoresce, it produces Röntgen rays, and causes the body to emit cathode rays. Interesting information is afforded by measuring the heat produced by the cathode rays, and also the charge of electricity brought to the body by the rays; such measurements have been made by the author\*, and later in greater detail by Cady+. Cady's method was to measure (1) the heat produced in a bolometer strip against which the rays struck, and (2) the negative charge acquired by the bolometer per second; the latter, it is important to notice, need not be the same as the charge carried by the corpuscles striking the body in one second, for some of the corpuseles may rebound from the body without giving up a charge, or the impact of the rays may cause the body to give out cathode rays, carrying from it a negative charge, or positively electrified atoms, giving to it an additional negative charge; thus if I is the charge carried by the corpuscles, i that acquired by the bolometer per second, then I is not necessarily the same as i. If V is the potential difference between the electrodes in the tube, then the energy carried by the corpuscles is VI. Cady measured the ratio of Vi to Q the mechanical equivalent of the heat developed in unit time; he found that this ratio depends greatly upon the value of i; as long as i is large it is greater than unity, diminishing as i diminishes; when i gets very small (less than  $10^{-7}$  ampères), the ratio becomes constant and equal to '83; as the ratio is less than unity it follows that there is an emission of negative electricity from the bolometer,

<sup>\*</sup> J. J. Thomson, Phil. Mag. v. 44, p. 293, 1893.

<sup>†</sup> Cady, Drude's Ann. i. p. 678, 1900.

either by the reflection of the cathode rays, or by the emission of secondary cathode rays from its surface. We have seen that the measurement of i and V does not give the energy reaching the surface through the cathode rays; a slight modification of the experiment would, however, give the data by which this energy could be determined; all that is necessary would be to surround the bolometer by an insulated Faraday cylinder, into which the rays were admitted through a small opening, and then to measure the charge received by this cylinder in unit time.

E. Wiedemann\* has shown that the energy spent in producing phosphorescence is but a small fraction of the incident energy.

Mechanical effects produced by the rays. A secondary 290. result of the thermal effects produced by the rays are the very interesting mechanical effects which have been especially studied by Crookes† and Puluz‡. A typical example of these is afforded by the well-known experiment due to Crookes represented in Fig. 163, where the axle of a very light mill with a series of vanes

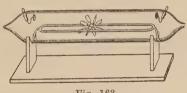


Fig. 163.

is mounted on glass rails, in a vacuum tube; when the discharge passes through the tube the cathode rays strike against the upper vanes and the wheel rotates and travels from the negative to the positive end of the tube.

A simple calculation will show that we cannot ascribe the rotation to the momentum communicated to the vanes by the impact of the corpuscles against them; for, take the case when the rays are so powerful that they carry the very large current of 10<sup>-5</sup> ampères, and that they move with the very high velocity of  $10^{10}$  cm./sec.: if N is the number of corpuscles striking a surface in unit time, m the mass of the corpuscles; then supposing the

<sup>\*</sup> E. Wiedemann, Wied. Ann. lxvi. p. 61, 1898.

<sup>†</sup> Crookes, Phil. Trans. 1879, pt. i. p. 152.

<sup>‡</sup> Puluz, Radiant Electrode Matter. Physical Society's Reprint of Memoirs, p. 275.

corpuscles to rebound from the surface with a velocity equal to that with which they impinge against it, the momentum communicated to the surface in unit time is  $2Nm10^{10}$ ; if e is the charge carried by a corpuscle, then Ne is the current carried by the rays, in our case 10<sup>-6</sup> in absolute measure; hence the momentum communicated to the surface per second is equal to  $2\frac{m}{a}$  104 dynes, or as  $m/e = 10^{-7}$  to  $2 \times 10^{-3}$  dynes: this is equivalent to a difference of pressure on the two sides of a vane 1 sq. cm. in area of onefive-hundred-millionth part of an atmosphere; an effect altogether too small to explain the movement of a body such as that represented in Fig. 163. This movement is probably due to an effect similar to that observed in a radiometer, as the impact of the cathode rays will make one side of the vanes much hotter than the other. Starke\* has shown that when the vanes are arranged so that the radiometer effect is eliminated, the mechanical effect is exceedingly small—in his experiments, where the current carried by the cathode rays was 10<sup>-7</sup> ampères and the potential difference 10,000 volts—certainly less than 10<sup>-4</sup> dynes.

291. Electric charge carried by the cathode rays. The fact that the cathode rays carry a negative charge of electricity was proved in a very direct way by Perrin†. Fig. 164 represents a modification of his experiment. The rays start from the

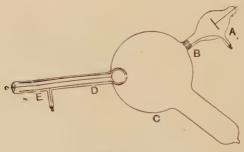


Fig. 164.

cathode A and pass through a slit in a brass rod B, which fits lightly into the neck of the tube; this rod is connected with the

<sup>\*</sup> Starke, Drude's Ann. iii. p. 101, 1900.

<sup>+</sup> Perrin, Comptes Rendus, exxi. p. 1130, 1895.

earth and used as an anode; the rays after passing through the slit enter the spherical vessel C. In this vessel there are two coaxial metal cylinders, the outer one D connected with the earth, the inner one E carefully insulated and connected with an electrometer. The cylinders are placed so as to be out of the direct line of fire of the rays. When the discharge passed through the tube and the cathode rays passed horizontally through the vessel C, the inner cylinder E received a small, but only small, negative charge. The cathode rays were then deflected by a magnet; their path could be inferred from the position of the phosphorescent patch on the walls of C; when the deflection was increased, so that the position of the path showed that the rays had fallen on the opening of the cylinders, there was a very great increase in the negative charge received by E; when the rays had been so much deflected that the phosphorescent patch fell below the slit the negative charge in the cylinder E again disappeared. This experiment shows that the rays carry a negative charge, as it proves that the negative electrification follows exactly the same course as the rays producing the phosphorescence on the glass.

This experiment also shows that the cathode rays make the gas through which they pass a conductor of electricity; for if in the experiment the discharge is kept continuously passing through the tube and the cathode rays deflected until they pass into the cylinder, the negative charge on the cylinder will rise to a certain value, beyond which it will not increase however long the discharge may be kept running; this shows that the gas around the cylinder is a conductor, and the steady state of the cylinder is reached when it loses as much electricity by conduction through the gas as it gains from the cathode rays. The same thing is shown when the cylinder is given a negative charge before the discharge through the gas begins: if this charge is less than a certain value the cathode rays will increase the charge; if however it is greater than this value, the cathode rays will diminish the charge until it falls to this critical value.

292. Reflection of cathode rays. When cathode rays strike the surface of either a conductor or an insulator cathode rays start from the surface in all directions; this phenomenon is called the diffuse reflection of the cathode rays: we must be careful

however to remember that reflection is used in a different sense from that which is usual in optics, where for example we should not speak of the phosphorescent light given out by such a substance as quinine when struck by ultra-violet light as reflected rays; in the case of the cathode rays all the cathode rays proceeding from a surface struck by cathode rays are called reflected rays. The existence of such rays is easily shown by an experiment due to Goldstein\*. The cathode rays from the cathode C

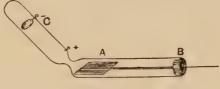


Fig. 165.

fall on the plate A which can be rotated by a handle passing through a stuffing-box. The half of the tube AB on the illuminated side of A becomes phosphorescent from the cathode rays diffusely reflected from A. The reflection occurs even when the plate does not itself become phosphorescent under cathode rays.

293. Measurements of the amount of 'reflection' experienced by cathode rays when incident upon different substances and at different angles of incidence have been made by Campbell Swinton<sup>†</sup>, by Starke<sup>†</sup>, and by Austin and Starke§. Campbell Swinton's experiments, which had for their object the measurement of the variation of the 'reflected' rays at various angles of incidence and emergence, were arranged as represented in Fig. 166. C is the cathode; A the reflecting surface, a flat piece of platinum which could be rotated about its axis; F a Faraday cylinder which receives the rays emitted by the surface; this could be set so that the opening made any required angle with the direction of the incident rays; the charge received by this cylinder was taken as the measure of the amount of reflection. Campbell Swinton

<sup>\*</sup> Goldstein, Wied. Ann. xv. p. 254, 1882.

<sup>+</sup> Campbell Swinton, Proc. Roy. Soc. lxiv. p. 377, 1899.

<sup>‡</sup> Starke, Wied. Ann. lxvi. p. 49, 1898; Drude's Ann. iii. p. 75, 1900.

<sup>§</sup> Austin and Starke, Drude's Ann. ix. p. 271, 1902.

came to the conclusion that although the 'reflection' was very diffuse there was appreciably more in the direction in which the angle of emergence was equal to the angle of incidence than in

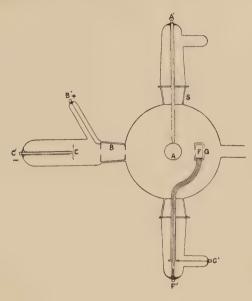


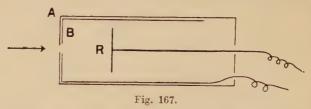
Fig. 166.

any other direction; he found that the total amount of emission was slightly greater at oblique than at normal incidence; he measured also the charge received by the reflector and found that though with normal incidence it received a large negative charge, the charge diminished as the incidence became more oblique, vanished, and finally with very oblique incidence became positive. The positive charge received by the reflector has also been observed by Austin and Starke (l.c.).

Starke determined the proportion between the incident and receding rays, or rather the ratio of the negative charge acquired by the reflector to that carried by the receding rays.

The principle of the method used by Starke is as follows. The cathode rays enter through a hole in the cylinder and strike the reflector; the cylinder and reflector are each connected to earth through high-resistance galvanometers; when the rays strike against the reflector currents pass through these galvanometers;

let  $i_1, i_2$  be the currents through the galvanometers connected with the reflector and cylinder respectively; let N be the number of corpuscles striking the reflector in unit time, n the number leaving



it in the same time, e the charge on a corpuscle; then, if there is no ionisation in the gas of the cylinder, no escape of the receding rays through the hole, and no diffusion of the incident rays in the cylinder causing some of the incident rays to strike the walls of the cylinder instead of the reflector, we have

$$(N-n) e = i_1; ne = i_2;$$
  $\frac{n}{N} = \frac{i_2}{i_1 + i_2};$ 

or

hence if we measure  $i_1$  and  $i_2$  we can determine the value of n/N; in practice some corrections are necessary, for which we must refer to Starke's paper (l.c.); the value of n/N depends upon the metal; the following are Starke's values for this quantity:

Metal	Density	n/N	Metal	Density	n/N
Pt	21·5 11·3 10·5 9·9 8·9 8·5	·72 ·63 ·59 ·58 ·48 ·45	Brass Fe Zn Al Mg	8·1 7·7 7·1 2·6 1·7	*43 *40 *40 *25 *25

Thus the value of n/N increases with the density of the metal; the numbers given above are roughly proportional to the square root of the density; we see that even for the lightest metals the number of corpuscles receding from the surface is as much as one quarter of the number of those approaching it. The preceding values of n/N are when the incidence of the cathode rays is normal; in this case n/N does not depend upon the velocity of the incident rays.

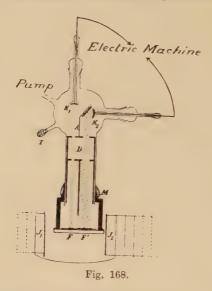
- 294. The fact observed by Campbell Swinton (l.c.) that when the incidence is very oblique the reflector acquires a positive instead of a negative charge, has been carefully studied by Starke and Austin\*, who have measured the charge received by the reflector for cathode rays incident at various angles; they find that the angle of incidence at which the charge received by the reflector changes from - to + depends on the material of which the reflector is made and the velocity of the rays. With denser reflectors the change from - to + takes place at a smaller angle of incidence than it does with lighter reflectors; and, again, the smaller the velocity of the rays the smaller the critical angle. The amount of influence exerted by the nature of the metal, and the velocity of the rays, may be illustrated by the following numbers due to Austin and Starke. With a platinum reflector, and with cathode rays produced by a potential difference of 9000 volts, the critical angle of incidence was 60°; with a copper reflector, and a potential difference of 8700 volts, the critical angle was 80°, and with a potential difference of 5000 volts, 70°.
- 295. Since, in some cases, the reflector receives a positive charge from the impact of the negatively electrified corpuscles, more corpuscles must leave the surface than arrive at it; it follows that the velocity of the receding corpuscles must, on the average, be less than that of the approaching ones, otherwise the energy emitted by the reflector would be greater than the energy received. Measurements of the velocity of the 'reflected' rays, by means of the deflection they experience in a magnetic field, have been made by Merritt<sup>†</sup>, Austin and Starke (l. c.), and Gehrcke<sup>+</sup><sub>τ</sub>; both Merritt and Austin and Starke came to the conclusion that the velocity of the reflected rays was much the same as that of the incident; Gehrcke, however, by a very ingenious method showed that among the 'reflected' rays there were a large number whose velocities were considerably less than that of the incident rays. Gehrcke's method is represented in Fig. 168;  $K_1$  and  $K_2$  are two cathodes connected together and with the negative pole of an electrical machine; the rays from  $K_1$  went straight from the cathode on to a fluorescent screen FF', while those from  $K_2$  fell on

<sup>\*</sup> Austin and Starke, Drude's Ann., ix. p. 271, 1902.

<sup>+</sup> Merritt, Physical Review, vii. p. 217, 1898.

<sup>‡</sup> Gehrcke, Drude's Ann., viii. p. 81, 1902.

a magnesium reflector, the 'reflected' rays from which fell on the same screen.  $J_1$  and  $J_2$  are the coils for producing the magnetic



field. The appearance of the phosphorescence on the screen before and after the magnetic field was started is shown in Fig. 169.



Fig. 169.

The middle patches F, F' represent the phosphorescence without a magnetic field due to the direct and reflected rays respectively; the patches above and below these represent the phosphorescence when the magnetic field was on, the upper and lower patches corresponding to fields in opposite directions. It will be noticed that while the patch of phosphorescence, due to the direct rays,

has not been sensibly broadened by the magnetic field, the narrow patch due to the 'reflected' rays has become a broad band, showing the presence of some rays much more easily deflected, and therefore moving more slowly than the incident rays. Since one of the boundaries of the reflected patch keeps in line with one of the direct patch, there must be some of the reflected rays which move with approximately the same velocity as the incident rays.

We conclude from this experiment that a surface struck by cathode rays emits secondary rays which on the average move more slowly than the primary ones. The ratio of the number of secondary to the number of primary rays is greater at oblique than at normal incidence. The 'reflection' of cathode rays at the surface of a solid seems in many respects analogous to the emission of corpuscles from a body illuminated by ultra-violet light. The corpuscles in the primary rays penetrate some little distance below the surface, ionising the molecules against which they strike; the secondary corpuscles produced in this way, and perhaps also some of the primary ones whose motion has been reversed by the collision they have made with the molecules of the reflector, escape from the reflector and form the reflected cathode rays.

The path of a corpuscle which strikes the reflector obliquely will be nearer the surface than if it strikes the reflector normally, and thus the corpuscles liberated by it will have a shorter distance to travel before reaching the surface of the reflector and emerging from it, we should therefore expect the oblique rays to produce more reflected rays.

296. Transmission of Cathode Rays. It was for a long time believed that even the thinnest slice of a solid was impervious to cathode rays. Thus Goldstein and Crookes had shown that bodies as thin as a film of collodion or glass blown as thin as possible cast intensely black shadows when interposed between the cathode and the walls of the tube. In 1892, however, Hertz\* found that behind a piece of gold-leaf or thin aluminium foil there was appreciable phosphorescence, and that the phosphorescence was deflected by a magnet.

<sup>\*</sup> Hertz, Wied. Ann. xlv. p. 28, 1892.

297. Lenard's Experiments. Lenard\* made a series of most interesting experiments on the passage of cathode rays through very thin films. The rays were produced in a tube like that represented in Fig. 170.

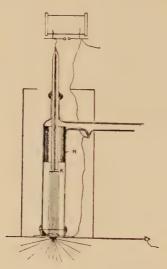


Fig. 170.

K, the cathode, is an aluminium disc fastened to a stiff wire which is surrounded by a glass tube; the anode is a brass tube surrounding part of the wire carrying the cathode. The end of the tube opposite the cathode is closed by a metal cap fastened to the tube by marine-glue; a hole 1.7 mm. in diameter is bored through this cap and covered with a piece of thin aluminium foil, about '00265 mm. thick. This window is in metallic contact with the cap, and was together with the anode connected with earth. The tube is exhausted until the difference of potential between the cathode and anode is very great, and strong cathode rays reach the window. In a dark room a diffuse light spreads from the window into the air outside; this light is brightest close to the window, its outline is very indefinite; with a strong discharge in the tube the light can be traced to some centimetres away from the tube. Phosphorescent bodies placed in the neighbourhood of the window phosphoresce. In air at ordinary pressures the rays proceeding from the window diffuse

<sup>\*</sup> Lenard, Wied. Ann. li. p. 225, 1894.

out very rapidly, and shadows cast by solid bodies placed in their path are ill defined and many times larger than the bodies casting them. These rays are much more easily studied if the window, instead of opening on to the air, opens on to another tube from which the air can be exhausted: when the air in this tube is at a low pressure, the rays travel a well-defined path and can easily be studied. The rays are deflected by a magnet, by an electric field, and carry a negative charge of electricity; the ratio of the charge to the mass of the carrier has been determined by Lenard (see p. 95) and found to have the same value as for cathode rays. These facts show that these rays are cathode rays; it is often, however, convenient to distinguish between cathode rays inside and outside the tube producing them; it is thus desirable to keep the term Lenard rays for the latter and use cathode rays for those inside the tube.

Lenard measured the absorption of these rays by various substances, and arrived at the simple law connecting absorption with density, already discussed on p. 310. Lenard measured the intensity of his rays by the phosphorescence they produced in a solution of pentadekylparatoloketone. Seitz\*, who has made similar measurements, measured the total charge of electricity carried by the rays. We must remember that unless all the rays are moving with the same velocity the two methods may give different results; in the electrical method all the corpuscles count equally, whatever their velocity may be; in the optical method, however, this is no longer the case, the more rapidly moving corpuscles producing much more phosphorescence than the same number of corpuscles with smaller velocity.

298. We have, when considering the reflection of the cathode rays, supposed that the incident rays gave by means of collisions sufficient energy to some of the corpuscles in the metal to enable them to escape from it. In the case of reflection we have to deal with the corpuscles which emerge from the face of the metal first struck by the rays; when, however, the metal is very thin, some of the corpuscles travelling in the same direction as the incident rays may come out on the far side of the metal and form part of the bundle of transmitted rays; many of these secondary rays will be moving with smaller velocities than the

<sup>\*</sup> Seitz, Drude's Ann. iv. p. 1, 1901.

primary rays, and thus the transmitted rays will not be homogeneous, and the electrical and optical methods of estimating their intensity may, as explained above, give different results.

- 299. A loss of velocity in the rays emerging from thin plates of metal has been observed by Leithausers\* and Des Coudres+; the latter has shown also that the patch of phosphorescence due to these rays is under the action of a magnetic field drawn out into a broad patch, showing that the transmitted rays are not homogeneous (compare the corresponding result found by Gehrcke for the reflected rays, see p. 508). Des Coudres showed also that the rays which emerge obliquely from the metal have smaller velocities than those emerging normally.
- 300. Scattering of Cathode Rays inside the tube. Measurements of the scattering of cathode rays inside the discharge tube have been made by Kaufmann+, who employed the electrical method. The greatest potential differences employed was only about 7500 volts, so that the velocity of the rays in Kaufmann's experiments was very much less than in those of Lenard. The principle of the method used by Kaufmann was as follows. Consider a bundle of rays originally horizontal passing through the gas, then if  $N_0$  is the number of corpuscles crossing a vertical plane AB in unit time, the number crossing a parallel plane CD at a distance x from AB will be  $N_0 \epsilon^{-bx}$ , where b is by definition the coefficient of absorption; if e is the charge carried by a corpuscle the quantity of negative electricity entering the space between AB and CD in unit time is  $N_0e$ , the amount leaving it is  $N_0e\epsilon^{-bx}$ ; hence if ABCD is surrounded by a metallic cylinder the quantity of electricity received by the cylinder in unit time is  $N_0 e(1 - \epsilon^{-bx})$ ; hence, if we compare the charge received by the cylinder with that which passes through the end CD, we shall find  $(1-\epsilon^{-bx})/\epsilon^{-bx}$ , from which we can deduce the value of b. Kaufmann in this way determined b for nitrogen, carbonic oxide, carbonic acid and hydrogen, at pressures ranging from about 1/50 to 1/28 of a millimetre of mercury and with potential differences from about 2500 to 7500 volts: he

<sup>\*</sup> Leithausers, Sitz. Berlin. Akad. d. Wissensch. Mar. 13, 1902.

<sup>+</sup> Des Coudres, Phys. Zeits. iv. p. 140, 1902.

<sup>#</sup> Kaufmann, Wied. Ann. lxix. p. 95, 1899.

found that if V is the potential difference in the discharge tube in volts, p the pressure in millimetres of mercury, then for the same gas, within the limits of pressure and potential difference indicated, bV/p was constant; *i.e.* the absorption coefficient is proportional to the pressure and inversely proportional to the kinetic energy of the corpuscle. The values for the different gases are indicated in the following table:

Gas	bV/p	Molecular weight
${ m H}_2$	730	2
$N_2$	5650	28
CO	6380	28
$CO_2$	6830	44

The values of b do not follow those of the molecular weight as closely as the values determined by Lenard; one reason for this may be the greater velocities of the rays investigated by Lenard; we have seen (p. 315) that it is only for very rapidly moving cathode rays that we could expect Lenard's law to be strictly true; another reason may be that in the method used by Kaufmann the positive and negative ions produced by the primary rays by collision with the molecules of the gas might diffuse with different velocities to the conductors in the tube, so that part of the current measured in these experiments may be due to secondary ionisation.

301. Magnetic Spectrum of Cathode Rays. Birkeland\* found that when the cathode rays are produced by means of an induction coil, a patch of cathodic phosphorescence is not merely displaced by a magnetic field, but is broken up into several distinct patches; thus, for example, if there is originally a narrow straight band of phosphorescence, then under the magnetic field several parallel bright bands of phosphorescence separated by comparatively dark spaces are observed. This is called the magnetic spectrum. I have obtained similar effects by deflecting the rays by electric instead of magnetic forces. This splitting up of the rays shows that the original bundle of cathode rays is not homogeneous, but is made up of groups moving with different, and finitely different, velocities; each group being differently deflected, the slower ones more than the faster.

<sup>\*</sup> Birkeland, Comptes Rendus, exxiii. p. 92, 1897.

Strutt\* has shown that the magnetic spectrum is due to the want of uniformity necessarily associated with the use of an induction coil, which produces a discontinuous discharge, and that if the cathode rays are produced by a large electrostatic machine, or a large number of storage cells, either of which gives a continuous discharge, the phosphorescence is not broken up into separate patches by a magnetic or an electric field.

302. Path of the Cathode Rays in the Discharge Tube. The cathode rays are deflected by an electric force; thus, as the electric field is very intense in the Crookes dark space, the rays as they pass through this space will, unless the lines of force in it are straight (this is approximately the case when the cathode is a large plane disc), be deflected and their paths will not coincide with the normals to the cathode at their point of projection. The amount of deflection of the path from this normal will depend mainly upon the rate at which the intensity of the electric field diminishes as we recede from the cathode: if, as in the case when the pressure is not very low, the field close to the cathode is very much more intense than that at some distance away from it, the corpuscles will acquire so much energy while still close to the cathode that they will not be much deflected by the comparatively feeble fields traversed by them during the rest of the journey; in this case the paths of the rays will be approximately the normals to the cathode, so that if the cathode is a hollow spherical bowl the rays will travel along the radii of the sphere and will be brought to a focus at its centre. If however the strength of the field only changes slowly as we recede from the cathode, we shall get much greater deviation than in the last case, for not only will the velocity they acquire while still close to the cathode be smaller, but also the deflecting force when they get away from the cathode will be greater. The paths of the rays will now be no longer along the normals because of the deflecting force, nor will they, owing to the inertia of the corpuscles, be along the lines of force unless these are straight. The paths of the corpuscles will be between the normal and the lines of force; thus, for example, in the case of the hollow bowl, the path will be between the normal CP and the line of force PQ (Fig. 171); thus, if the

<sup>\*</sup> Strutt, Phil. Mag. v. 48, p. 478, 1899.

paths cross the axis of the bowl at all, they will do so at points on the far side of the centre. It is well known that when, as in

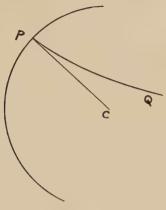


Fig. 171.

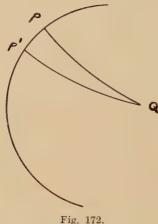
the bulbs used for producing Röntgen rays, a cathode of this kind is used, the 'focus' gets further from the cathode as the exhaustion is increased. Goldstein\*, who made a series of beautiful experiments on the phosphorescent patterns produced by curved cathodes of different shapes, showed, by using an unsymmetrical cathode, that the rays crossed when the pressure was comparatively high, but did not do so at very high exhaustions. The appearance of the cathode rays from a curved cathode is shown by the diagrams in Fig. 173 taken from a paper by Campbell Swinton†; it will be seen that this is very different from that which would result if the rays travelled along the normals to the cathode.

- 303. The motion of the corpuscles in a vacuum tube offers a fine field for the application of Hamilton's Principle of Varying Action: for since the cathode is an equipotential surface, and the corpuscles leave that surface normally and with equal amounts of energy, their paths will, by the Principle of Varying Action, be the orthogonal trajectories of a system of surfaces.
- 304. We have regarded the cathode rays as originating from positive ions which were formed by the cathode rays themselves

<sup>\*</sup> Goldstein, Wied. Ann. xv. p. 254, 1882.

<sup>+</sup> Campbell Swinton, Proc. Roy. Soc. lxi. p. 79, 1897.

at a distance from the cathode. If however the path PQ of the cathode ray is curved (Fig. 172), and if the positive ion is produced at Q, then, in consequence of the difference in mass between



the positive and negative ions, the path of the positive ion up to the cathode will not be QP, but some other path such as QP'; thus the cathode rays produced at P will, when the paths are not straight lines, give rise to positive ions which will help to make cathode rays which start not from P but from some other point P'.

The distance between the places where the positive ions strike the cathode and the origin of the cathode ray producing these ions will be greatest for the rays which start from near the boundary of the cathode, as these travel through the part of the electric field where the lines of force are most curved; there will thus not be many positive ions striking against the outer parts of the cathode, on this account the rate of emission of the cathode rays increases as we approach the centre of the cathode; on the other hand, if the cathode is curved the electric force close to the cathode will be a minimum at the centre, so that on this account the rays would be fewer along the axis; taking both these effects into consideration we should expect there would be a tendency for the rays to attain a maximum at some place intermediate between the centre and edge of the cathode

The observations of Campbell Swinton\* establish the existence of such an effect; he found that with concave cathodes, when the pressure of the gas is within certain limits, the cathode rays do not form a solid pencil but are condensed into a hollow conical shell. He proved this by means of the phosphorescence produced by these rays on a carbon plate whose plane was at right angles to the cathode: the phosphorescent patch was a circular ring with in some cases a bright spot at the centre. The appearance of the phosphorescence is represented in Fig. 173.

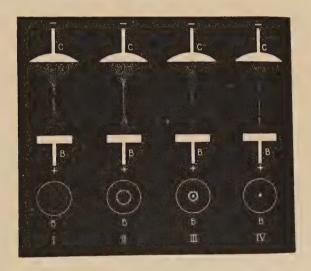


Fig. 173.

This hollowness of the bundle of cathode rays was found by Campbell Swinton to depend on the curvature of the cathode, it did not occur when this was plane.

305. Repulsion of Cathodic Streams. Goldstein+ found that when in a discharge tube there are two cathodes connected together, the cathodic rays from one cathode are deflected when they pass through the dark space surrounding the other cathode.

One of Goldstein's experiments was as follows: one of the cathodes was a hollow metal cylinder a, from which a pencil of cathode rays issued, producing luminosity in the gas through

<sup>\*</sup> Campbell Swinton, Proc. Roy. Soc. lxi. p. 79, 1897.

<sup>+</sup> Goldstein, Eine neue Form der elektrischen Abstossung.

which they travelled; the other cathode (b) was a wire at right angles to the axis of the bundle of rays proceeding from a; when



Fig. 174.

b was disconnected from a the path of the rays from a was straight, but when a and b were connected the cathode rays from a were bent sharply away when they approached b. Goldstein found that the amount of deflection did not depend on the material of which the cathodes were made, nor on the nature of the gas through which the rays passed. The deflection ceased if the deflecting cathode was surrounded by a screen of some solid substance.

Another example of the deflection of two cathode streams is afforded by an experiment made by Crookes\*; a and b (Fig. 175) are two metal discs, either or both of which can be made into

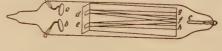


Fig. 175.

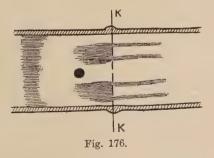
cathodes, a diaphragm with two holes cut in it is placed in front of these discs, and the path of the rays through the tube is marked out by the phosphorescence they excite in a chalked plate inclined at a small angle to their path. When a is the cathode and b is idle the rays travel along the path df, while when a is idle and b the cathode they travel along ef. When, however,

<sup>\*</sup> Sir W. Crookes, Phil. Trans. 1879, part ii. p. 652.

a and b are cathodes simultaneously the paths of the rays are dg and eh respectively, the two streams having apparently repelled each other. Crookes attributed the divergence of the rays to the repulsion between the negative charges of electricity travelling along with them. E. Wiedemann and Ebert\*, however, by a modification of this experiment, have shown that this is not the cause of the repulsion; they provided the holes d and e with shutters, and found that when e and e were simultaneously cathodes eh was the path of the rays through e, whether the window at e was open or shut, although when it was shut there were of course no cathode rays travelling along e0 to deflect those passing through e1, showing that the deflection of the rays has its origin in the space between e2 and e3.

The effects we have been describing can all be explained by the electrostatic repulsion of the negative electricity travelling along the cathode rays, by the strong electric field which surrounds a cathode; this repulsion is appreciable only when the rays from one cathode pass through the dark space of the deflecting cathode, because, as we have seen, the intensity of the electric field is very much greater in the dark space than it is at any other part of the discharge; we have, on page 435, discussed a method of using this deflection of the cathode rays for measuring the strength of the electric field in the tube.

306. Canalstrahlen or Positive Rays. When a perforated cathode is used, there may, if the pressure is between certain limits, be observed luminous streams passing through the holes in



the cathode, emerging on the side of the cathode remote from the anode, and travelling in straight lines, as in Fig. 176; these were

<sup>\*</sup> Wiedemann and Ebert, Wied. Ann. xlvi. p. 158, 1891.

first observed by Goldstein\*, and called by him Canalstrahlen. They excite phosphorescence on the part of the glass against which they strike, and if this glass is soda glass the places struck by these rays show, when observed through the spectroscope, the sodium lines. Wehnelt† has shown that when these rays strike against a copper plate they oxidise it; the cathode rays, as we have seen (p. 496), reduce an oxidised plate. Schmidt‡ has shown that the oxidation of metals by the Canalstrahlen is not due to the impact of the rays but is an indirect effect due to the rays producing active oxygen when they pass through the gas; he showed this by casting a shadow on the copper plate by interposing between it and the rays a solid obstacle, the part of the plate in shadow was as much oxidised as that exposed to the direct impact of the rays. In hydrogen Schmidt observed that the Canalstrahlen exert a reducing effect.

Though these rays are much less deflected than the cathode rays by electric and magnetic fields, they do suffer appreciable deflection, and W. Wien has shown (see p. 117) that the direction of these deflections indicates that the Canalstrahlen consist of positively charged particles; he has measured, by the method indicated in Chap. V., the ratio of the charge to the mass, and finds for the maximum value of this quantity 104, which is the ratio of the charge to the mass for the hydrogen ion in the electrolysis of solutions. Wien found that, in addition to the rays which give this limiting value to e/m, there were always other rays present which gave smaller values for e/m, and that there was no evidence that the change in this quantity was discontinuous, which it would be if the charge could only change by multiples of e and the mass by multiples of m. I have observed similar variations in the value of e/m for the positive ions given off from incandescent wires; I think this variation is probably due to the positive ions losing their charges before they reach the glass where they produce phosphorescence; what is measured in these determinations is ratio of the mean value of e to m; if now the positive ion gets neutralised by a negative charge before it reaches the glass, then the mean value of e would be smaller

<sup>\*</sup> Goldstein, Berlin Sitz. xxxix. p. 691, 1886; Wied. Ann. lxiv. p. 45, 1898.

<sup>†</sup> Wehnelt, Wied. Ann. lxvii. p. 421, 1899.

<sup>‡</sup> Schmidt, Drude's Ann. ix. p. 703, 1902.

than if it retained its charge up to the moment of impact. We must remember that the gas through which the Canalstrahlen move is ionised, and that there are plenty of corpuscles about to neutralise the positive charge. It may be urged that if the ions had lost their charge before striking the glass, they would not be able to produce phosphorescence, since, as far as our knowledge extends, phosphorescence is not produced by the impact of uncharged molecules; but, according to Wien's determination, the positive ions in the Canalstrahlen are moving with a velocity of more than 10<sup>8</sup> cm./sec.: we have no experience of molecules moving with anything like this velocity; the shock of the collision might be sufficient to ionise the molecule afresh, and thus produce in the neighbourhood of the place of impact effects analogous to those produced by the collision of charged ions.

307. Several experiments have been made by W. Wien\*, Ewers+ and Villard; to detect the positive charge carried by the Canalstrahlen by catching, as in Perrin's experiment on the negative charge carried by the cathode rays (see p. 502), the Canalstrahlen in a Faraday cylinder, and observing the charge acquired by that cylinder. The aforesaid physicists differ in their interpretation of the results they obtain; all agree that under certain circumstances the Faraday cylinder, placed behind a perforated cathode, receives a positive charge of electricity, but while Wien and Ewers think that this charge is carried by the Canalstrahlen, Villard is of opinion that it is a secondary effect due to the slow diffusion into the cylinder of ions from other parts of the tube. In his experiments he found that the Canalstrahlen were able to penetrate into the cylinder for some time before it gave any indication of a positive charge, indeed if the charge only lasted a short time, the positive charge in the cylinder first appeared some little time after the discharge had stopped. It seems possible that while the discharge is passing the gas in the tube is too good a conductor to allow the charge on the cylinder to accumulate; just as in Perrin's experiment the conductivity of the gas prevents the negative charge on the cylinder rising above a certain value, however

<sup>\*</sup> W. Wien, Wied. Ann. lxv. p. 445, 1898.

<sup>†</sup> Ewers, Wied. Ann. lxix. p. 167, 1899.

<sup>†</sup> Villard, Journal de Physique, [3], t. viii. pp. 5 and 140, 1899.

long the cathode rays are kept playing on the cylinder; when the discharge stops, the gas recovers its insulating power, and the cylinder can retain any charge that diffuses into it; if this view is correct, the positive charge observed in the cylinder is due mainly, at any rate, to diffusion and not to convection by the Canalstrahlen.

In spite of the indecisive results obtained by this experiment, the magnetic and electric deflections obtained by W. Wien seem conclusive evidence that the Canalstrahlen carry a positive charge.

On the view of the discharge given in Chap. XVI. there is a stream of positively charged molecules moving towards the cathode, causing this to emit cathode rays; if the cathode is perforated, part of this stream may pass through the holes, producing in the gas behind the cathode luminosity, forming in fact the Canalstrahlen, or positive rays as we may call them, if we think this view of their constitution sufficiently established.

## CHAPTER XVIII.

## RÖNTGEN RAYS.

RÖNTGEN found in 1895 that when the pressure in a discharge tube is so low that the walls of the tube are vividly phosphorescent, rays which are propagated in straight lines come from the tube; these rays illuminate a screen made of phosphorescent substance, and affect a photographic plate placed in their path. Röntgen showed too that these rays were not entirely stopped even by substances opaque to ordinary light, such as the flesh of the hand, and that if the hand is placed between the bulb and a phosphorescent screen, the shadow cast by the flesh is not so dark as that cast by the bones, and thus the shape of the latter can be distinguished. The rays which produce these effects are now called Röntgen rays. The character of the rays depends greatly upon the state of the tube in which they are produced; if the pressure in the tube is very low, so that the potential difference between its terminals is very large, the rays are much more penetrating than when the pressure of the gas is higher, and the potential difference between its electrodes smaller; very penetrating rays are sometimes called hard rays, the more easily absorbable rays, soft ones. We have already seen that even the rays emitted at any one time by the same tube are not all of one type (see p. 246).

We have already discussed a good many of the properties of the Röntgen rays in connection with the power they possess of ionising a gas through which they pass; we shall now consider the other properties of these rays.

Röntgen showed, and the observation has been confirmed by very many subsequent experimenters, that the rays are not bent

when going from one medium to another, and therefore that they suffer no deviation after passing through a solid prism.

We have seen (p. 258) that Röntgen rays when they strike against a solid, a liquid, or even a gas, generate secondary rays which in the case of impact against a solid or a liquid are of a much less penetrating character than the incident ones; the incidence of Röntgen rays on the surface of a solid will therefore give rise to radiation proceeding from the surface; by far the greater part of this 'reflected' radiation is diffuse, i.e. though the incident rays are all travelling in one direction, the 'reflected' rays will spread out in all directions. The question as to whether this 'diffuse return' of the rays, as Sir George Stokes called it, is accompanied by specular reflection, in other words, whether there is an excess of the reflected rays in the direction in which the angle of reflection is equal to the angle of incidence, is one on which observers disagree. Lord Blythswood\* and Rood+ have obtained photographs in which there is evidence of this effect; other observers have, however, been unable to detect it. The specular reflection must in any case be small, since the transparency of a powder is the same as that of the same bulk of material when solid, and the definition through it as good.

No evidence of any polarisation of the rays has been obtained; the opacity of two crystals of tourmaline or of herapathite, placed one on the top of the other, is the same when the axes of the crystals are crossed as when they are parallel.

The Röntgen rays increase the electrical conductivity of badly conducting liquids as well as of gases<sup>†</sup>, they increase also the electric absorption of solids. Curie§ has lately shown that the rays from radium also produce the same effect on liquids.

309. Source of the Rays. By taking photographs of a card pierced with pinholes, and drawing the lines joining the photograph of a hole with the hole itself, and finding their points of intersection, it has been shown that the spot struck by the cathode rays is the place from which the Röntgen rays originate.

<sup>\*</sup> Lord Blythswood, Proc. Roy. Soc. lix. p. 330, 1896.

<sup>+</sup> Rood, Silliman's Journal, [4], ii. p. 173, 1896.

<sup>‡</sup> J. J. Thomson, Nature, lv. p. 606, 1897.

<sup>§</sup> Curie, Comptes Rendus, exxxiv. p. 420, 1902.

Thus when the rays strike the walls of the tube, the phosphorescent part of the glass is the origin of the rays; when a 'focus tube,' i.e. one with a hollow cathode, and a plate of some infusible substance placed where the cathode rays converge, the part of the plate struck by the cathode rays is the source of the Röntgen rays. Campbell Swinton\* has shown that cathode rays impinging normally on the plate are more effective in producing Röntgen rays than those which strike obliquely against the plate. The Röntgen rays produced when the cathode rays strike against a plane area come off approximately uniformly in all directions. This is shown by the following experiment: a hemispherical photographic film is placed so that its centre is at C, a point on a metal plate struck by cathode rays travelling in any direction; the Röntgen rays starting from the plate affect the film, and when the photograph is developed its intensity is found to be approximately uniform until we approach quite close to the line where the plane of the plate intersects the film. When the rays are produced by the impact of the cathode rays against the glass walls of the tube more rays appear to come out from any place normally than obliquely; this is, however, a secondary effect due to the absorption of the rays by the glass through which they have to pass; as the rays which come out obliquely have to pass through a greater thickness of glass than those which emerge normally they are more enfeebled by the absorption due to the glass.

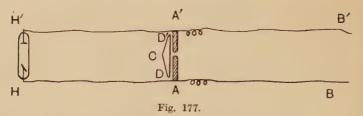
310. Velocity of Propagation of Röntgen Rays. Experiments to determine the velocity of the Röntgen rays have been made by Brunhes† and Blondlot‡. The property used in each distance to detect the rays was the effect these rays have in facilitating the passage of a spark. This property, it must be confessed, does not seem well fitted for the purpose; for since the effect of the rays on the spark is due to the ionisation of the gas close to the spark gap, and as the gas when once ionised would remain so for an appreciable time, the effect of the rays on the spark might persist for some time after the rays had stopped, and thus the brightening of the spark by the rays is not

<sup>\*</sup> Campbell Swinton, Proc. Roy. Soc. lxiii. p. 432, 1898.

<sup>+</sup> Brunhes, Comptes Rendus, cxxx. p. 169, 1900.

<sup>#</sup> Blondlot, Comptes Rendus, exxxv. p. 666, 1902.

conclusive evidence that the rays fall on the spark gap simultaneously with the passage of the spark. The method adopted by Blondlot, in his experiments which have just



been published, is indicated by the diagram in Fig. 177. B, B' are the terminals of the secondary of an induction coil, these are connected with the plates A and A' of a Hertz radiator, and to the terminals H and H' of a tube exhausted sufficiently to emit Röntgen rays. A resonator made of copper wire folded into a triangle CDD' is placed beneath the radiator. The spark gap C of the resonator is placed so that it receives Röntgen rays from the tube HH', but is protected from all other radiation by screens of black paper and an aluminium plate. The radiator AA' consists of two horizontal brass cylinders immersed in vaseline oil. The view taken by Blondlot of the action of this apparatus is as follows: when the current in the primary of the induction coil is broken the difference of potential between H and H' increases until it is sufficient to send a discharge through the tube and cause it to emit Röntgen rays; when the potential difference increases a little further a spark passes between  $\boldsymbol{A}$  and A', short circuiting, as it were, this circuit and extinguishing the discharge through the tube HH'. The length of the gap between A and A' was adjusted so that the potential required to produce the spark was only slightly greater than that required to send a discharge through the tube, so that the tube was extinguished very soon after the spark commenced and the radiator commenced to vibrate. The electromotive force round the resonator will be still longer in rising to a value great enough to spark across C, so that, if the tube is close to C, the Röntgen rays will have left C long before the spark passes, and thus if the effect of the rays on the spark is confined to the time when the rays are actually falling on the spark gap the rays will have no influence upon the spark. Blondlot found that in this case the sparks are

not affected by placing a lead plate between the tube HH' and the spark gap C. If now long wires are inserted between A and Hand A' and H', the extinction of the rays in the tube HH' will take place at a longer interval after the commencement of the spark between A and A', and if the wires are sufficiently long the delay may be so great that the spark may have commenced at C before the rays have ceased to fall upon the spark gap, so that the rays may increase the brilliancy of the spark; in this case Blondlot found that the interposition of a lead plate diminished the brightness of the spark. The arrival of the rays at the spark gap can also be delayed by moving the tube HH' away, keeping the lengths of wire between A and H and A' and H' constant, but uncoiling the wire so as to allow of the motion of HH'. Blondlot found that moving the tube away increases the brightness of the sparks when the Röntgen rays fall on the spark gap, but when the rays are stopped by a lead plate the motion of the tube has no effect upon the sparks. When the tube is just so far away from the gap that the rays pass through the gap during the whole of the time the sparks are passing across  $\hat{C}$ , the effect of the rays will be a maximum, for increasing the distance of the tube from the gap will diminish the intensity of the rays at the spark gap without increasing the time during which they and the electric field act together at the gap: pushing the tube nearer the gap diminishes the time of conjoint action of the rays and field at the spark gap. Let us suppose that the tube is in such a position that the sparks are at their brightest, and suppose now that the length of the wires between A and H and also between A' and H' is shortened by a length l; let Vbe the velocity of propagation of an electrical disturbance along  ${f a}$  wire, then if we suppose that the extinction of the bulb HH'is due to the propagation of the drop of potential at AA' produced by the short circuiting of this circuit by the spark, the rays will terminate at the time l/V earlier than they did before; if they were just contemporaneous with the force at the gap before, they can be made so again by moving the tube a distance l' further from the gap without altering the length of the wires, provided l'/V' = l/V, where V' is the velocity of Röntgen rays through air; provided also that the lengthening of the wires and the displacement of the tube does not affect the magnitude and duration of the forces acting on the spark gap. Blondlot's

method is then to start with the bulb in the position in which the sparks are brightest, shorten or lengthen the wires AH and A'H' by l, and then measure the distance l' through which he has to displace the tube until the brightness of the sparks is again a maximum; then we have, on the preceding theory, V'/V = l'/l. Blondlot found, as the result of a large number of experiments, that l' is equal to l; hence he concludes that the velocity of propagation of Röntgen rays through the air is equal to the velocity of propagation of an electrical disturbance along a metal wire, and this is known to be equal to the velocity of light; so that he regards the experiments as proving that the velocity of Röntgen rays is the same as that of light.

I do not see how Blondlot's explanation of the effects could apply unless the effects produced by the rays on the spark gap ceased simultaneously with the rays, and if this effect is due to the ionisation of the gas round the air gap we should expect the effect to last some time after the rays cease.

311. Diffraction of Röntgen Rays. Many experiments have been made to test whether, as in the case of light, there are both inside and outside the boundary of the shadows cast by very small objects, variations in the intensity of the rays corresponding to the well-known diffraction fringes. Röntgen\*, who investigated this point, was never able to satisfy himself that the effects he obtained were undoubtedly due to diffraction. Fomm<sup>†</sup> observed in the photograph of a narrow slit light and dark bands which looked like diffraction bands, but observations with different sized slits showed that this could not be their origin, and Haga and Wind; have explained them as contrast These observers, who have made long-continued researches on this subject, have obtained with a narrow V-shaped slit, only a few thousandths of a millimetre broad at its widest point and made of platinum plates about half a millimetre thick. effects which would be produced by diffraction, and which have not been explained in any other way. The image of such a slit is shown on a greatly magnified scale in Fig. 178 §: this diagram

<sup>\*</sup> Röntgen, Wied. Ann. lxiv. p. 18, 1898.

<sup>†</sup> Fomm, Wied. Ann. lix. p. 350, 1896.

<sup>‡</sup> Haga and Wind, Wied. Ann. lxviii. p. 884, 1899.

<sup>§</sup> Wind, Physikalische Zeitschrift, ii. p. 292, 1901.

represents one of the photographs with its vertical dimensions magnified two hundred times, while the horizontal dimensions are



Fig. 178.

only doubled. The broadening of the narrow part of the shadow is the effect relied upon for showing the diffraction. To obtain a similar amount of broadening with light of a definite wave length, the length of the wave would have to be of the order  $2 \times 10^{-8}$  cm. If we regard the Röntgen rays as due to discontinuous pulses, this will be the order of the thickness of the pulse for the particular rays under consideration.

312. We have no evidence that the Röntgen rays suffer any deflection when passing through magnetic fields strong enough to produce very large deflections of cathode rays.

#### CHAPTER XIX.

### PROPERTIES OF MOVING ELECTRIFIED BODIES.

313. As Röntgen rays are produced when the cathode rays strike against an obstacle, and as the cathode rays consist of negatively charged particles, it is of interest to examine the effects which are produced when the motion of a charged particle is suddenly stopped.

When a particle with a charge e of electricity is moving uniformly parallel to the axis of z with a velocity w, it produces at a point whose coordinates relative to the particle are x, y, z, a radial electric polarization equal to

$$\frac{e}{4\pi} \frac{V}{(V^2 - w^2)^{\frac{1}{2}}} \left\{ \frac{x^2 + y^2 + z^2}{\left(x^2 + y^2 + \frac{V^2}{V^2 - w^2} z^2\right)^3} \right\}^{\frac{1}{2}},$$

and a magnetic force whose components  $\alpha$ ,  $\beta$ ,  $\gamma$  parallel to the axes of x, y, z respectively are given by the equations

$$\begin{split} \alpha &= -\frac{e\,Vw}{(\,V^2 - \,w^2\,)^{\frac{1}{2}}} \, \frac{y}{\left\{x^2 + \,y^2 + \frac{V^2}{V^2 - \,w^2}\,z^2\right\}^{\frac{3}{2}}}, \\ \beta &= \frac{e\,Vw}{(\,V^2 - \,w^2\,)^{\frac{1}{2}}} \, \frac{x}{\left\{x^2 + \,y^2 + \frac{V^2}{V^2 - \,w^2}\,z^2\right\}^{\frac{3}{2}}}, \\ \gamma &= 0, \end{split}$$

V being the velocity of propagation of electrodynamic disturbances through the medium surrounding the sphere (see Recent Researches in Electricity and Magnetism, pp. 18—19).

When w the velocity with which the particle is moving is small compared with V, the radial electric polarization becomes

$$rac{e}{4\pi} rac{1}{\{x^2 + y^2 + z^2\}},$$

the same as when the particle is at rest; and the components of the magnetic force are given by

$$\alpha = -ew \frac{y}{(x^2 + y^2 + z^2)^{\frac{3}{2}}},$$

$$\beta = ew \frac{x}{(x^2 + y^2 + z^2)^{\frac{3}{2}}},$$

$$\gamma = 0.$$

**314.** In an electric field in which the components of the electric polarization are f, g, h, those of the magnetic induction a, b, c, there is mechanical momentum, the components U, V, W of which per unit volume are given by the equations

$$U = cg - bh,$$

$$V = ah - cf,$$

$$W = bf - ag$$

(see Recent Researches, p. 13).

Substituting the expressions we have given for the polarization and magnetic force due to the moving charged particle and integrating throughout the space outside a small sphere of radius a described round the electrified point we find if P, Q, R are the components of the resultant momentum of the medium outside the sphere in this direction

$$P = 0, Q = 0,$$

$$R = \frac{1}{2} \frac{\mu e^2}{a} \frac{V^2}{(V^2 - w^2)^{\frac{1}{2}}} \left\{ \Im\left(1 - \frac{1}{4} \frac{V^2}{w^2}\right) + \frac{1}{2} \sin 2\Im\left(1 + \frac{1}{2} \frac{V^2}{w^2} \cos 2\Im\right) \right\}$$
.....(1),

where  $\mu$  is the magnetic permeability of the medium and

$$\sin \Im = \frac{w}{V}$$

(see Recent Researches, p. 21); when w is small compared with V, the value of R reduces to

$$\frac{2}{3}\frac{\mu e^2}{a}w.$$

Thus if m' is the mass of the particle the momentum due to its motion is not m'w but in virtue of the momentum in the electromagnetic field

$$m'w + R$$

or when w is small

$$\left(m' + \frac{2}{3} \frac{\mu e^2}{a}\right) w.$$

Thus the particle will in this case behave as if its mass were increased by  $\frac{2}{3}\frac{\mu e^2}{a}$ .

315. In the general case when w is not small, let  $\chi$  denote m'w + R and suppose the particle is acted on by a magnetic force H at right angles to its direction of motion, the mechanical force acting upon the particle is Hew, hence if in the time  $\delta t$  the direction of motion is deflected through an angle  $\delta \theta$  we have

$$\chi \delta \theta = Hew \delta t$$
;

if  $\delta s$  be an element of the path,  $\rho$  its radius of curvature, then

 $\delta\theta = \frac{\delta s}{\rho} = \frac{w \, \delta t}{\rho},$  $\rho = \frac{\chi}{H_0};$ 

hence

but if e/m is the ratio of the charge to the effective mass then

 $\rho = \frac{mw}{He},$ 

hence

$$m = \frac{\chi}{w} = m' + \frac{R}{w}.$$

Now from the expression (1) for R we see that when w approaches V, R/w increases rapidly, hence if what we may call the electrical mass is comparable with the mechanical, we should expect m/e would vary with the velocity of the particle, increasing as the velocity increases. From the expression given for R we see that it is only with particles moving with velocities comparable with that of light that we could expect to get measurable variations in the value of m/e; happily particles travelling with these speeds are furnished by radium and the value of m/e for these rapidly moving molecules has been made the subject of a most interesting research by Kaufmann\*.

<sup>\*</sup> Kaufmann, Göttingen Nach., Nov. 8, 1901.

316. The method used by Kaufmann is illustrated in Fig. 179.

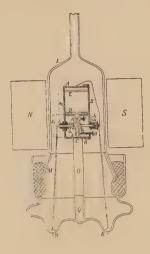


Fig. 179.

A small piece of radium was placed at C in a vessel from which the air was extracted, the radiations from the radium passed through a strong electric field in the space between the parallel plates  $P_1$ ,  $P_2$  which were 1525 cm. apart and maintained at a potential difference of 6750 volts, they then passed through a small hole D in a diaphragm and then on to a photographic plate E; during the whole of their journey from C to E the rays were under the influence of a magnetic field produced by the electromagnet NS; the deflection due to the magnetic field was at right angles to that due to the electric. If the electric and magnetic fields were not in action all the rays from the radium would strike the photographic plate at the same point, when however the rays are exposed to the electric and magnetic fields the deflection will depend upon the velocity, so that the rays of different velocities will now strike the plate at different points and the impression produced by the radium on a plate will be a curved line; by measuring the photograph the deflection due to the magnetic field and also that due to the electric field can be found, and from these deflections (see Chap. V.) the values of v the velocity of the particles and the corresponding value of e/m can be found. Kaufmann found that when his plates were exposed for several

days he got a clearly defined curve from which he deduced the following values of e/m and v.

$v \times 10^{-10}$	$e/m \times 10^{-7}$	
2.83	.63	
2·72	·77	
2·59	·975	
2:48	1·17	
2:36	1·31	

It is clear from these numbers that e/m diminishes as the velocity of the particle increases, so that if e remains the same the value of m increases with the velocity. As this increase must be due to the 'electrical mass' it follows that the electrical mass must be comparable with the mechanical mass. To find the proportion between the two, we must make some assumption as to the distribution of electricity on the corpuscle. Kaufmann assumed that the distribution was the same as if the corpuscle were a conducting sphere; the electrical field due to a moving conducting sphere has been solved in great detail by Searle\*. On this supposition Kaufmann calculated from his experiments that the electrical mass of a slowly moving corpuscle was about \frac{1}{2} of the mechanical mass. He points out that the proportion will depend upon the assumption made as to the distribution of electricity over the corpuscle, and in a later paper he shows that his experiments are consistent with the view that the whole of the mass is electrical.

There does not seem to me any reason for attributing electrical conductivity to the corpuscle itself, and I prefer to take another view of the electric field due to a corpuscle and to assume that it coincides with that part of the field due to a point charge which is outside a small sphere of radius a having the point charge for centre. On this supposition the electrical mass is R/w where R is given by equation (1). Using this formula I have calculated, on the supposition that the whole of the mass is electrical, the ratios of the masses of the corpuscles moving with the velocities occurring in Kaufmann's experiments to the mass of a corpuscle

<sup>\*</sup> Searle, Phil. Mag. v. 44, p. 340, 1897.

moving with an exceedingly small velocity; the values of this ratio  $(\rho)$  are given in the following table,  $\rho'$  are the values observed by Kaufmann.

$v \times 10^{-10}$	ρ'	ρ
2·85	3·1	3:09
2·72	2·42	2:43
2·59	2·0	2:04
2·48	1·66	1:83
2·36	1·5	1:65

Thus the observed and calculated values of  $\rho$  do not differ by more than 10 per cent., suggesting that all the mass of the corpuscles is electrical in its origin. On this supposition the mass of a slowly moving corpuscle is  $\frac{2}{3}\frac{\mu e^2}{a}$  or  $m/e = \frac{2}{3}\mu e/a$ , from the known values of m/e and e we find a to be about  $10^{-13}$  cm. As the mass of a corpuscle has been seen to have an electrical origin the question naturally suggests itself whether the masses of all bodies may not have the same origin.

317. The phenomena we have described in the earlier part of the book show that corpuscles are a constituent of all bodies, so that part of the mass of these bodies is due to the corpuscles and is therefore electrical: it is easy to imagine a form of atom for which the whole mass would be electrical. For suppose that the atoms are made up of a large number of negatively electrified corpuscles each corpuscle being associated with its corresponding positive charge, and suppose that these positive charges are spread over a much greater volume than the corpuscles, the aggregation thus formed would consist of a distribution of positive electricity through a sphere, the corpuscles being distributed through the sphere in such a way as to be in equilibrium under their own repulsions and the attractive force to the centre of the sphere arising from the positive electrification, in fact we should get an atom similar to that described by Lord Kelvin in his paper "Æpinus Atomized" (Phil. Mag. Mar. 1902). If the radius of the sphere occupied by the positive electrification is large compared with the radius of a corpuscle, it is easy to show that the mass of the atom will only differ slightly from the sum of the masses of the individual

corpuscles considered as discrete systems. Thus in any aggregation or dissociation of a system of atoms the changes in the mass would, since the number of corpuscles remains unaltered, be exceedingly small in comparison with the whole mass of the atoms in any particular state.

318. There is another point of view from which we may regard the question of electrical mass which may perhaps be most easily explained by considering the simple case of a moving charged particle. If a, b, c are the components of the magnetic induction, f, g, h those of the polarization, i.e. the number of Faraday tubes passing through unit area at right angles to their length, then (see *Recent Researches*, p. 13) the components of the momentum in the field are

$$cg - bh$$
,  $ah - cf$ ,  $bf - ag$ .

The magnetic field is due to the motion of the Faraday tubes, and if the charged point is moving parallel to the axis of z with a velocity w we have (see *Recent Researches*, p. 8)

$$a = -4\pi\mu wg,$$

$$b = 4\pi\mu wf,$$

$$c = 0,$$

where  $\mu$  is the magnetic permeability of the medium through which the Faraday tubes are moving. Substituting these values for a, b, c in the expressions for the components of the momentum we find that these become

$$-4\pi\mu w f h$$
,  $-4\pi\mu w g h$ ,  $4\pi\mu (f^z + g^z + h^z) w - 4\pi\mu h^z w$ .

Thus the resultant momentum is at right angles to the direction of the Faraday tube and is in the plane through the tube and the direction of motion of the particle, the magnitude of the resultant momentum is

$$4\pi\mu\left(f^{2}+g^{2}+h^{2}\right)w\sin\theta,$$

where  $\theta$  is the angle between the Faraday tube and its direction of motion, thus  $w \sin \theta$  is the velocity of the tube at right angles to its length. Hence we see that the momentum in the field is the same as would exist if the Faraday tubes carry with them when they move at right angles to themselves a mass of the ether equal per unit volume to  $4\pi\mu \, (f^2 + g^2 + h^2)$ , while when the tubes move parallel to their length they do not drag any ether along with

them. The momentum in the field is the momentum of this bound ether. Thus on this view the electrical mass of a charged body represents the mass of the ether dragged along or imprisoned by the Faraday tubes associated with that body, and thus on the hypothesis mentioned above that all mass is electrical in its origin it would follow that the mass of all bodies has its origin in the ether dragged along by the Faraday tubes associated with the body (see *Proceedings of Cambridge Philosophical Society*, Mar. 1903); the author hopes shortly to publish a more detailed account of the consequences which result from this point of view.

Effect of suddenly stopping a moving charged particle.

319. The author gave an analytical investigation of this question in the *Philosophical Magazine* for Feb. 1897; the following geometrical treatment of the same problem is based upon the method of Faraday tubes. Let us consider the case of a charged point moving so slowly that the Faraday tubes are uniformly distributed, and suppose the point to be suddenly stopped, the effect of stopping the point will be that a pulse travels outwards from it with the velocity V, but as the Faraday tubes have inertia they will until the pulse reaches them go on moving uniformly

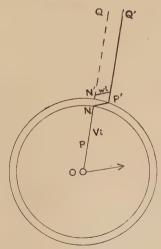


Fig. 180.

with a velocity w parallel to the axis of z, i.e. they will continue in the same state of motion as before the stoppage of the point.

Let us consider the behaviour of a tube which at the moment of stopping the charge had the position PQ, and consider the state of things after an interval t from the stoppage; a pulse whose thickness  $\delta$  depends on the time taken to stop the particle will have travelled out to a distance Vt. In front of this pulse the motion of the tubes will not have been affected, i.e. they have travelled parallel to themselves through a distance wt parallel to the axis of z; behind the pulse the tube will have been brought to rest along the line it occupied when the point was stopped, thus the portions behind and in front of the pulse will be represented by ON, P'Q' in Fig. 180. Hence to preserve the continuity

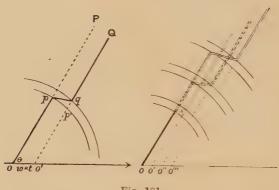


Fig. 181.

of the tube it must bend sharply round in the pulse itself, so that now the tube has a considerable tangential component. The stoppage of the point will thus produce a tangential component in the electric force which we proceed to calculate, supposing that the pulse is very thin so that the tube in it may be regarded as approximately straight. Then

$$\frac{\text{tangential electric polarization}}{\text{normal electric polarization}} = \frac{P'N'}{NN'} = \frac{w \sin \theta t}{\delta} \dots (1),$$

where t is the time which has elapsed since the stoppage of the particle and  $\delta$  is the thickness of the pulse.

The left-hand diagram in Fig. 181 shows the configuration of the tube at the times when, if the particle had not been stopped, it would have been at o', o", o".

Since the normal electric polarization at a distance r from the

particle is equal to  $e/4\pi r^2$  and if V is the velocity of propagation of the disturbance Vt = r, we have from (1)

tangential electric polarization = 
$$\frac{e}{4\pi r\delta} \frac{w \sin \theta}{V}$$
;

as this electric polarization is moving at right angles to itself

with a velocity V it produces a magnetic force at right angles to the polarization and to its direction of motion, i.e. parallel to, but in the opposite direction to the magnetic force before the particle was stopped and equal to  $4\pi V$  times the polarization, i.e. to  $\frac{e}{x^{3}}w\sin\theta$ ; hence in the pulse we have (1) a tangential electric polarization equal to  $ew \sin \theta/4\pi r \delta V$ , and (2) a magnetic force equal to  $ew \sin \theta/r\delta$ ; as these only vary inversely as the distance from the particle while the polarization and magnetic force before the particle was stopped varied inversely as the square of the distance, their magnitudes in the pulse will except in the immediate neighbourhood of the particle be very great compared with their values outside the pulse. Thus the stoppage of the charged particle is accompanied by the propagation outwards of a thin pulse of very intense electric and magnetic force; pulses produced in this way constitute I believe the Röntgen rays. It will be seen that on the Electromagnetic Theory of Light the pulses which we suppose to constitute the Röntgen rays are in many respects identical with waves of visible light; both consist of electric and magnetic forces at right angles to

each other and to the direction of propagation; the difference between the Röntgen rays and a beam of sodium light is that the thickness of the Röntgen ray pulse is very small compared with the wave-length of sodium light, and that in the Röntgen rays there is not that regular periodic character occurring in a train of waves of constant wave-length. Sir George Stokes in the Wilde Lecture given before the Manchester Philosophical Society showed that many of the differences between Röntgen rays and ordinary light, such for example as the absence of refraction, could be explained by the theory that the Röntgen

rays consisted of pulses whose thickness was very small compared with the wave-length of visible light.

A very complete investigation of the diffraction of Röntgen rays from this point of view has been given by Sommerfeld\*.

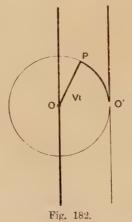
<sup>\*</sup> Sommerfeld, Physik. Zeit. (1) p. 105, (2) p. 55, 1900.

320. If H is the magnetic force in the pulse the energy per unit volume of the pulse is  $\frac{\mu}{4\pi}H^2$  (half of this is due to the magnetic and half to the electric field), substituting the value given for H and integrating throughout the volume of the pulse we find that the energy in the pulse is

 $\frac{2}{3}\frac{\mu e^2w^2}{\delta}$ 

Thus the amount of energy radiated away in the pulse varies inversely as the thickness of the pulse, and the thickness of the pulse depends upon the abruptness with which the particle is stopped; if the stoppage is very abrupt the pulse is thin, if it is gradual it is wide. The amount of energy radiated away in Röntgen rays bears to the energy in the field the ratio of 2a to  $\delta$ , where a is the radius of the corpuscle; see p. 532. If  $\delta$  is equal to 2a then all the energy (assuming that the mass of the particle arises wholly from electrical causes) will be radiated away; with thicker pulses only a portion of the energy is radiated, the rest is absorbed where the particle is stopped.

321. In the preceding investigation we have supposed that the velocity of the particle is small compared with the velocity of light, the same method will however apply when this limitation is removed.



When the particle moves with the velocity of light the electric and magnetic forces before the stoppage are confined to a plane through the centre of the sphere at right angles to its direction of motion. To find the effect at a time t after the stoppage of such a

particle we apply the same principle as before, that outside a pulse whose radius is Vt the field is the same as if the particle had gone on moving uniformly with the velocity it had when stopped, and that between the charged particle and the pulse the distribution of Faraday tubes is uniform. Thus we shall find a deformation of the Faraday tubes such as is shown in Fig. 183; the plane of magnetic and electric force travels on as if the particle had not been stopped, since it always keeps just outside the sphere of radius Vt and there is in addition a spherical pulse formed by the parts joining the Faraday tubes inside the sphere to those outside.

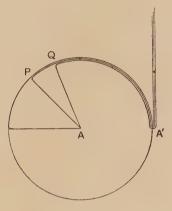


Fig. 183.

322. To find the magnitude of the tangential polarization T we may proceed as follows. Consider an element of the pulse ABCDEFGH formed by the intersection of two meridian planes ABFE, DCGH inclined at an angle  $\delta\phi$  and two cones BCGF, ADHE whose semi-vertical angles are  $\theta$  and  $\theta + d\theta$  with the outer and inner spheres bounding the pulse, then since there is no free electricity inside this element the number of lines of force which leave the face BCGF must equal the sum of the numbers entering the faces ADEH and EFGH, hence if  $\delta$  is the thickness of the pulse, T the tangential polarization, we have

$$\frac{d}{d\theta} (T\delta r \sin \theta \, d\phi) \, d\theta = \frac{e}{4\pi r^2} r d\theta \, r \sin \theta \, d\phi,$$
$$\frac{d}{d\theta} (T\delta r \sin \theta) = \frac{e}{4\pi} \sin \theta,$$

or 
$$T = \frac{e}{4\pi r \delta} \frac{1 - \cos \theta}{\sin \theta},$$

and H the magnetic force in the spherical pulse is given by the equation

$$H = \frac{eV}{r\delta} \frac{1 - \cos \theta}{\sin \theta}.$$

Magnetic and Electric Forces due to the acceleration of charged particles.

323. In the investigation in Art. 319 we supposed that the particle was reduced to rest; exactly the same method will however give us the effects produced when smaller changes in the velocity of the particle occur and when the velocity of the particle is altered without being destroyed. We saw in Art. 319 that when a particle moving with a velocity w is reduced to rest, *i.e.* when a change w is produced in the velocity, a tangential electric polarization T and a tangential magnetic force H are produced which, at a distance r from the particle, are at the time r/V after stopping the particle given by the equations

$$T = \frac{ew \sin \theta}{4\pi r \delta V}, \quad H = \frac{ew \sin \theta}{r \delta};$$

if  $\tau$  is the time taken to stop the particle,  $\delta$  (the thickness of the pulse) is equal to  $V\tau$ , hence we may write

$$T = \frac{ew \sin \theta}{4\pi V^2 r \tau}, \ H = \frac{ew \sin \theta}{r V \tau}.$$

If now the velocity of the particle instead of being diminished by w in the time  $\tau$  is increased by  $\delta w$  in the same time, we can prove by exactly the same method that there will be a tangential electric polarization T' and a magnetic force H' given by the equations

$$T' = - \, \frac{e \delta w \sin \, \theta}{4 \pi \, V^2 r \tau} \, , \quad H' = - \, \frac{e \delta w \sin \, \theta}{r \, V \tau} \, ; \label{eq:T'}$$

since  $\delta w$  is the increase in the velocity in the time  $\tau$ ,  $\delta w = f\tau$ , where f is the acceleration of the particle; hence substituting this value for  $\delta w$ , we have

$$T' = -\frac{ef\sin\theta}{4\pi V^2 r}, \quad H' = -\frac{ef\sin\theta}{rV},$$

thus an accelerated charged particle produces in the surrounding field tangential, magnetic, and electric forces which vary inversely as the distance from the particle.

By Poynting's theorem the rate at which energy is flowing radially through unit area of surface is  $V^2T'H'$ ; integrating this expression over the surface of a sphere having its centre at the particle, we find that the rate at which energy crosses the surface is  $\frac{2}{3}\frac{e^2f^2}{V}$ , a result given by Larmor (*Phil. Mag.* v. 44, p. 503, 1897).

**324.** The radiation of energy from the moving charged particle will modify its motion; thus supposing the particle to have the mass m and to be acted upon by a uniform force X, then if v is the velocity of the particle the kinetic energy is  $\frac{1}{2}mv^2$  and the acceleration is  $\frac{dv}{dt}$ ; suppose that in time  $\delta t$  the particle moves over a distance  $\delta x$ , the work done on the particle by the external force is  $Xe\delta x$ , this work must equal the increase in the kinetic energy plus the energy radiated away in time  $\delta t$ , hence

$$Xe\delta x = \delta\left(\frac{1}{2}mv^{2}\right) + \frac{2}{3}\frac{e^{2}}{V}\left(\frac{dv}{dt}\right)^{2}\delta t,$$

$$Xev = mv\frac{dv}{dt} + \frac{2}{3}\frac{e^{2}}{V}\left(\frac{dv}{dt}\right)^{2}.....(1);$$

or

we see from this equation that if the particle starts from rest its acceleration is initially zero instead of Xe/m.

Solving equation (1), we find

$$t = \frac{2}{3} \frac{e^2}{V} \frac{1}{m} \left\{ \log \frac{Xe}{Xe - m \frac{dv}{dt}} + \frac{m \frac{dv}{dt}}{Xe - m \frac{dv}{dt}} \right\} \dots (2).$$

Thus if T is the time required for the acceleration to reach half its final value Xe/m, we have

$$T = \frac{2}{3} \frac{e^2}{V} \frac{1}{m} \{ \log_e 2 + 1 \}.$$

Thus, until a time comparable with  $e^2/Vm$  has elapsed, the acceleration of the particle and therefore the rate at which it is losing energy by radiation will be small compared with their

final values; thus if a pulse of electric force passes over a charged particle a much smaller proportion of the energy in the pulse will be radiated away if the pulse is so thin that the time taken for it to pass over the particle is comparable with T than will be radiated from the thick pulses whose time of transit is much longer, for then the thin pulses will have much greater penetrating power than the thick ones. The expression given in Art. 138 for the coefficient of absorption of a Röntgen ray only applies to the case when the pulse is so thick that the time taken for it to pass over a charged particle is large compared with  $e^2/mV$ , the coefficient of absorption for thinner pulses is much smaller.

# SUPPLEMENTARY NOTES.

#### CHAPTER I.

EXPERIMENTS made by McClennan (American Physical Society, Dec. 1902), Rutherford and Cooke (ibid.), Strutt (Nature, Feb. 19, 1903) have shown that the leak through air in a closed vessel depends upon the material of which the walls of the vessel are made; the variations with different substances are very considerable, thus Strutt found that with one specimen of platinum for the walls of the vessel, the current through the vessel was three times that when the walls were made of glass. This shows that part of the ionisation is due to radiation given out by the walls. The same conclusion had previously been arrived at by Patterson (Proc. Camb. Phil. Soc. XII. p. 44); as the result of his experiments on the variation of the current through a large vessel with the pressure; he found that starting from atmospheric pressure the first diminution of pressure produced little or no effect upon the leak, it was not until the pressure had been considerably reduced that diminution in pressure produced a proportionate diminution in the rate of leak, this is precisely what would occur if the ionisation were due to easily absorbed rays given out by the sides of the vessel which at high pressures got absorbed before they reached the opposite sides of the vessel, for in this case as long as the pressure is high enough to make the gas absorb all the rays before they travel across the vessel, the number of ions produced and therefore the saturation current will be independent of the pressure; when however the pressure is reduced so low that the rays given out by the walls are able to travel across the vessel without being absorbed a diminution of the pressure will diminish the ionization and therefore the saturation current. Strutt (loc. cit.) has observed similar effects.

Part of the ionization in a closed vessel seems to be due to a very penetrating radiation which traverses the walls of the vessel, for McClennan (loc. cit.) and Rutherford have shown that if the vessel be shielded by an envelope of lead or a thick layer of water the saturation current is reduced by about 20 °/<sub>o</sub>. We do not know yet whether

the ionisation due to these very penetrating rays is directly due to their passage through the gas or whether it arises mainly from a more absorbable secondary radiation excited in the walls of the vessel by the passage through them of the more penetrating rays. Patterson's experiments seem to point to the latter as the more probable. These penetrating rays may possibly come from the constituent of the atmosphere which produces the induced radio-activity on a negatively-electrified rod (see page 328). Rutherford has shown that this gives out penetrating rays; the same substance seems to be the origin of the radio-activity which C. T. R. Wilson has observed in freshly fallen rain, as the rate at which this dies away is about the same as that on a negatively electrified wire. The substance apparently deposits on the drops as they fall through the air.

The radiation from the walls seems most probably due to a trace of a very radio-active substance present in the material, as walls made of different samples of the same substances such as lead, platinum or tinfoil give very different ionisations.

Elster and Geitel (*Physikalische Zeitschrift*, III. p. 574) show that air absorbed in the soil possesses very much greater conductivity than atmospheric air. It is shown (p. 553) that water from deep wells contains a radio-active gas very similar in its properties to the emanation of radium. The diffusion of these gases from the soil and water into the air must increase its conductivity; they cannot however explain the conductivity of a gas shut up in a closed vessel, as the activity of the gas derived from water dies away to half its value in a few days. Thus after the gas had been shut up for a week or two this course of radio-activity would disappear, and we must look to other causes to explain the conductivity of gases confined in closed vessels; the experiments described above indicate that the ionisation may be due to radiation from the sides of the vessel and to rays from outside penetrating the walls.

With reference to meteorological observations on the state of ionisation of the air it may be well to point out that observations on the rate of escape from an electrified body in the open air are of little value as the current is not saturated and the leak depends upon the velocity as well as upon the number of the ions. We can test the number of ions present in the air when in a steady state by drawing it rapidly through a tube and measuring the saturation current between an axial wire and the tube. To determine the rate at which ions are being produced in the free air is very difficult, as to get the current saturated we must enclose the air in a vessel and then we get the additional ionisation due to the walls of the vessel.

#### CHAPTER II.

Since this work was in type M. Langevin has published in his remarkably able thesis, Recherches sur les gaz ionises, University of Paris, 1902, some very important investigations on the law of the recombination of ions and the velocities of the ions in the electric field. He shows by a simple calculation that the recombination of the positive and negative ions is brought about by the approach of the ions caused by the electrical attraction between them; if it were not for this attraction the rate of recombination of the ions would be very small compared with that which actually exists. The number of collisions between the positive and negative ions caused by their mutual attraction can easily be shown to equal  $4\pi (k_1 + k_2) ePN$ , when  $k_1$  and  $k_2$  are the velocities of the positive and negative ions under unit electric force P and N respectively, the number of positive and negative ions in unit volume, if every collision resulted in recombination, then a, the coefficient of recombination as defined on p. 15, would equal

$$4\pi (k_1 + k_2) e$$
,

only a fraction of the collisions will however result in recombination, in the other cases the kinetic energy acquired by the ions in their approach to each other will cause them to separate again after collision, and at low pressure when the velocities of the ions under electric forces are large, this fraction should be less than at high pressures when the velocities are small, if  $\epsilon$  is the fraction of the number of collisions which result in recombination

$$a = 4\pi\epsilon (k_1 + k_2) e$$
.

Langevin determines the value of  $\epsilon$  by the following method: if the gas between two parallel metal plates maintained at a constant difference of potential is exposed to Röntgen rays for the exceedingly small time during which a single discharge from an induction coil lasts, the ions produced in the space between the plates will begin to move towards the plates, the positive ions moving towards the negative plate, and the negative towards the positive; as the ions move past each other some of them will recombine, so that Q the number of negative ions coming up to the positive plate will be less than  $Q_0$ , the number of negative ions produced by the Röntgen rays between the plates, the stronger the electric field between the plates the faster will the ions move up to the plates and the less time will there be for them to recombine and in consequence the less the difference between Q and  $Q_0$ . Langevin shows that if  $\sigma$  is the density of the electricity on the electrified plates

 $\frac{\epsilon Q}{\sigma} = \log\left(1 + \frac{\epsilon Q_0}{\sigma}\right).$ 

From this expression it is possible to calculate  $\epsilon$ ; the results of Langevin's experiments are shown in the following table:

Air		CO <sub>2</sub>	1
Pressure in mm.	€	Pressure in mm.	· · ·
152	0.01	135	0.01
375	0.06	352	0.13
760	0.27	550	0.27
1550	0.62	758	0.21
2320	0.80	1560	0.95
5 atm.	0.90	2380	0.97
		1	

The effect of pressure on the chance of collision resulting in recombination is very clearly seen; thus at the pressure of 152 mm. only one collision in one hundred results in recombination, at the atmospheric pressure the number has increased to one in four and at the pressure of 5 atm. to nine out of ten.

From the equation

$$\alpha = 4\pi\epsilon (k_1 + k_2) e_1$$

' a/e can be deduced when  $\epsilon$  is known.

The values got by Langevin, McClung, and Townsend are in close agreement, they are given in the following table:

	a/e			
	Langevin	McClung	Townsend	
Air	3200	3384	3400	
$CO_2$	3400	3492	3500	

Method of determining the velocity of the ions under an electric field.

Langevin has determined  $k_1$  and  $k_2$  by the following method; suppose the region between the parallel plates AB, CD is exposed for a very short space of time to Röntgen rays, if there is such a strong electric field between the plates that the recombination of the ions can be neglected, then if the field were kept in one direction all the negative ions would go to the positive plate and all the positive ones to

the negative; if however the field were reversed before all the ions got across, then the charge received by a plate would be less than in the previous case, the difference would evidently depend upon the velocities of the ions; if we make a series of measurements of the charge received by the plate when the field is reversed at different intervals after the ionisation we shall evidently have the means of determining  $k_1$  and  $k_2$ .

The numbers obtained by Langevin by this method are at atmospheric pressure.

	Air		$\mathrm{CO}_2$		
$k_1$	$k_2$	$k_{2}/k_{1}$	$k_1$	$k_2$	$k_2/k_1$
420	510	1.22	257	270	1.05

Langevin also investigated the variation of the velocity with the pressure; as explained in the text the velocity of an ion should vary inversely as the pressure as long as the nature of the ion does not change, as however the negative ion at very low pressures is the corpuscle, while at atmospheric pressures it is the corpuscle attached to several molecules of the gas, we must as we reduce the pressure arrive at a stage where the negative ion begins to get simpler and when therefore the velocity will increase more rapidly than the reciprocal of the pressure, this effect is clearly shown by the results of Langevin's experiments, which are given in the following table:

Negative ions		Positive ions			
p	$k_2$	$pk_2/76$	p	$k_1$	$pk_{1}/76$
7·5 (cm.) 20·0 41·5 76·0 142·0	6560 2204 994 510 270	647 580 530 510 505	7·5 (cm.) 20·0 41·5 76·0 142·0	4430 1634 782 420 225	437 430 427 420 425

The velocities  $k_1$  and  $k_2$  are under unit electrostatic force, *i.e.* 300 volts per cm.

The increase in the value of  $pk_2$  with diminished pressure for pressures below 20 cm. is clearly marked. There is a rise but a much smaller one in the value of  $pk_1$ .

Page 19. McClung has lately investigated at the Cavendish Laboratory the effect of temperature upon a, and finds that a increases rapidly as the temperature increases.

#### CHAPTER VI., p. 130.

H. A. Wilson has determined (*Phil. Mag.* [6] v., p. 429, 1903) e the charge on an ion as follows: he produces a cloud in the ionised gas, using an expansion which will produce condensation on the negative but not on the positive ions, thus all the drops are negatively electrified; he then observes the rate of fall of these drops in an electric field, the electric force being vertical; if X is the value of the force, acting so as to make the drop move upwards, e the charge on the drop, and a its radius, the downward force on the drop is  $g + \frac{4}{3}\pi a^3 - Xe$ ; hence by Stokes's rule the velocity v with which the drop falls will be given by the equal

$$v = \frac{2}{9} \left( g - \frac{3Xe}{4\pi a^3} \right) \frac{a^2}{\mu};$$

thus by measuring v for different values of X we can get a and e; by this method Wilson finds

 $e = 3.1 \times 10^{-10}$  (c. g. s. electrostatic units).

## CHAPTER VII., p. 144.

C. T. R. Wilson has recently shown by using a very large vessel for the expansion that the few nuclei which act as centres of condensation in a gas not exposed to external ionising influences such as Röntgen rays carry charges and can, like those due to the Röntgen rays, be removed by an electric field. He shows that the reason that the external field produced no effect with smaller vessels is that in this case the few ions in the vessel could be so easily removed by a small electric force that differences of potential accidentally present in the vessel were sufficient to remove the nuclei without the help of an additional electric field.

## CHAPTER VIII., p. 160.

H. A. Wilson has recently shown that the presence of even a very small quantity of hydrogen enormously increases the leak of negative electricity from an incandescent platinum wire. The part of the leak

which depends on the hydrogen increases less rapidly with the temperature than the part independent of the hydrogen, so that at very high temperatures the latter is the more important.

#### CHAPTER XI., p. 255.

The more recent determinations of the work required to ionise a molecule indicate a higher value than that given in the text. Thus Langevin (*Recherches sur les yaz ionises*) from the results of some experiments of Townsend's comes to the conclusion that the work done on the ionic charge in falling through a potential difference of 60 volts is a superior limit to the work required to ionise a molecule. Stark (*Drudes Ann.* iv. p. 411, 1901; vii. p. 421, 1902) obtains values ranging from 20 to 50 volts for the same quantity.

The effect of temperature on the ionisation of a gas by Röntgen rays has been lately investigated by McClung at the Cavendish Laboratory; he finds as the result of experiments made on gases at constant pressure and at constant density, that the amount of ionisation in a given number of molecules of a gas exposed to Röntgen rays is independent of the temperature, and is not, as Perrin thought, proportional to the absolute temperature. He finds also that the absorption of the rays by a given number of molecules is independent of the temperature of the molecules.

### CHAPTER XI., p. 258.

The fact that ionisation obeys the additive law points to the conclusion that it is an atomic property, so that the likelihood of an atom being ionised will depend upon the internal kinetic energy possessed by the atom; there are good reasons for thinking that the amount of this energy possessed by an atom as well as the number of atoms possessing a given amount of internal kinetic energy are to a very large extent independent of the temperature of the gas; if we take this view we can understand why the very small proportion of molecules ionised does not increase rapidly with the temperature.

# CHAPTER XI., p. 260.

Barkla (*Phil. May.* [6] v., p. 685, 1903) has made a very careful examination of the secondary Röntgen rays produced when the primary rays pass through a gas; he has shown that when the primary rays pass through different gases at the same pressure the intensity of the secondary radiation is proportional to the density of the gas. Thus

for example the intensity of the secondary radiation due to oxygen is to that from CO<sub>2</sub> as 32 is to 44. He finds too that the penetrating power of secondary radiation differs little, if at all, from that of the primary, so that the effect produced by the gas may be described as a scattering of the primary rays. Langevin (Recherches sur les gaz ionises) has investigated the secondary radiation produced when the primary rays fall upon a metallic surface, and has shown that the denser the metal the smaller the penetration of the secondary rays, and also that the penetrating power of the secondary rays increases with that of the primary.

#### CHAPTER XII., p. 290.

Rutherford and Soddy (*Phil. Mag.* [6] v., p. 576, 1903) give strong reasons for supposing that radio-activity is the result of the breaking up of the atom; thus the radium atom breaks up at first into the positively electrified particles which constitute the  $\alpha$  rays, the emanation, and possibly other substances; the emanation breaks up one of the products, being the substance which gives rise to induced radio-activity, this, as it is radio-active, breaks down again into products which, since they are not radio-active, have not been detected.

W. B. Hardy has recently shown that the rays from radium as well as Röntgen rays produced very marked reddish-brown coloration in a solution of iodoform in chloroform.

## CHAPTER XII., p. 302.

A very interesting account of the properties of radium will be found in the theses entitled *Recherches sur les substances radio-actives*, lately published by Mme. Curie.

Mme. Curie and Laborde have recently shown (Comptes Rendus, Mar. 16, 1903) that the salts of radium are the seat of a continuous development of heat which maintains them at a temperature considerably in their experiments (1.5° C.) above that of the surrounding heat. They found that the heat produced by 1 gramme of radium per hour is about 100 calories.

The existence of the  $\alpha$  radiation has been beautifully shown by Sir William Crookes by the following method: a small piece of a salt of radium is placed close to a screen of zinc blende; on examining the screen in a dark room by a lens it is seen to be dotted over with scintillating phosphorescent patches which are continually changing their places, these patches mark the spots where the screen is struck by the positively electrified  $\alpha$  rays.

#### CHAPTER XII., p. 322.

More recent experiments made by Debierne indicate that actinium is a distinct substance, as it has been found to give out an emanation whose activity lasts only for a few seconds; the induced radio-activity due to actinium is said to die away rather more slowly than that due to radium.

As the duration of the activity of a radio-active substance is the property by which it is most easily recognised it may be useful to give a table of the time taken for the activity to fall to half its value for those cases in which it has been determined.

Time taken for activity to fall to half its value.

Thorium emanation, 1 minute.

Induced activity due to thorium, 11 hours.

Radium emanation, 4 days.

Induced activity due to radium, 28 minutes.

Actinium emanation, a few seconds.

Induced activity due to actinium, rather less than 28 minutes.

Radio-active gas from water, 4 days.

Induced radio-activity due to this gas, about 40 minutes.

Induced radio-activity on a negatively

electrified wire in the open air, about 40 minutes.

The Curies have found that when bodies have been exposed for a long time to the radium emanation there is in addition to the radioactivity which disappears in 28 minutes a small residual activity which takes months to disappear.

### CHAPTER XII., p. 326.

Experiments recently made at the Cavendish Laboratory have shown that by far the greater part of the conductivity produced by bubbling air through water is due to the presence in the water of a radio-active gas. The amount of this gas varies much in different samples of water, in fresh deep well water from many parts of England I have found it in considerable quantity, while there is very little in surface or rain water. This gas is liberated when air is bubbled through the water, it can also be obtained by boiling the water, the gas expelled from water by boiling having very high conductivity. When once the gas has been drawn out of the water, subsequent boiling or bubbling produces very little conducting gas.

Mr Adams in some experiments made at the Cavendish Laboratory found that water after a rest of about a week recovered to some extent its power of giving off a radio-active gas, the maximum recovery amounting to about 10°/, of the gas initially present. independent existence of this gas was shown in the following way: a large quantity of highly conducting gas was liquefied at the Royal Institution by Professor Dewar, the liquid so obtained was allowed to evaporate and the gas coming off at the beginning of the evaporation and also at the very end when it was nearly completed collected and tested, the gas coming off at the beginning was found to have far less conductivity than the gas had before liquefaction while the gas left over at the end had about 30 times the original conductivity. The conductivity can also be taken out of the gas by passing it slowly through a tube immersed in liquid air. The radio-active gas resembles very closely the emanation from radium; its activity has been shown by Mr Adams to fall to one-half its original value in four days, the time taken for the same process in the radium emanation, the induced radio-activity due to the gas from water dies away to half its value in about 42 minutes, the same as that of a negatively electrified wire in air; according to Curie the time taken for the induced activity due to the radium emanation to fall to half its value is 28 minutes. I have also found that if to water from which the gas has been expelled, certain substances, notably finely powdered bricks, the blue clay from the Cambridge gault, or garden soil, are added, radio-active gas is again obtained by boiling or bubbling. I have not however by such means been able to get anything like the quantity of gas there is in Cambridge tap-water.

## CHAPTER XVIII., p. 525.

Blondlot has shown that the rays which affect the sparks in the experiment described on p. 525 are not Röntgen rays but a new type of ray which he calls N rays, these rays are emitted by incandescent burners as well as by sparks, they are refracted and are apparently of very long wave, some measured by Sagnac had a wave-length of  $\frac{1}{5}$  of a millimetre. The rays when they fall upon incandescent platinum increase its brightness without apparently increasing appreciably the average temperature of the glowing wire.

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